
pomegranate Documentation

Release 0.13.2

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pomegranate

pomegranate is a Python package that implements fast and flexible probabilistic models ranging from individual probability distributions to compositional models such as Bayesian networks and hidden Markov models. The core philosophy behind pomegranate is that all probabilistic models can be viewed as a probability distribution in that they all yield probability estimates for samples and can be updated given samples and their associated weights. The primary consequence of this view is that the components that are implemented in pomegranate can be stacked more flexibly than other packages. For example, one can build a Gaussian mixture model just as easily as building an exponential or log normal mixture model. But that's not all! One can create a Bayes classifier that uses different types of distributions on each features, perhaps modeling time-associated features using an exponential distribution and counts using a Poisson distribution. Lastly, since these compositional models themselves can be viewed as probability distributions, one can build a mixture of Bayesian networks or a hidden Markov model Bayes' classifier that makes predictions over sequences.

In addition to a variety of probability distributions and models, pomegranate has a variety of built-in features that are implemented for all of the models. These include different training strategies such as semi-supervised learning, learning with missing values, and mini-batch learning. It also includes support for massive data supports with out-of-core learning, multi-threaded parallelism, and GPU support.

CHAPTER 1

Thank You

No good project is done alone, and so I'd like to thank all the previous contributors to YAHMM, all the current contributors to pomegranate, and the many graduate students whom I have pestered with ideas and questions.

Contributions are eagerly accepted! If you would like to contribute a feature then fork the master branch and be sure to run the tests before changing any code. Let us know what you want to do on the issue tracker just in case we're already working on an implementation of something similar. Also, please don't forget to add tests for any new functions. Please review the [Code of Conduct](#) before contributing.

2.1 Installation

The easiest way to get pomegranate is through pip using the command

```
pip install pomegranate
```

This should install all the dependencies in addition to the package.

You can also get pomegranate through conda using the command

```
conda install pomegranate
```

This version may not be as up to date as the pip version though.

Lastly, you can get the bleeding edge from GitHub using the following commands:

```
git clone https://github.com/jmschrei/pomegranate
cd pomegranate
python setup.py install
```

On Windows machines you may need to download a C++ compiler if you wish to build from source yourself. For Python 2 this [minimal version of Visual Studio 2008](#) works well. For Python 3 this [version of the Visual Studio build tools](#) has been reported to work.

The requirements for pomegranate can be found in the requirements.txt file in the repository, and include numpy, scipy, networkx (v2.0 and above), joblib, cupy (if using a GPU), and cython (if building from source or on an Ubuntu machine).

2.1.1 FAQ

Q. I'm on a Windows machine and I'm still encountering problems. What should I do?

A. If those do not work, it has been suggested that <https://wiki.python.org/moin/WindowsCompilers> may provide more information. Note that your compiler version must fit your python version. Run `python -version` to tell which python version you use. Don't forget to select the appropriate Windows version API you'd like to use. If you get an error message "ValueError: Unknown MS Compiler version 1900" remove your Python's `Lib/distutils/distutil.cfg` and retry. See <http://stackoverflow.com/questions/34135280/valueerror-unknown-ms-compiler-version-1900> for details.

Q. I've been getting the following error: ``ModuleNotFoundError: No module named 'pomegranate.utils'.``

A. A reported solution is to uninstall and reinstall without cached files using the following:

```
pip uninstall pomegranate
pip install pomegranate --no-cache-dir
```

If that doesn't work for you, you may need to downgrade your version of numpy to 1.11.3 and try the above again.

Q. I've been getting the following error: ``MarkovChain.so: unknown file type, first eight bytes: 0x7F 0x45 0x4C 0x46 0x02 0x01 0x01 0x00.``

A. This can be fixed by removing the `.so` files from the pomegranate installation or by building pomegranate from source.

Q. I'm encountering some other error when I try to install pomegranate.

A. pomegranate has had some weird linker issues, particularly when users try to upgrade from an older version. In the following order, try:

1. Uninstalling pomegranate using pip and reinstalling it with the option `--no-cache-dir`, like in the above question.
2. Removing all pomegranate files on your computer manually, including egg and cache files that cython may have left in your `site-packages` folder
3. Reinstalling the Anaconda distribution (usually only necessary in issues where `libfortran` is not linking properly)

2.2 Code of Conduct

2.2.1 Our Pledge

In the interest of fostering an open and welcoming environment, we as contributors and maintainers pledge to making participation in our project and our community a harassment-free experience for everyone, regardless of age, body size, disability, ethnicity, gender identity and expression, level of experience, nationality, personal appearance, race, religion, or sexual identity and orientation.

2.2.2 Our Standards

Examples of behavior that contributes to creating a positive environment include:

- Using welcoming and inclusive language
- Being respectful of differing viewpoints and experiences
- Gracefully accepting constructive criticism

- Focusing on what is best for the community
- Showing empathy towards other community members

Examples of unacceptable behavior by participants include:

- The use of sexualized language or imagery and unwelcome sexual attention or advances
- Trolling, insulting/derogatory comments, and personal or political attacks
- Public or private harassment
- Publishing others' private information, such as a physical or electronic address, without explicit permission
- Other conduct which could reasonably be considered inappropriate in a professional setting

2.2.3 Our Responsibilities

Project maintainers are responsible for clarifying the standards of acceptable behavior and are expected to take appropriate and fair corrective action in response to any instances of unacceptable behavior.

Project maintainers have the right and responsibility to remove, edit, or reject comments, commits, code, wiki edits, issues, and other contributions that are not aligned to this Code of Conduct, or to ban temporarily or permanently any contributor for other behaviors that they deem inappropriate, threatening, offensive, or harmful.

2.2.4 Scope

This Code of Conduct applies both within project spaces and in public spaces when an individual is representing the project or its community. Examples of representing a project or community include using an official project e-mail address, posting via an official social media account, or acting as an appointed representative at an online or offline event. Representation of a project may be further defined and clarified by project maintainers.

2.2.5 Enforcement

Instances of abusive, harassing, or otherwise unacceptable behavior may be reported by contacting the project team at jmschreiber91@gmail.com. Because the project team currently consists of only one member, that member shall investigate within one week whether a violation of the code of conduct occurred and what the appropriate response is. That member shall then contact the original reporter and any other affected parties to explain the response and note feedback for the record. The project team is obligated to maintain confidentiality with regard to the reporter of an incident. Should you wish to file a report anonymously you should fill out a report at <https://goo.gl/forms/aQtIDdrhZf4Y8flk2>. If your report involves any members of the project team, if you feel uncomfortable making a report to the project team for any reason, or you feel that the issue has not been adequately handled, you are encouraged to send [your report](mailto:yourreport@conduct@numfocus.org) to conduct@numfocus.org where it will be independently reviewed by the NumFOCUS team.

Project maintainers who do not follow or enforce the Code of Conduct in good faith may face temporary or permanent repercussions as determined by other members of the project's leadership.

2.2.6 Attribution

This Code of Conduct is adapted from the [Contributor Covenant homepage](#), version 1.4.

For answers to common questions about this code of conduct, see <https://www.contributor-covenant.org/faq>.

2.3 FAQ

Can I create a usable model if I already know the parameters I want, but don't have data to fit to?

Yes! pomegranate has two ways of initializing models, either by starting off with pre-initialized distributions or by using the `Model.from_samples` class method. In the case where you have a model that you'd like to use you can create the model manually and use it to make predictions without the need to fit it to data.

How do I create a model directly from data?

pomegranate attempts to closely follow the scikit-learn API. However, a major area in which it diverges is in the initialization of models directly from data. Typically in scikit-learn one would create an estimator and then call the `fit` function on the training data. In pomegranate one would use the `Model.from_samples` class method, such as `BayesianNetwork.from_samples(X)`, to learn a model directly from data.

My data set has missing values. Can I use pomegranate?

Yes! pomegranate v0.9.0 merged missing value support. This means that you can learn models and run inference on data sets that have missing values just as easily as if they were fully observed. Indicate that a value is missing using either `numpy.nan` for numeric data sets or `'nan'` in string data sets.

What is the difference between "fit" and "from_samples"?

The `fit` method trains an initialized model, whereas the `from_samples` class method will first initialize the model and then train it. These are separated out because frequently a person already knows a good initialization, such as the structure of the Bayesian network but maybe not the parameters, and wants to fine-tune that initialization instead of learning everything directly from data. This also simplifies the backend by allowing the `fit` function to assume that the model is initialized instead of having to check to see if it is initialized, and if not then initialize it. This is particularly useful in structured models such as Bayesian networks or hidden Markov models where the `Model.from_samples` task is really structure learning + parameter learning, because it allows the `fit` function to be solely parameter learning.

How can I use pomegranate for semi-supervised learning?

When using one of the supervised models (such as naive Bayes or Bayes classifiers) simply pass in the label -1 for samples that you do not have a label for.

How can I use out-of-core learning in pomegranate?

Once a model has been initialized the `summarize` method can be used on arbitrarily sized chunks of the data to reduce them into their sufficient statistics. These sufficient statistics are additive, meaning that if they are calculated for all chunks of a dataset and then added together they can yield exact updates. Once all chunks have been summarized then `from_summaries` is called to update the parameters of the model based on these added sufficient statistics. Out-of-core computing is supported by allowing the user to load up chunks of data from memory, summarize it, discard it, and move on to the next chunk.

Does pomegranate support parallelization?

Yes! pomegranate supports parallelized model fitting and model predictions, both in a data-parallel manner. Since the backend is written in cython the global interpreter lock (GIL) can be released and multi-threaded training can be supported via joblib. This means that parallelization is utilized time isn't spent piping data from one process to another nor are multiple copies of the model made.

Does pomegranate support GPUs?

Currently pomegranate does not support GPUs.

Does pomegranate support distributed computing?

Currently pomegranate is not set up for a distributed environment, though the pieces are currently there to make this possible.

How can I cite pomegranate?

The research paper that presents pomegranate is:

Schreiber, J. (2018). Pomegranate: fast and flexible probabilistic modeling in python. Journal of Machine Learning Research, 18(164), 1-6.

which can be downloaded from [JML](#) or from [arXiv](#).

The paper can be cited as:

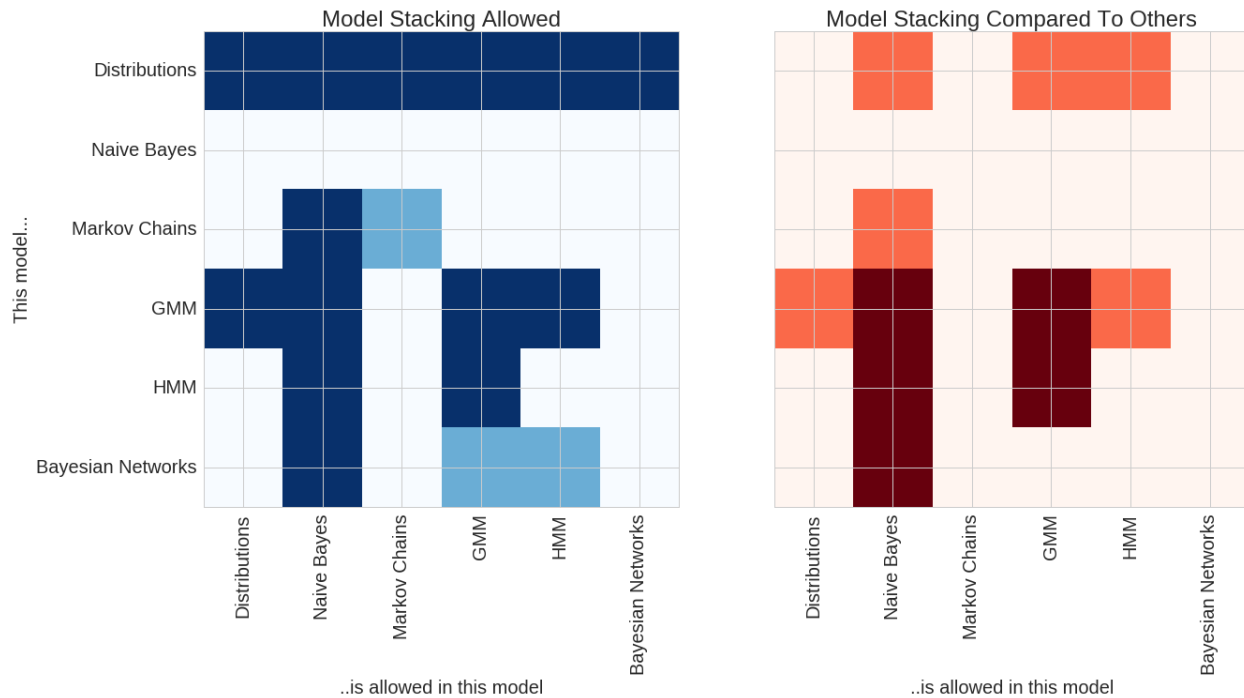
```
@article{schreiber2018pomegranate,
  title={Pomegranate: fast and flexible probabilistic modeling in python},
  author={Schreiber, Jacob},
  journal={Journal of Machine Learning Research},
  volume={18},
  number={164},
  pages={1--6},
  year={2018}
}
```

Alternatively, the GitHub repository can be cited as:

```
@misc{Schreiber2016,
  author = {Jacob Schreiber},
  title = {pomegranate},
  year = {2016},
  publisher = {GitHub},
  journal = {GitHub repository},
  howpublished = {\url{https://github.com/jmschrei/pomegranate}},
  commit = {enter commit that you used}
}
```

How does pomegranate compare to other packages?

A comparison of the features between pomegranate and others in the python ecosystem can be seen in the following two plots.



The plot on the left shows model stacks which are currently supported by pomegranate. The rows show each model, and the columns show which models those can fit in. Dark blue shows model stacks which currently are supported, and light blue shows model stacks which are currently being worked on and should be available soon. For example, all models use basic distributions as their main component. However, general mixture models (GMMs) can be fit into both Naive Bayes classifiers and hidden Markov models (HMMs). Conversely, HMMs can be fit into GMMs to form mixtures of HMMs. Soon pomegranate will support models like a mixture of Bayesian networks.

The plot on the right shows features compared to other packages in the python ecosystem. Dark red indicates features which no other package supports (to my knowledge!) and orange shows areas where pomegranate has an expanded feature set compared to other packages. For example, both pomegranate and sklearn support Gaussian naive Bayes classifiers. However, pomegranate supports naive Bayes of arbitrary distributions and combinations of distributions, such as one feature being Gaussian, one being log normal, and one being exponential (useful to classify things like ionic current segments or audio segments). pomegranate also extends naive Bayes past its “naivety” to allow for features to be dependent on each other, and allows input to be more complex things like hidden Markov models and Bayesian networks. There’s no rule that each of the inputs to naive Bayes has to be the same type though, allowing you to do things like compare a markov chain to a HMM. No other package supports a HMM Naive Bayes! Packages like hmmlearn support the GMM-HMM, but for them GMM strictly means Gaussian mixture model, whereas in pomegranate it ~can~ be a Gaussian mixture model, but it can also be an arbitrary mixture model of any types of distributions. Lastly, no other package supports mixtures of HMMs despite their prominent use in things like audio decoding and biological sequence analysis.

Models can be stacked more than once, though. For example, a “naive” Bayes classifier can be used to compare multiple mixtures of HMMs to each other, or compare a HMM with GMM emissions to one without GMM emissions. You can also create mixtures of HMMs with GMM emissions, and so the most stacking currently supported is a “naive” Bayes classifier of mixtures of HMMs with GMM emissions, or four levels of stacking.

How can pomegranate be faster than numpy?

pomegranate has been shown to be faster than numpy at updating univariate and multivariate gaussians. One of the reasons is because when you use numpy you have to use `numpy.mean(X)` and `numpy.cov(X)` which requires two full passes of the data. pomegranate uses additive sufficient statistics to reduce a dataset down to a fixed set of numbers which can be used to get an exact update. This allows pomegranate to calculate both mean and covariance in a single pass of the dataset. In addition, one of the reasons that numpy is so fast is its use of BLAS. pomegranate also

uses BLAS, but uses the cython level calls to BLAS so that the data doesn't have to pass between cython and python multiple times.

2.4 Release History

2.4.1 Version 0.13.0

Highlights

- A variety of minor bug fixes and speed improvements
- You can now pass in key sets to each model to define distributions over, even if that symbol doesn't occur in the training set
- The returns from *from_sample* uses class distributions instead of predefined ones, allowing for inheritance of distributions
- Checks added to ensure that input arrays are C ordered instead of transposed

Distributions

- JSON dtypes are checked to be numpy types instead of assumed to be
- `__eq__` and `__mul__` sped up for DiscreteDistributions

BayesianNetwork

- Fixed bug with constraint graphs when a node has both self loop and parent constraints

MarkovChains

- Fixed an issue with sampling length.

2.4.2 Version 0.12.1

Highlights

- A variety of minor bug fixes.

2.4.3 Version 0.12.0

Highlights

- MarkovNetwork models have been added in and include both inference and structure learning.
- Support for Python 2 has been deprecated.
- Markov network, data generator, and callback tutorials have been added in
- A robust *from_json* method has been added in to `__init__.py` that can deserialize JSONs from any pomegranate model.

MarkovNetwork

- MarkovNetwork models have been added in as a new probabilistic model.
- Loopy belief propagation inference has been added in using the FactorGraph backend
- Structure learning has been added in using Chow-Liu trees

BayesianNetwork

- Chow-Liu tree building has been sped up slightly, courtesy of @alexhenrie
- Chow-Liu tree building was further sped up by almost an order of magnitude
- Constraint Graphs no longer fail when passing in graphs with self loops, courtesy of @alexhenrie

BayesClassifier

- Updated the *from_samples* method to accept BayesianNetwork as an emission. This will build one Bayesian network for each class and use them as the emissions.

Distributions

- Added a warning to DiscreteDistribution when the user passes in an empty dictionary.
- Fixed the sampling procedure for JointProbabilityTables.
- GammaDistributions should have their shape issue resolved
- The documentation for BetaDistributions has been updated to specify that it is a Beta-Bernoulli distribution.

io

- New file added, io.py, that contains data generators that can be operated on
- Added DataGenerator, DataFrameGenerator, and a BaseGenerator class to inherit from

HiddenMarkovModel

- Added RandomState parameter to *from_samples* to account for randomness when building discrete models.

Misc

- Unnecessary calls to memset have been removed, courtesy of @alexhenrie
- Checking for missing values has been slightly refactored to be cleaner, courtesy of @mareksmid-lucid
- Include the LICENSE file in MANIFEST.in and simplify a bit, courtesy of @toddrme2178
- Added in a robust from_json method that can be used to deserialize a JSON for any pomegranate model.

docs

- Added io.rst to briefly describe data generators
- Added MarkovNetwork.rst to describe Markov networks
- Added links to tutorials that did not have tutorials linked to them.

Tutorials

- Added in a tutorial notebook for Markov networks
- Added in a tutorial notebook for data generators
- Added in a tutorial notebook for callbacks

CI

- Removed unit tests for Py2.7 from AppVeyor and Travis
- Added unit tests for Py3.8 to AppVeyor and Travis

2.4.4 Version 0.11.2

Highlights

- Faster BSNL, particularly when there is missing data, courtesy of @alexhenrie
- GPU acceleration should be fixed

BayesianNetwork

- A speed improvement by making *isnan* an inline function, courtesy of @alexhenrie
- A speed improvement by changing the manner that parent sets are iterated, courtesy of @alexhenrie

Utils

- The *enable_gpu* call has been moved to the bottom of the GPU checking code and so should not crash anymore.

2.4.5 Version 0.11.1

Highlights

- Added speed improvements to Bayesian network structure learning when missing data is present.

BayesianNetwork

- By default duplicates get merged in a data set so that there are fewer rows with larger weights, dramatically improving speed. However, because `np.nan != np.nan`, rows with missing values don't get merged. This fix changes `np.nan` to `None` so that the rows get merged appropriately.
- A few misc changes that sometimes improve speed.
- Changed the probability calculation when a node is being scored given a single row. Previously it would return 0, meaning that sometimes it will return the densest graph possible erroneously. This may change your networks in edge cases, but will reduce their complexity.

2.4.6 Version 0.11.0

Highlights

- Allowed for user specified custom distributions by implementing a Python fallback option if the distribution object doesn't inherit from the base distribution class.
- Fixed an issue with GammaDistribution update
- Removed deterministic seed being set in `hmm.bake`
- Made pomegranate compatible with NetworkX v2.0 and above
- NeuralHMMs and Neural Mixture Models are now possible through the custom distributions
- Many new tutorials

Distributions

- Fixed an error in GammaDistribution's cython level update step where sufficient statistics were incorrectly collected from a data set. This will only affect GammaDistributions that are used as part of a composition model rather than stand-alone ones.
- Added in support for custom distributions. This is done by checking whether a distribution is inherited from the base pomegranate distribution object. If not, it will use the python methods.
- Added in examples of using custom distributions, including neural networks, with pomegranate models.
- Made `NormalDistribution.blank` and `LogNormalDistribution.blank` return distributions with a standard deviation of 1, to avoid `DivisionByZero` errors.
- Added in a `NeuralNetworkWrapper` distribution that should handle wrapping a neural network correctly for use in pomegranate. This assumes a keras-like API.

HiddenMarkovModel

- Removed a deterministic seed being set in `hmm.bake`. These lines were set because it was thought that there was some randomness in either the internal state generation of the topological sort. However, it appears that this is not necessary, and so it has been removed.
- Fixed a bug where semi-supervised learning would not work because of an undefined variable.
- Added in support for networkx v2.0 and above using their new API.

Tutorials

- Revamped the tutorials in the tutorials folder, greatly expanding their scope
- Added in new tutorials about custom distributions and neural probabilistic models

2.4.7 Version 0.10.0

Highlights

- Broke distributions into their own files and placed them in their own folder
- Fixed Bayesian network failing in call to `np.isnan` when fitting to character data
- Added in callbacks to all models in the style of keras, with built-ins being `History`, `ModelCheckpoint`, and `CVLogger`. History is calculated for each model. Use `return_history=True` to get the model and the history object that contains training.
- Added top-level Makefile for convenience in development to `build/test/clean/install/uninstall` with multiple conda environments.
- Added top-level `rebuildconda` for convenience in development to create or re-create a conda development environment for a given python version, defaulting to 2.7.

Changelog

Callbacks

- Added in a callbacks module, and the use of callbacks in all iterative training procedures. Callbacks are called at the beginning of training, at the end of each epoch, and at the end of the training procedure, using the respective functions. See the documentation page for more details.

Distributions

- Broke the `distributions.pyx` into a folder where each distribution has its own file. This will speed up compilation when the code is modified.
- Added in a `dtype` attribute to `DiscreteDistribution`, `ConditionalProbabilityTable`, and `JointProbabilityTable`, to prevent automatic casting of keys as floats when converting to and from jsons
- For `MultivariateGaussianDistributions`, added in an epsilon when performing a ridge adjustment on a non-positive semidefinite matrix to hopefully completely fix this issue.
- `NormalDistribution` update should now check to see if the weights are below an epsilon, rather than equal to 0, resolving some stability issues.
- Fixed an issue with `BernoulliDistribution` where it would raise a `ZeroDivisionError` when `from_summaries` was called with no observations.
- Fixed an issue where an `IndependentComponentsDistribution` would print upon calls to `log_probability`

HiddenMarkovModel

- Changed the output to be the fit model, like in scikit-learn, instead of the total improvement, to allow for chaining
 - Added in callback functionality to both the `fit` and `from_samples` methods

- Added in the *return_history* parameter to both the *fit* and *from_samples* methods, which will return the history callback as well as the fit model
- Resolved an issue in the *summary* method where default weights were assigned to the wrong variable when not passed in.
- Resolved an issue where printing an empty model resulted in an error.

GeneralMixtureModel

- Changed the output to be the fit model, like in scikit-learn, instead of the total improvement, to allow for chaining
 - Added in callback functionality to both the *fit* and *from_samples* methods
 - Added in the *return_history* parameter to both the *fit* and *from_samples* methods, which will return the history callback as well as the fit model

NaiveBayes

- Added in callback functionality to both the *fit* and *from_samples* methods that will be used only in semi-supervised learning
- Added in the *return_history* parameter to both the *fit* and *from_samples* methods, which will return the history callback as well as the fit model that will be used only in semi-supervised learning

BayesClassifier

- Added in callback functionality to both the *fit* and *from_samples* methods that will be used only in semi-supervised learning
- Added in the *return_history* parameter to both the *fit* and *from_samples* methods, which will return the history callback as well as the fit model that will be used only in semi-supervised learning

BayesianNetwork

- Modified the built keymap to be a numpy array of objects to prevent casting of all keys as the type of the first column.

Makefile

- There is a new top-level “convenience” Makefile for development to make it easy to develop with two conda environments. The default is for two conda environments, py2.7 and py3.6, but those could be overridden at run time with, for example, *make PY3_ENV=py3.6.2 biginstall*. Targets exist for *install*, *test*, *bigclean*, and *nbtest* along with variations of each that first activate either one or both conda environments. For example, *make biginstall* will install for both *py2.7* and *py3.6* environments. When developing pomegranate, one frequently wants to do a fully clean build, wipe out all installed targets, and replace them. This can be done with *make bigclean biguninstall biginstall*. In addition, there is a target *nbtest* for testing all of the jupyter notebooks to ensure that the cells run. See the Makefile for a list of additional conda packages to install for this to work. The default is to stop on first error but you can run *make ALLOW_ERRORS=-allow-errors nbtest* to run all cells and then inspect the html output manually for errors.
- There is a new top-level “convenience” *rebuildconda* script which will remove and create a conda environment for development. Be careful using it that the environment you want to rebuild is the right one. You can list environments with *conda info -envs*. The default is to rebuild the 2.7 environment with name *py2.7*. With

this, you can create an alternative environment, test it out, and remove it as in `./rebuildconda 2.7.9 ; make PY2_ENV=py2.7.9 bigclean py2build py2test py2install nbtest ; source deactivate ; conda env remove --name py2.7.9`.

2.4.8 Version 0.9.0

Highlights

- Missing value support has been added in for all models except factor graphs. This is done by included the string `nan` in string datasets, or `numpy.nan` in numeric datasets. Model fitting and inference is supported for all models for this. The technique is to not collect sufficient statistics from missing data, not to impute the missing values.
- The unit testing suite has been greatly expanded, from around 140 tests to around 370 tests.

Changelog

HiddenMarkovModel

- The documentation has been fixed so that states are defined as `State(NormalDistribution(0, 1))` instead of incorrectly as `State(Distribution(NormalDistribution(0, 1)))`
- Fixed a bug in `from_samples` that was causing a `TypeError` if `name` was not specified when using `DiscreteDistribution` with custom labels.
- Expanded the number of unit tests to include missing value support and be more comprehensive

Distributions

- Multivariate Gaussian distributions have had their parameter updates simplified. This doesn't lead to a significant change in speed, just less code.
- Fixed an issue where Poisson Distributions had an overflow issue caused when calculating large factorials by moving the log inside the product.
- Fixed an issue where Poisson Distributions were not correctly calculating the probability of 0 counts.
- Fixed an issue where Exponential Distribution would fail when fed integer 0-mode data.
- Fixed an issue where IndependentComponentDistribution would have incorrect per-dimension weights after serialization.
- Added in missing value support for fitting and log probability calculations for all univariate distributions, ICD, MGD, and CPTs through calculating sufficient statistics only on data that exists. The only distributions that currently do not support missing values are `JointProbabilityTables` and `DirichletDistributions`.
- Fixed an issue with multivariate Gaussian distributions where the covariance matrix is no longer invertible with enough missing data by subtracting the smallest eigenvalue from the diagonal

K-Means

- Added in missing value support for k-means clustering by ignoring dimensions that are missing in the data. Can now fit and predict on missing data.
- Added in missing value support for all initialization strategies
- Added in a suite of unit tests

- Added in the *distance* method that returns the distance between each point and each centroid

GeneralMixtureModel

- Added in missing value support for mixture models through updates to the distributions
- Fixed an issue where passing in a list of distributions to *from_samples* along with a number of components did not produce a mixture of IndependentComponentsDistribution objects
- Expanded the unit test suite and added tests for missing value support

BayesianNetwork

- Vectorized the *predict_proba* method to take either a single sample or a list of samples
- Changed the output of *predict_proba* to be individual symbols instead of a distribution where one symbol has a probability of 1 when fed in as known prior knowledge.
- Added in an *n_jobs* parameter to parallelize the prediction of samples. This does not speed up a single sample, only a batch of samples.
- Factored out *_check_input* into a function that be used independently
- Added unit tests to check each of the above functions extensively
- Missing value support added for the *log_probability*, *fit*, and *from_samples* methods. Chow-Liu trees are not supported for missing values, but using a constraint graph still works.

2.4.9 Version 0.8.1

Highlights

This will serve as a log for the changes added for the release of version 0.8.1.

- Univariate offsets have been added to allow for distributions to be fit to a column of data rather than a vector of numbers. This stops the copying of data that had to be done previously.

Changelog

Base

- Parameters *column_idx* and *d* have been added to the *_summarize* method that all models expose. This is only useful for univariate distributions and models that fit univariate distributions and can be ignored by other models. The *column_idx* parameter specifies which column in a data matrix the distribution should be fit to, essentially serving as an offset. *d* refers to the number of dimensions that the data matrix has. This means that a univariate distribution will fit to all samples *i* such that $i*d + column_idx$ in a pointer array. Multivariate distributions and models using those can ignore this.
- A convenience function *to_yaml* was added to *State* and *Model* classes. *YAML* is a superset of *JSON* that can be 4 to 5 times more compact. You need the *yaml* package installed to use it.

Distributions

- The *summarize* method has been moved from most individual distributions to the *Distribution* base object, as has the *fit* method.
- *min_std* has been moved from the *from_summaries* method and the *fit* method to the *__init__* method for the *NormalDistribution* and *LogNormalDistribution* objects.

NaiveBayes

- Moved the *fit* and *summarize* methods to *BayesModel* due to their similarity with *BayesClassifier*

BayesClassifier

- Moved the *fit* and *summarize* methods to *BayesModel* due to their similarity to *NaiveBayes*

GeneralMixtureModel

- Fixed a bug where *n_jobs* was ignored in the *from_samples* method because *batch_size* was reset for the k-means initialization

HiddenMarkovModel

- The default name of a *HiddenMarkovModel* has been changed from “None” to “HiddenMarkovModel”

2.4.10 Version 0.8.0

Highlights

This will serve as a log for the changes added for the release of version 0.8.0.

Changelog

k-means

- k-means has been changed from using iterative computation to using the alternate formulation of euclidean distance, from $\|a - b\|^2$ to using $\|a\|^2 + \|b\|^2 - 2\|a \cdot b\|$. This allows for the centroid norms to be cached, significantly speeding up computation, and for *dgemm* to be used to solve the matrix matrix multiplication. Initial attempts to add in GPU support appeared unsuccessful, but in theory it should be something that can be added in.
- k-means has been refactored to more natively support an out-of-core learning goal, by allowing for data to initially be cast as numpy memorymaps and not coercing them to arrays midway through.

Hidden Markov Models

- Allowed labels for labeled training to take in string names of the states instead of the state objects themselves.
- Added in *state_names* and *names* parameters to the *from_samples* method to allow for more control over the creation of the model.
- Added in semi-supervised learning to the *fit* step that can be activated by passing in a list of labels where sequences that have no labels have a *None* value. This allows for training to occur where some sequences are fully labeled and others have no labels, not for training to occur on partially labeled sequences.
- Supervised initialization followed by semi-supervised learning added in to the *from_samples* method similarly to other methods. One should do this by passing in string labels for state names, always starting with `<model_name>-start`, where *model_name* is the *name* parameter passed into the *from_samples* method. Sequences that do not have labels should have a *None* instead of a list of corresponding labels. While semi-supervised learning using the *fit* method can support arbitrary transitions amongst silent states, the *from_samples* method does not produce silent states, and so other than the start and end states, all states should be symbol emitting states. If using semi-supervised learning, one must also pass in a list of the state names using the *state_names* parameter that has been added in.
- Fixed bug in supervised learning where it would not initialize correctly due to an error in the semi-supervised learning implementation.
- Fixed bug where model could not be plotted without pygraphviz due to an incorrect call to `networkx.draw`.

General Mixture Models

- Changed the initialization step to be done on the first batch of data instead of the entire dataset. If the entire dataset fits in memory this does not change anything. However, this allows for out-of-core updates to be done automatically instead of immediately trying to load the entire dataset into memory. This does mean that out-of-core updates will have a different initialization now, but then yield exact updates after that.
- Fixed bug where passing in a 1D array would cause an error by recasting all 1D arrays as 2D arrays.

Bayesian Networks

- Added in a *reduce_dataset* parameter to the *from_samples* method that will take in a dataset and create a new dataset that is the unique set of samples, weighted by their weighted occurrence in the dataset. Essentially, it takes a dataset that may have repeating members, and produces a new dataset that is entirely unique members. This produces an identically scoring Bayesian network as before, but all structure learning algorithms can be significantly sped up. This speed up is proportional to the redundancy of the dataset, so large datasets on a smallish (< 12) number of variables will see massive speed gains (sometimes even 2-3 orders of magnitude!) whereas past that it may not be beneficial. The redundancy of the dataset (and thus the speedup) can be estimated as $n_samples / n_possibilities$, where *n_samples* is the number of samples in the dataset and *n_possibilities* is the product of the number of unique keys per variable, or 2^{*d} for binary data with *d* variables. It can be calculated exactly as $n_samples / n_unique_samples$, as many datasets are biased towards repeating elements.
- Fixed a premature optimization where the parents were stripped from conditional probability tables when saving the Bayesian Network to a json, causing an error in serialization. The premature optimization is that in theory pomegranate is set up to handle cyclic Bayesian networks and serializing that without first stripping parents would cause an infinite file size. However, a future PR that enabled cyclic Bayesian networks will account for this error.

Naive Bayes

- Fixed documentation of *from_samples* to actually refer to the naive Bayes model.
- Added in semi-supervised learning through the EM algorithm for samples that are labeled with -1.

Bayes Classifier

- Fixed documentation of *from_samples* to actually refer to the Bayes classifier model.
- Added in semi-supervised learning through the EM algorithm for samples that are labeled with -1.

Distributions

- Multivariate Gaussian Distributions can now use GPUs for both log probability and summarization calculations, speeding up both tasks ~4x for any models that use them. This is added in through CuPy.

Out Of Core

- The parameter “batch_size” has been added to HMMs, GMMs, and k-means models for built-in out-of-core calculations. Pass in a numpy memory map instead of an array and set the batch size for exact updates (sans initialization).

Minibatching

- The parameter “batches_per_epoch” has been added to HMMs, GMMs, and k-means models for build-in mini-batching support. This specifies the number of batches (as defined by “batch_size”) to summarize before calculating new parameter updates.
- The parameter “lr_decay” has been added to HMMs and GMMs that specifies the decay in the learning rate over time. Models may not converge otherwise when doing minibatching.

Parallelization

- *n_jobs* has been added to all models for both fitting and prediction steps. This allows users to make parallelized predictions with their model without having to do anything more complicated than setting a larger number of jobs.

Tutorials

- Removed the PyData 2016 Chicago Tutorial due to it’s similarity to `tutorials_0_pomegranate_overview`.

2.5 The API

pomegranate has a minimal core API that is made possible because all models are treated as a probability distribution regardless of complexity. Regardless of whether it’s a simple probability distribution, or a hidden Markov model that uses a different probability distribution on each feature, these methods can be used. Each model documentation page

has an API reference showing the full set of methods and parameters for each method, but generally all models have the following methods and parameters for the methods.

```
>>> model.probability(X)
```

This method will take in either a single sample and return its probability, or a set of samples and return the probability of each one, given the model.

```
>>> model.log_probability(X)
```

The same as above but returns the log of the probability. This is helpful for numeric stability.

```
>>> model.fit(X, weights=None, inertia=0.0)
```

This will fit the model to the given data with optional weights. If called on a mixture model or a hidden Markov model this runs expectation-maximization to perform iterative updates, otherwise it uses maximum likelihood estimates. The shape of data should be (n, d) where n is the number of samples and d is the dimensionality, with weights being a vector of non-negative numbers of size (n,) when passed in. The inertia shows the proportion of the prior weight to use, defaulting to ignoring the prior values.

```
>>> model.summarize(X, weights=None)
```

This is the first step of the two step out-of-core learning API. It will take in a data set and optional weights and extract the sufficient statistics that allow for an exact update, adding to the cached values. If this is the first time that summarize is called then it will store the extracted values, if it's not the first time then the extracted values are added to those that have already been cached.

```
>>> model.from_summaries(inertia=0.0)
```

This is the second step in the out-of-core learning API. It will use the extracted and aggregated sufficient statistics to derive exact parameter updates for the model. Afterwards it will reset the stored values.

```
>>> model.clear_summaries()
```

This method clears whatever summaries are left on the model without updating the parameters.

```
>>> Model.from_samples(X, weights=None)
```

This method will initialize a model to a data set. In the case of a simple distribution it will simply extract the parameters from the case. In the more complicated case of a Bayesian network it will jointly find the best structure and the best parameters given that structure. In the case of a hidden Markov model it will first find clusters and then learn a dense transition matrix.

2.5.1 Compositional Methods

These methods are available for the compositional models, i.e., mixture models, hidden Markov models, Bayesian networks, naive Bayes classifiers, and Bayes' classifiers. These methods perform inference on the data. In the case of Bayesian networks it will use the forward-backward algorithm to make predictions on all variables for which values are not provided. For all other models, this will return the model component that yields the highest posterior P(MID) for some sample. This value is calculated using Bayes' rule, where the likelihood of each sample given each component multiplied by the prior of that component is normalized by the likelihood of that sample given all components multiplied by the prior of those components.

```
>>> model.predict(X)
```

This will return the most likely value for the data. In the case of Bayesian networks this is the most likely value that the variable takes given the structure of the network and the other observed values. In the other cases it is the model component that most likely explains this sample, such as the mixture component that a sample most likely falls under, or the class that is being predicted by a Bayes' classifier.

```
>>> model.predict_proba(X)
```

This returns the matrix of posterior probabilities $P(M|D)$ directly. The predict method is simply running argmax over this matrix.

```
>>> model.predict_log_proba(X)
```

This returns the matrix of log posterior probabilities for numerical stability.

2.6 Out of Core Learning

- [IPython Notebook Tutorial](#)

Sometimes datasets which we'd like to train on can't fit in memory but we'd still like to get an exact update. pomegranate supports out of core training to allow this, by allowing models to summarize batches of data into sufficient statistics and then later on using these sufficient statistics to get an exact update for model parameters. These are done through the methods `model.summarize`` and `model.from_summaries``. Let's see an example of using it to update a normal distribution.

```
>>> from pomegranate import *
>>> import numpy
>>>
>>> a = NormalDistribution(1, 1)
>>> b = NormalDistribution(1, 1)
>>> X = numpy.random.normal(3, 5, size=(5000,))
>>>
>>> a.fit(X)
>>> a
{
  "frozen" :false,
  "class" : "Distribution",
  "parameters" :[
    3.012692830297519,
    4.972082359070984
  ],
  "name" : "NormalDistribution"
}
>>> for i in range(5):
>>>     b.summarize(X[i*1000:(i+1)*1000])
>>> b.from_summaries()
>>> b
{
  "frozen" :false,
  "class" : "Distribution",
  "parameters" :[
    3.01269283029752,
    4.972082359070983
  ],
  "name" : "NormalDistribution"
}
```

This is a simple example with a simple distribution, but all models and model stacks support this type of learning. Lets next look at a simple Bayesian network.

We can see that before fitting to any data, the distribution in one of the states is equal for both. After fitting the first distribution they become different as would be expected. After fitting the second one through summarize the distributions become equal again, showing that it is recovering an exact update.

2.6.1 FAQ

Q. How many examples should I summarize at a time?

A. You should summarize the largest amount of data that fits in memory. The larger the block of data, the more efficient the calculations can be, particularly if GPU computing is being used.

Q. Can I still do multi-threading / use a GPU with out-of-core learning?

A. Absolutely. You will have to call `joblib` yourself if you use the formulation above but the computational aspects of the call to summarize have the GIL released and so multi-threading can be used.

Q. Does out of core learning give exact or approximate updates?

A. It gives exact updates as long as the total set of examples that are summarized is the same. Sufficient statistics are collected for each of the batches and are equal to the sufficient statistics that one would get from the full dataset. However, the initialization step is done on only a single batch. This may cause the final models to differ due simply to the different initializations. If one has pre-defined initializations and simply calls `fit`, then the exact same model will be yielded.

2.7 Data Generators and IO

- [IPython Notebook Tutorial](#)

The main way that data is fed into most Python machine learning models is formatted as numpy arrays. However, there are some cases where this is not convenient. The first case is when the data doesn't fit into memory. This case was dealt with a little bit in the Out of Core documentation page. The second case is when the data lives in some other format, such as a CSV file or some type of data base, and one doesn't want to create an entire copy of the data formatted as a numpy array.

Fortunately, pomegranate supports the use of data generators as input rather than only taking in numpy arrays. Data generators are objects that wrap data sets and yield batches of data in a manner that is specified by the user. Once the generator is exhausted the epoch is ended. The default data generator is to yield contiguous chunks of examples of a certain batch size until the entire data set has been seen, finish the epoch, and then start over.

The strength of data generators is that they allow the user to have a much greater degree of control over the training process than hardcoding a few training schemes. By specifying how exactly a batch is generated from the data set (and the preprocessing that might go into converting examples for use by the model) and exactly when an epoch ends, users can do a wide variety of out-of-core and mini-batch training schemes without anything needed to be built-in to pomegranate.

See the tutorial for more information about how to use and define your own data generators.

2.8 Semi-Supervised Learning

Semi-supervised learning is a branch of machine learning that deals with training sets that are only partially labeled. These types of datasets are common in the world. For example, consider that one may have a few hundred images that are properly labeled as being various food items. They may wish to augment this dataset with the hundreds of

thousands of unlabeled pictures of food floating around the internet, but not wish to incur the cost of having to hand label them. Unfortunately, many machine learning methods are not able to handle both labeled and unlabeled data together and so frequently either the unlabeled data is tossed out in favor of supervised learning, or the labeled data is only used to identify the meaning of clusters learned by unsupervised techniques on the unlabeled data.

Probabilistic modeling offers an intuitive way of incorporating both labeled and unlabeled data into the training process through the expectation-maximization algorithm. Essentially, one will initialize the model on the labeled data, calculate the sufficient statistics of the unlabeled data and labeled data separately, and then add them together. This process can be thought of as vanilla EM on the unlabeled data except that at each iteration the sufficient statistics from the labeled data (MLE estimates) are added.

pomegranate follows the same convention as scikit-learn when it comes to partially labeled datasets. The label vector y is still of an equal length to the data matrix X , with labeled samples given the appropriate integer label, but unlabeled samples are given the label -1 . While $np.nan$ may be a more intuitive choice for missing labels, it isn't used because $np.nan$ is a double and the y vector is integers. When doing semi-supervised learning with hidden Markov models, however, one would pass in a list of labels for each labeled sequence, or *None* for each unlabeled sequence, instead of -1 to indicate an unlabeled sequence.

All models that support labeled data support semi-supervised learning, including naive Bayes classifiers, general Bayes classifiers, and hidden Markov models. Semi-supervised learning can be done with all extensions of these models natively, including on mixture model Bayes classifiers, mixed-distribution naive Bayes classifiers, using multi-threaded parallelism, and utilizing a GPU. Below is a simple example. Notice that there is no difference in the `from_samples` call, the presence of -1 in the label vector is enough.

```
import numpy

from sklearn.datasets import make_blobs
from sklearn.model_selection import train_test_split
from pomegranate import NaiveBayes, NormalDistribution

n, d, m = 50000, 5, 10
X, y = make_blobs(n, d, m, cluster_std=10)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.1)

n_unlabeled = int(X_train.shape[0] * 0.999)
idxs = numpy.random.choice(X_train.shape[0], size=n_unlabeled)
y_train[idxs] = -1

model = NaiveBayes.from_samples(NormalDistribution, X_train, y_train, verbose=True)
```

While HMMs can theoretically be trained on sequences of data that are only partially labeled, currently semi-supervised learning for HMMs means that some sequences are fully labeled, and some sequences have no labels at all. This means that instead of passing in a normal label vector as a list of lists such as `[[model.start, s1, s2, model.end], [model.start, s1, s1, model.end]]`, one would pass in a list of mixed list/None types, with lists defining the labels for labeled sequences, and None specifying that a sequence is unlabeled. For example, if the second sequence was unlabeled, one would pass in `[[model.start, s1, s2, model.end], None]` instead.

2.8.1 FAQ

Q. What ratio of unlabeled / labeled data is typically best?

A. It's hard to say. However, semi-supervised learning works best when the underlying distributions are **more complicated than the labeled data captures**. If your data is simple Gaussian blobs, not many samples are needed and adding in unlabeled samples likely will not help. However, if the true underlying distributions are some complex mixture of components but your labeled data looks like a simple blob, semi-supervised learning can help significantly.

Q. If this uses EM, what's the difference between semi-supervised learning and a mixture model?

A. Semi-supervised learning is a middle ground between unsupervised learning and supervised learning. As such, it adds together the sufficient statistics from unsupervised learning (using the EM algorithm) and supervised learning (using MLE) to get the complete model. An immediate benefit of this is that since there is a supervised initialization, the learned components will always align with the intended classes instead of being randomly assigning class values.

Q. Can parallelism be used with semi-supervised learning?

A. Yes. All aspects of pomegranate that can be used with naive Bayes classifiers or general Bayes classifiers can be used in the context of semi-supervised learning in the same way one would do so in supervised learning. One need only set the `n_jobs` parameters as normal. Literally the only difference for the user that the label vector now contains many `-1` values.

2.9 Parallelism

pomegranate supports multi-threaded parallelism through the `joblib` library. Typically, python applications use multi-processing in order to get around the Global Interpreter Lock (GIL) that prevents multiple threads from running in the same Python process. However, since pomegranate does most of its computation using only C level primitives, it can release the GIL and enable multiple threads to work at the same time. The main difference that a user will notice is that it is more memory efficient, because instead of copying the data across multiple processes that each have their own memory allocated, each thread in pomegranate can operate on the same single memory allocation.

Using parallelism in pomegranate is as simple as specifying the `n_jobs` parameter in any of the methods— both fitting and prediction methods!

For example:

```
import pomegranate, numpy

X = numpy.random.randn(1000, 1)

# No parallelism
model = GeneralMixtureModel.from_samples(NormalDistribution, 3, X)

# Some parallelism
model = GeneralMixtureModel.from_samples(NormalDistribution, 3, X, n_jobs=2)

# Maximum parallelism
model = GeneralMixtureModel.from_samples(NormalDistribution, 3, X, n_jobs=-1)
```

If you instead have a fit model and you're just looking to speed up prediction time, you need only pass the `n_jobs` parameter in to those methods as well.

```
model = <fit model>
X = numpy.random.randn(1000, 1)

# No parallelism
y = model.predict_proba(X)

# Some parallelism
y = model.predict_proba(X, n_jobs=2)

# Maximum parallelism
y = model.predict_proba(X, n_jobs=-1)
```

2.9.1 FAQ

Q. What models support parallelism?

A. All models should support parallel fitting. All models (except for HMMs) support parallel predictions natively through the `n_jobs` parameter. Basic distributions do not support parallelism as they typically take a negligible amount of time to do anything with.

Q. How can I parallelize something that doesn't have built-in parallelism?

A. You can easily write a parallelized prediction wrapper for any model using multiprocessing. It would likely look like the following:

```
from joblib import Parallel, delayed
from pomegranate import BayesianNetwork

def parallel_predict(name, X):
    """Load up a pomegranate model and predict a subset of X"""

    model = BayesianNetwork.from_json(name)
    return model.predict(X)

X_train, X_test = numpy.load("train.data"), numpy.load("test.data")

model = BayesianNetwork.from_samples(X_train)
with open("model.json", "w") as outfile:
    outfile.write(model.to_json())

n = len(X_test)
starts, ends = [i*n/4 for i in range(4)], [(i+1)*n/4 for i in range(4)]

y_pred = Parallel(n_jobs=4)( delayed(parallel_predict)(
    X_test[start:end]) for start, end in zip(starts, ends))
```

Q. What is the difference between multiprocessing and multithreading?

A. Multiprocessing involves creating a whole new Python process and passing the relevant data over to it. Multithreading involves creating multiple threads within the same Python process that all have access to the same memory. Multithreading is frequently more efficient because it doesn't involve copying potentially large amounts of data between different Python processes.

Q. Why don't all modules use multithreading?

A. Python has the Global Interpreter Lock (GIL) enabled which prevents more than one thread to execute per processes. The work-around is multiprocessing, which simply creates multiple processes that each have one thread working. When one uses Cython, they can disable the GIL when using only C-level primitives. Since most of the compute-intensive tasks involve only C-level primitives, multithreading is a natural choice for pomegranate. In situations where the size of the data is small and the cost of transferring it from one process to another is negligible, then multithreading can simply make things more complicated.

2.10 GPU Usage

pomegranate has GPU accelerated matrix multiplications to speed up all operations involving multivariate Gaussian distributions and all models that use them. This has led to an approximately 4x speedup for multivariate Gaussian mixture models and HMMs compared to using BLAS only. This speedup seems to scale better with dimensionality, with higher dimensional models seeing a larger speedup than smaller dimensional ones.

By default, pomegranate will activate GPU acceleration if it can import cupy, otherwise it will default to BLAS. You can check whether pomegranate is using GPU acceleration with this built-in function:

```
>>> import pomegranate
>>> print(pomegranate.utils.is_gpu_enabled())
```

If you'd like to deactivate GPU acceleration you can use the following command:

```
>>> pomegranate.utils.disable_gpu()
```

Likewise, if you'd like to activate GPU acceleration you can use the following command:

```
>>> pomegranate.utils.enable_gpu()
```

2.10.1 FAQ

Q. Why cupy and not Theano?

A. pomegranate only needs to do matrix multiplications using a GPU. While Theano supports an impressive range of more complex operations, it did not have a simple interface to support a matrix-matrix multiplication in the same manner that cupy does.

Q. Why am I not seeing a large speedup with my GPU?

A. There is a cost to transferring data to and from a GPU. It is possible that the GPU isn't fast enough, or that there isn't enough data to utilize the massively parallel aspect of a GPU for your dataset.

Q. Does pomegranate work using my type of GPU?

A. The supported GPUs will be better documented on the cupy package.

Q. Is multi-GPU supported?

A. Currently, no. In theory it should be possible, though.

2.11 Missing Values

- [IPython Notebook Tutorial](#)

As of version 0.9.0, pomegranate supports missing values for almost all methods. This means that models can be fit to data sets that have missing values in them, inference can be done on samples that have missing values, and even structure learning can be done in the presence of missing values. Currently, this support exists in the form of calculating sufficient statistics with respect to only the variables that are present in a sample and ignoring the missing values, in contrast to imputing the missing values and using those for the estimation.

Missing value support was added in a manner that requires the least user thought. All one has to do is add `numpy.nan` to mark an entry as missing for numeric data sets, or the string `'nan'` for string data sets. pomegranate will automatically handle missing values appropriately. The functions have been written in such a way to minimize the overhead of missing value support, by only acting differently when a missing value is found. However, it may take some models longer to do calculations in the presence of missing values than on dense data. For example, when calculating the log probability of a sample under a multivariate Gaussian distribution one can typically use BLAS or a GPU since a dot product is taken between the data and the inverse covariance matrix. Unfortunately, since missing data can occur in any of the columns, a new inverse covariance matrix has to be calculated for each sample and BLAS cannot be utilized at all.

As an example, when fitting a `NormalDistribution` to a vector of data, the parameters are estimated simply by ignoring the missing values. A data set with 100 observations and 50 missing values would produce the same model

as a data set comprised simply of the 100 observations. This comes into play when fitting multivariate models, like an `IndependentComponentsDistribution`, because each distribution is fit to only the observations for their specific feature. This means that samples where some values are missing can still be utilized in the dimensions where they are observed. This can lead to more robust estimates that by imputing the missing values using the mean or median of the column.

Here is an example of fitting a univariate distribution to data sets with missing values:

```
>>> import numpy
>>> from pomegranate import *
>>>
>>> X = numpy.random.randn(100)
>>> X[75:] = numpy.nan
>>>
>>> NormalDistribution.from_samples(X)
{
  "frozen" :false,
  "class" : "Distribution",
  "parameters" :[
    -0.0007138484812874587,
    1.0288813172046551
  ],
  "name" : "NormalDistribution"
}
>>> NormalDistribution.from_samples(X[:75])
{
  "frozen" :false,
  "class" : "Distribution",
  "parameters" :[
    -0.0007138484812874587,
    1.0288813172046551
  ],
  "name" : "NormalDistribution"
}
```

Multivariate Gaussian distributions take a slightly more complex approach. The means of each column are computed using the available data, but the covariance is calculated using sufficient statistics calculated from pairs of variables that exist in a sample. For example, if the sample was (2.0, 1.7, `numpy.nan`), then sufficient statistics would be calculated for the variance of the first and second variables as well as the covariance between the two, but nothing would be updated about the third variable.

All univariate distributions return a probability of 1 for missing data. This is done to support inference algorithms in more complex models. For example, when running the forward algorithm in a hidden Markov model in the presence of missing data, one would simply ignore the emission probability for the steps where the symbol is missing. This means that when getting to the step when a missing symbol is being aligned to each of the states, the cost is simply the transition probability to that state, instead of the transition probability multiplied by the likelihood of that symbol under that states' distribution (or, equivalently, having a likelihood of 1.) Under a Bayesian network, the probability of a sample is just the product of probabilities under distributions where the sample is fully observed.

See the tutorial for more examples of missing value support in pomegranate!

2.11.1 FAQ

Q. How do I indicate that a value is missing in a data set?

A. If it is a numeric data set, indicate that a value is missing using `numpy.nan`. If it is strings (such as 'A', 'B', etc...) use the string 'nan'. If your strings are stored in a numpy array, make sure that the full string 'nan' is

present. numpy arrays have a tendency to truncate longer strings if they're defined over shorter strings (like an array containing 'A' and 'B' might truncate 'nan' to be 'n').

Q. Are all algorithms supported?

A. Almost all! The only known non-supported function is Chow-Liu tree building. You can fit a Gaussian Mixture Model, run k-means clustering, decode a sequence using the Viterbi algorithm for a hidden Markov model, and learn the structure of a Bayesian network on data sets with missing values now!

Q. It is much slower to fit models using multivariate Gaussian distributions to missing data. Why?

A. When calculating the log probability of a point with missing values, a new inverse covariance matrix needs to be calculated over the subset of variables that are observed. This is a double whammy for speed because you need to (1) invert a matrix once per sample, and (2) cannot use BLAS for the calculation since there is no fixed sized covariance matrix to operate with.

Q. Performance on data sets without missing values appears to be worse now. What should I do?

A. Please report it on the GitHub issue tracker or email me. I have tried to minimize overhead in as many places as I can, but I have not run speed tests on all cases. Please include a sample script, and the amount of time it took.

2.12 Callbacks

- [IPython Notebook Tutorial](#)

Callback refer to functions that should be executing during the training procedure. These functions can be executed either at the start of training, the end of each epoch, or at the end of training. They mirror in style the callbacks from keras, and so are passed in using the *callbacks* keyword in *fit* and *from_sample* methods.

In pomegranate, a callback is an object that inherits from the *pomegranate.callbacks.Callback* object and has the following three methods implemented or inherited:

- *on_training_begin(self)* : What should happen when training begins.
- *on_epoch_end(self, logs)* : What should happen at the end of an epoch. The model will pass a dictionary of logs to each callback with each call that includes summary information about the training. The logs file is described more in depth below.
- *on_training_end(self, logs)* : What should happen when training ends. The final set of logs is passed in as well.

The log dictionary that is returned has the following entries:

- *epoch* : *int*, the iteration or epoch that the model is currently on
- *improvement* : *float*, the improvement since the latest iteration in the training set log probability
- *total_improvement* : *float*, the total improvement seen in the training set log probability since the beginning of training
- *log_probability* : *float*, the log probability of the training set after this round of training
- *last_log_probability* : *float*, the log probability of the training set before this round of training
- *duration* : *float*, the time in seconds that this epoch took
- *epoch_start_time* : the time according to *time.time()* that this epoch began
- *epoch_end_time* : the time according to *time.time()* that this epoch ended
- *n_seen_batches* : *int*, the number of batches that have been seen by the model, only useful for mini-batching
- *learning_rate* : The learning rate. This is undefined except when a decaying learning rate is set.

The following callbacks are built in to pomegranate:

1. `History()`: This will keep track of the above values in respective lists, e.g., `history.epochs` and `history.improvements`. This callback is automatically run by all models, and is returned when `return_history=True` is passed in.

```
from pomegranate.callbacks import History
from pomegranate import *

model = HiddenMarkovModel.from_samples(X) # No history returned
model, history = HiddenMarkovModel.from_samples(X, return_history=True)
```

2. `ModelCheckpoint(name=None, verbose=True)`: This callback will save the model parameters to a file named `{name}.{epoch}.json` at the end of each epoch. By default the name is the name of the model, but that can be overridden with the name passed in to the callback object. The verbosity flag indicates if it should print a message to the screen indicating that a file was saved, and where to, at the end of each epoch.

```
>>> from pomegranate.callbacks import ModelCheckpoint
>>> from pomegranate import *
>>> HiddenMarkovModel.from_samples(X, callbacks=[ModelCheckpoint()])
```

3. `CSVLogger(filename, separator=',', append=False)`: This callback will save the statistics from the logs dictionary to rows in a file at the end of each epoch. The filename specifies where to save the logs to, the separator is the symbol to separate values, and `append` indicates whether to save to the end of a file or to overwrite it, if it currently exists.

```
>>> from pomegranate.callbacks import CSVLogger, ModelCheckpoint
>>> from pomegranate import *
>>> HiddenMarkovModel.from_samples(X, callbacks=[CSVLogger('model.logs'),
↳ModelCheckpoint()])
```

4. `LambdaCallback(on_training_begin=None, on_training_end=None, on_epoch_end=None)`: A convenient wrapper that allows you to pass functions in that get executed at the appropriate points. The function `on_epoch_end` and `on_training_end` should accept a single argument, the dictionary of logs, as described above.

```
>>> from pomegranate.callbacks import LambdaCheckpoint
>>> from pomegranate import *
>>>
>>> def on_training_end(logs):
>>>     print("Total Improvement: {:.4f}".format(logs['total_improvement']))
>>>
>>> HiddenMarkovModel.from_samples(X, callbacks=[LambdaCheckpoint(on_training_end=on_
↳training_end)])
```

2.13 Probability Distributions

IPython Notebook Tutorial

While probability distributions are frequently used as components of more complex models such as mixtures and hidden Markov models, they can also be used by themselves. Many data science tasks require fitting a distribution to data or generating samples under a distribution. pomegranate has a large library of both univariate and multivariate distributions which can be used with an intuitive interface.

Univariate Distributions

<i>UniformDistribution</i>	A uniform distribution between two values.
<i>BernoulliDistribution</i>	A Bernoulli distribution describing the probability of a binary variable.
<i>NormalDistribution</i>	A normal distribution based on a mean and standard deviation.
<i>LogNormalDistribution</i>	A lognormal distribution over non-negative floats.
<i>ExponentialDistribution</i>	Represents an exponential distribution on non-negative floats.
<i>PoissonDistribution</i>	The probability of a number of events occurring in a fixed time window.
<i>BetaDistribution</i>	A beta-bernoulli distribution.
<i>GammaDistribution</i>	This distribution represents a gamma distribution, parameterized in the alpha/beta (shape/rate) parameterization.
<i>DiscreteDistribution</i>	A discrete distribution, made up of characters and their probabilities, assuming that these probabilities will sum to 1.0.

Kernel Densities

<i>GaussianKernelDensity</i>	A quick way of storing points to represent a Gaussian kernel density in one dimension.
<i>UniformKernelDensity</i>	A quick way of storing points to represent an Exponential kernel density in one dimension.
<i>TriangleKernelDensity</i>	A quick way of storing points to represent an Exponential kernel density in one dimension.

Multivariate Distributions

<i>IndependentComponentsDistribution</i>	Allows you to create a multivariate distribution, where each distribution is independent of the others.
<i>MultivariateGaussianDistribution</i>	
<i>DirichletDistribution</i>	A Dirichlet distribution, usually a prior for the multinomial distributions.
<i>ConditionalProbabilityTable</i>	A conditional probability table, which is dependent on values from at least one previous distribution but up to as many as you want to encode for.
<i>JointProbabilityTable</i>	A joint probability table.

While there are a large variety of univariate distributions, multivariate distributions can be made from univariate distributions by using `IndependentComponentsDistribution` with the assumption that each column of data is independent from the other columns (instead of being related by a covariance matrix, like in multivariate gaussians). Here is an example:

```
d1 = NormalDistribution(5, 2)
d2 = LogNormalDistribution(1, 0.3)
d3 = ExponentialDistribution(4)
d = IndependentComponentsDistribution([d1, d2, d3])
```

Use `MultivariateGaussianDistribution` when you want the full correlation matrix within the feature vector. When you want a strict diagonal correlation (i.e no correlation or “independent”), this is achieved using `IndependentComponentsDistribution` with `NormalDistribution` for each feature. There is no implementation of spherical or other variations of

correlation.

2.13.1 Initialization

Initializing a distribution is simple and done just by passing in the distribution parameters. For example, the parameters of a normal distribution are the mean (μ) and the standard deviation (σ). We can initialize it as follows:

```
from pomegranate import *
a = NormalDistribution(5, 2)
```

However, frequently we don't know the parameters of the distribution beforehand or would like to directly fit this distribution to some data. We can do this through the `from_samples` class method.

```
b = NormalDistribution.from_samples([3, 4, 5, 6, 7])
```

If we want to fit the model to weighted samples, we can just pass in an array of the relative weights of each sample as well.

```
b = NormalDistribution.from_samples([3, 4, 5, 6, 7], weights=[0.5, 1, 1.5, 1, 0.5])
```

2.13.2 Probability

Distributions are typically used to calculate the probability of some sample. This can be done using either the `probability` or `log_probability` methods.

```
>>> a = NormalDistribution(5, 2)
>>> a.log_probability(8)
-2.737085713764219
>>> a.probability(8)
0.064758797832971712
>>> b = NormalDistribution.from_samples([3, 4, 5, 6, 7], weights=[0.5, 1, 1.5, 1, 0.5])
>>> b.log_probability(8)
-4.437779569430167
```

These methods work for univariate distributions, kernel densities, and multivariate distributions all the same. For a multivariate distribution you'll have to pass in an array for the full sample.

```
>>> d1 = NormalDistribution(5, 2)
>>> d2 = LogNormalDistribution(1, 0.3)
>>> d3 = ExponentialDistribution(4)
>>> d = IndependentComponentsDistribution([d1, d2, d3])
>>>
>>> X = [6.2, 0.4, 0.9]
>>> d.log_probability(X)
-23.205411733352875
```

2.13.3 Fitting

We may wish to fit the distribution to new data, either overriding the previous parameters completely or moving the parameters to match the dataset more closely through inertia. Distributions are updated using maximum likelihood estimates (MLE). Kernel densities will either discard previous points or downweight them if inertia is used.

```
d = NormalDistribution(5, 2)
d.fit([1, 5, 7, 3, 2, 4, 3, 5, 7, 8, 2, 4, 6, 7, 2, 4, 5, 1, 3, 2, 1])
d
{
  "frozen" :false,
  "class" : "Distribution",
  "parameters" :[
    3.9047619047619047,
    2.13596776114341
  ],
  "name" : "NormalDistribution"
}
```

Training can be done on weighted samples by passing an array of weights in along with the data for any of the training functions, like the following:

```
d = NormalDistribution(5, 2)
d.fit([1, 5, 7, 3, 2, 4], weights=[0.5, 0.75, 1, 1.25, 1.8, 0.33])
d
{
  "frozen" :false,
  "class" : "Distribution",
  "parameters" :[
    3.538188277087034,
    1.954149818564894
  ],
  "name" : "NormalDistribution"
}
```

Training can also be done with inertia, where the new value will be some percentage the old value and some percentage the new value, used like `d.from_samples([5,7,8], inertia=0.5)` to indicate a 50-50 split between old and new values.

2.13.4 API Reference

For detailed documentation and examples, see the README.

class pomegranate.distributions.**BernoulliDistribution**

A Bernoulli distribution describing the probability of a binary variable.

from_summaries()

Update the parameters of the distribution from the summaries.

sample()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

class pomegranate.distributions.**BetaDistribution**

A beta-bernoulli distribution.

This object is a beta-bernoulli distribution. This means that it uses a beta distribution to model the distribution of values that the rate value can take rather than it being a single number.

This should not be confused with a Beta distribution by itself.

clear_summaries ()

Clear the summary statistics stored in the object.

from_summaries ()

Use the summaries in order to update the distribution.

sample ()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

class pomegranate.distributions.**ConditionalProbabilityTable**

A conditional probability table, which is dependent on values from at least one previous distribution but up to as many as you want to encode for.

bake ()

Order the inputs according to some external global ordering.

clear_summaries ()

Clear the summary statistics stored in the object.

fit ()

Update the parameters of the table based on the data.

from_samples ()

Learn the table from data.

from_summaries ()

Update the parameters of the distribution using sufficient statistics.

joint ()

This will turn a conditional probability table into a joint probability table. If the data is already a joint, it will likely mess up the data. It does so by scaling the parameters the probabilities by the parent distributions.

keys ()

Return the keys of the probability distribution which has parents, the child variable.

log_probability ()

Return the log probability of a value, which is a tuple in proper ordering, like the training data.

marginal ()

Calculate the marginal of the CPT. This involves normalizing to turn it into a joint probability table, and then summing over the desired value.

sample ()

Return a random sample from the conditional probability table.

summarize ()

Summarize the data into sufficient statistics to store.

to_json()

Serialize the model to a JSON.

Parameters

separators [tuple, optional] The two separators to pass to the `json.dumps` function for formatting. Default is `(',', ':')`.

indent [int, optional] The indentation to use at each level. Passed to `json.dumps` for formatting. Default is 4.

Returns

json [str] A properly formatted JSON object.

class `pomegranate.distributions.DirichletDistribution`

A Dirichlet distribution, usually a prior for the multinomial distributions.

clear_summaries()

Clear the summary statistics stored in the object. Parameters ——— None Returns ——— None

fit()

Set the parameters of this Distribution to maximize the likelihood of the given sample. Items holds some sort of sequence. If weights is specified, it holds a sequence of value to weight each item by.

from_samples()

Fit a distribution to some data without pre-specifying it.

from_summaries()

Update the internal parameters of the distribution.

sample()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

class `pomegranate.distributions.DiscreteDistribution`

A discrete distribution, made up of characters and their probabilities, assuming that these probabilities will sum to 1.0.

bake()

Encoding the distribution into integers.

clamp()

Return a distribution clamped to a particular value.

clear_summaries()

Clear the summary statistics stored in the object.

equals()

Return if the keys and values are equal

fit()

Set the parameters of this Distribution to maximize the likelihood of the given sample. Items holds some sort of sequence. If weights is specified, it holds a sequence of value to weight each item by.

from_samples ()
Fit a distribution to some data without pre-specifying it.

from_summaries ()
Use the summaries in order to update the distribution.

items ()
Return items of the underlying dictionary.

keys ()
Return the keys of the underlying dictionary.

log_probability ()
Return the log prob of the X under this distribution.

mle ()
Return the maximally likely key.

probability ()
Return the prob of the X under this distribution.

sample ()
Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

summarize ()
Reduce a set of observations to sufficient statistics.

to_json ()
Serialize the distribution to a JSON.

Parameters

separators [tuple, optional] The two separators to pass to the json.dumps function for formatting. Default is (';', ' : ').

indent [int, optional] The indentation to use at each level. Passed to json.dumps for formatting. Default is 4.

Returns

json [str] A properly formatted JSON object.

values ()
Return values of the underlying dictionary.

class pomegranate.distributions.**ExponentialDistribution**

Represents an exponential distribution on non-negative floats.

clear_summaries ()
Clear the summary statistics stored in the object.

from_summaries ()
Takes in a series of summaries, represented as a mean, a variance, and a weight, and updates the underlying distribution. Notes on how to do this for a Gaussian distribution were taken from here: <http://math.stackexchange.com/questions/453113/how-to-merge-two-gaussians>

sample ()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

class pomegranate.distributions.**GammaDistribution**

This distribution represents a gamma distribution, parameterized in the alpha/beta (shape/rate) parameterization. ML estimation for a gamma distribution, taking into account weights on the data, is nontrivial, and I was unable to find a good theoretical source for how to do it, so I have cobbled together a solution here from less-reputable sources.

clear_summaries ()

Clear the summary statistics stored in the object.

fit ()

Set the parameters of this Distribution to maximize the likelihood of the given sample. Items holds some sort of sequence. If weights is specified, it holds a sequence of value to weight each item by. In the Gamma case, likelihood maximization is necessarily numerical, and the extension to weighted values is not trivially obvious. The algorithm used here includes a Newton-Raphson step for shape parameter estimation, and analytical calculation of the rate parameter. The extension to weights is constructed using vital information found way down at the bottom of an Experts Exchange page. Newton-Raphson continues until the change in the parameter is less than epsilon, or until iteration_limit is reached See: http://en.wikipedia.org/wiki/Gamma_distribution http://www.experts-exchange.com/Other/Math_Science/Q_23943764.html

from_summaries ()

Set the parameters of this Distribution to maximize the likelihood of the given sample given the summaries which have been stored. In the Gamma case, likelihood maximization is necessarily numerical, and the extension to weighted values is not trivially obvious. The algorithm used here includes a Newton-Raphson step for shape parameter estimation, and analytical calculation of the rate parameter. The extension to weights is constructed using vital information found way down at the bottom of an Experts Exchange page. Newton-Raphson continues until the change in the parameter is less than epsilon, or until iteration_limit is reached See: http://en.wikipedia.org/wiki/Gamma_distribution http://www.experts-exchange.com/Other/Math_Science/Q_23943764.html

sample ()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

summarize ()

Take in a series of items and their weights and reduce it down to a summary statistic to be used in training later.

class pomegranate.distributions.**IndependentComponentsDistribution**

Allows you to create a multivariate distribution, where each distribution is independent of the others. Distribu-

tions can be any type, such as having an exponential represent the duration of an event, and a normal represent the mean of that event. Observations must now be tuples of a length equal to the number of distributions passed in.

```
s1 = IndependentComponentsDistribution([ExponentialDistribution(0.1), NormalDistribution(5, 2)])
```

```
s1.log_probability((5, 2))
```

```
clear_summaries ()
```

Clear the summary statistics stored in the object.

```
fit ()
```

Set the parameters of this Distribution to maximize the likelihood of the given sample. Items holds some sort of sequence. If weights is specified, it holds a sequence of value to weight each item by.

```
from_samples ()
```

Create a new independent components distribution from data.

```
from_summaries ()
```

Use the collected summary statistics in order to update the distributions.

```
log_probability ()
```

What's the probability of a given tuple under this mixture? It's the product of the probabilities of each X in the tuple under their respective distribution, which is the sum of the log probabilities.

```
sample ()
```

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

```
summarize ()
```

Take in an array of items and reduce it down to summary statistics. For a multivariate distribution, this involves just passing the appropriate data down to the appropriate distributions.

```
to_json ()
```

Convert the distribution to JSON format.

```
class pomegranate.distributions.JointProbabilityTable
```

A joint probability table. The primary difference between this and the conditional table is that the final column sums to one here. The joint table can be thought of as the conditional probability table normalized by the marginals of each parent.

```
bake ()
```

Order the inputs according to some external global ordering.

```
clear_summaries ()
```

Clear the summary statistics stored in the object.

```
fit ()
```

Update the parameters of the table based on the data.

```
from_samples ()
```

Learn the table from data.

```
from_summaries ()
```

Update the parameters of the table.

log_probability()

Return the log probability of a value, which is a tuple in proper ordering, like the training data.

marginal()

Determine the marginal of this table with respect to the index of one variable. The parents are index 0..n-1 for n parents, and the final variable is either the appropriate value or -1. For example: table = A B C p(C) ... data ... table.marginal(0) gives the marginal wrt A table.marginal(1) gives the marginal wrt B table.marginal(2) gives the marginal wrt C table.marginal(-1) gives the marginal wrt C

sample()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

summarize()

Summarize the data into sufficient statistics to store.

to_json()

Serialize the model to a JSON.

Parameters

separators [tuple, optional] The two separators to pass to the json.dumps function for formatting. Default is (';', ': ').

indent [int, optional] The indentation to use at each level. Passed to json.dumps for formatting. Default is 4.

Returns

json [str] A properly formatted JSON object.

class pomegranate.distributions.**LogNormalDistribution**

A lognormal distribution over non-negative floats.

The parameters are the mu and sigma of the normal distribution, which is the the exponential of the log normal distribution.

clear_summaries()

Clear the summary statistics stored in the object.

from_summaries()

Takes in a series of summaries, represented as a mean, a variance, and a weight, and updates the underlying distribution. Notes on how to do this for a Gaussian distribution were taken from here: <http://math.stackexchange.com/questions/453113/how-to-merge-two-gaussians>

sample()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

class pomegranate.distributions.**MultivariateGaussianDistribution**

clear_summaries ()

Clear the summary statistics stored in the object.

from_samples ()

Fit a distribution to some data without pre-specifying it.

from_summaries ()

Set the parameters of this Distribution to maximize the likelihood of the given sample. Items holds some sort of sequence. If weights is specified, it holds a sequence of value to weight each item by.

sample ()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

class pomegranate.distributions.**NormalDistribution**

A normal distribution based on a mean and standard deviation.

clear_summaries ()

Clear the summary statistics stored in the object.

from_summaries ()

Takes in a series of summaries, represented as a mean, a variance, and a weight, and updates the underlying distribution. Notes on how to do this for a Gaussian distribution were taken from here: <http://math.stackexchange.com/questions/453113/how-to-merge-two-gaussians>

sample ()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

class pomegranate.distributions.**PoissonDistribution**

The probability of a number of events occurring in a fixed time window.

A probability distribution which expresses the probability of a number of events occurring in a fixed time window. It assumes these events occur with at a known rate, and independently of each other. It can operate over both integer and float values.

clear_summaries ()

Clear the summary statistics stored in the object.

from_summaries ()

Takes in a series of summaries, consisting of the minimum and maximum of a sample, and determine the global minimum and maximum.

sample ()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

class pomegranate.distributions.**UniformDistribution**

A uniform distribution between two values.

clear_summaries ()

Clear the summary statistics stored in the object.

from_summaries ()

Takes in a series of summaries, consisting of the minimum and maximum of a sample, and determine the global minimum and maximum.

sample ()

Sample from this uniform distribution and return the value sampled.

2.14 General Mixture Models

[IPython Notebook Tutorial](#)

General Mixture models (GMMs) are an unsupervised probabilistic model composed of multiple distributions (commonly referred to as components) and corresponding weights. This allows you to model more complex distributions corresponding to a singular underlying phenomena. For a full tutorial on what a mixture model is and how to use them, see the above tutorial.

2.14.1 Initialization

General Mixture Models can be initialized in two ways depending on if you know the initial parameters of the model or not: (1) passing in a list of pre-initialized distributions, or (2) running the `from_samples` class method on data. The initial parameters can be either a pre-specified model that is ready to be used for prediction, or the initialization for expectation-maximization. Otherwise, if the second initialization option is chosen, then k-means is used to initialize the distributions. The distributions passed for each component don't have to be the same type, and if an `IndependentComponentDistribution` object is passed in, then the dimensions don't need to be modeled by the same distribution.

Here is an example of a traditional multivariate Gaussian mixture where we pass in pre-initialized distributions. We can also pass in the weight of each component, which serves as the prior probability of a sample belonging to that component when doing predictions.

```
>>> from pomegranate import *
>>> d1 = MultivariateGaussianDistribution([1, 6, 3], [[1, 0, 0], [0, 1, 0], [0, 0, 1]])
>>> d2 = MultivariateGaussianDistribution([2, 8, 4], [[1, 0, 0], [0, 1, 0], [0, 0, 1]])
```

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```
>>> d3 = MultivariateGaussianDistribution([0, 4, 8], [[2, 0, 0], [0, 3, 0], [0, 0, 1]])
>>> model = GeneralMixtureModel([d1, d2, d3], weights=[0.25, 0.60, 0.15])
```

Alternatively, if we want to model each dimension differently, then we can replace the multivariate Gaussian distributions with `IndependentComponentsDistribution` objects.

```
>>> from pomegranate import *
>>> d1 = IndependentComponentsDistribution([NormalDistribution(5, 2),
↳ ExponentialDistribution(1), LogNormalDistribution(0.4, 0.1)])
>>> d2 = IndependentComponentsDistribution([NormalDistribution(3, 1),
↳ ExponentialDistribution(2), LogNormalDistribution(0.8, 0.2)])
>>> model = GeneralMixtureModel([d1, d2], weights=[0.66, 0.34])
```

If we do not know the parameters of our distributions beforehand and want to learn them entirely from data, then we can use the `from_samples` class method. This method will run k-means to initialize the components, using the returned clusters to initialize all parameters of the distributions, i.e. both mean and covariances for multivariate Gaussian distributions. Afterwards, expectation-maximization is used to refine the parameters of the model, iterating until convergence.

```
>>> from pomegranate import *
>>> model = GeneralMixtureModel.from_samples(MultivariateGaussianDistribution, n_
↳ components=3, X=X)
```

If we want to model each dimension using a different distribution, then we can pass in a list of callables and they will be initialized using k-means as well.

```
>>> from pomegranate import *
>>> model = GeneralMixtureModel.from_samples([NormalDistribution,
↳ ExponentialDistribution, LogNormalDistribution], n_components=5, X=X)
```

2.14.2 Probability

The probability of a point is the sum of its probability under each of the components, multiplied by the weight of each component c , $P = \sum_{i \in M} P(D|M_i)P(M_i)$. The `probability` method returns the probability of each sample under the entire mixture, and the `log_probability` method returns the log of that value.

2.14.3 Prediction

The common prediction tasks involve predicting which component a new point falls under. This is done using Bayes rule $P(M|D) = \frac{P(D|M)P(M)}{P(D)}$ to determine the posterior probability $P(M|D)$ as opposed to simply the likelihood $P(D|M)$. Bayes rule indicates that it isn't simply the likelihood function which makes this prediction but the likelihood function multiplied by the probability that that distribution generated the sample. For example, if you have a distribution which has 100x as many samples fall under it, you would naively think that there is a ~99% chance that any random point would be drawn from it. Your belief would then be updated based on how well the point fit each distribution, but the proportion of points generated by each sample is important as well.

We can get the component label assignments using `model.predict(data)`, which will return an array of indexes corresponding to the maximally likely component. If what we want is the full matrix of $P(M|D)$, then we can use `model.predict_proba(data)`, which will return a matrix with each row being a sample, each column being a component, and each cell being the probability that that model generated that data. If we want log probabilities instead we can use `model.predict_log_proba(data)` instead.

2.14.4 Fitting

Training GMMs faces the classic chicken-and-egg problem that most unsupervised learning algorithms face. If we knew which component a sample belonged to, we could use MLE estimates to update the component. And if we knew the parameters of the components we could predict which sample belonged to which component. This problem is solved using expectation-maximization, which iterates between the two until convergence. In essence, an initialization point is chosen which usually is not a very good start, but through successive iteration steps, the parameters converge to a good ending.

These models are fit using `model.fit(data)`. A maximum number of iterations can be specified as well as a stopping threshold for the improvement ratio. See the API reference for full documentation.

2.14.5 API Reference

class `pomegranate.gmm.GeneralMixtureModel`

A General Mixture Model.

This mixture model can be a mixture of any distribution as long as they are all of the same dimensionality. Any object can serve as a distribution as long as it has `fit(X, weights)`, `log_probability(X)`, and `summarize(X, weights)/from_summaries()` methods if out of core training is desired.

Parameters

distributions [array-like, shape (n_components,)] The components of the model as initialized distributions.

weights [array-like, optional, shape (n_components,)] The prior probabilities corresponding to each component. Does not need to sum to one, but will be normalized to sum to one internally. Defaults to None.

Examples

```
>>> from pomegranate import *
>>>
>>> d1 = NormalDistribution(5, 2)
>>> d2 = NormalDistribution(1, 1)
>>>
>>> clf = GeneralMixtureModel([d1, d2])
>>> clf.log_probability(5)
-2.304562194038089
>>> clf.predict_proba([[5], [7], [1]])
array([[ 0.99932952,  0.00067048],
       [ 0.99999995,  0.00000005],
       [ 0.06337894,  0.93662106]])
>>> clf.fit([[1], [5], [7], [8], [2]])
>>> clf.predict_proba([[5], [7], [1]])
array([[ 1.          ,  0.          ],
       [ 1.          ,  0.          ],
       [ 0.00004383,  0.99995617]])
>>> clf.distributions
array([ {
  "frozen" :false,
  "class"  :"Distribution",
  "parameters" :[
    6.6571359101390755,
    1.2639830514274502
```

(continues on next page)

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```

    ],
    "name" : "NormalDistribution"
  },
  {
    "frozen" : false,
    "class" : "Distribution",
    "parameters" : [
      1.498707696758334,
      0.4999983303277837
    ],
    "name" : "NormalDistribution"
  }
], dtype=object)

```

Attributes

distributions [array-like, shape (n_components,)] The component distribution objects.

weights [array-like, shape (n_components,)] The learned prior weight of each object

clear_summaries ()

Remove the stored sufficient statistics.

Parameters

None

Returns

None

copy ()

Return a deep copy of this distribution object.

This object will not be tied to any other distribution or connected in any form.

Parameters

None

Returns

distribution [Distribution] A copy of the distribution with the same parameters.

fit ()

Fit the model to new data using EM.

This method fits the components of the model to new data using the EM method. It will iterate until either max iterations has been reached, or the stop threshold has been passed.

Parameters

X [array-like or generator, shape (n_samples, n_dimensions)] This is the data to train on. Each row is a sample, and each column is a dimension to train on.

weights [array-like, shape (n_samples,), optional] The initial weights of each sample in the matrix. If nothing is passed in then each sample is assumed to be the same weight. Default is None.

inertia [double, optional] The weight of the previous parameters of the model. The new parameters will roughly be $\text{old_param} \times \text{inertia} + \text{new_param} \times (1 - \text{inertia})$, so an inertia of 0 means ignore the old parameters, whereas an inertia of 1 means ignore the new parameters. Default is 0.0.

pseudocount [double, optional, positive] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Only effects mixture models defined over discrete distributions. Default is 0.

stop_threshold [double, optional, positive] The threshold at which EM will terminate for the improvement of the model. If the model does not improve its fit of the data by a log probability of 0.1 then terminate. Default is 0.1.

max_iterations [int, optional, positive] The maximum number of iterations to run EM for. If this limit is hit then it will terminate training, regardless of how well the model is improving per iteration. Default is 1e8.

batch_size [int or None, optional] The number of samples in a batch to summarize on. This controls the size of the set sent to *summarize* and so does not make the update any less exact. This is useful when training on a memory map and cannot load all the data into memory. If set to None, *batch_size* is 1 / *n_jobs*. Default is None.

batches_per_epoch [int or None, optional] The number of batches in an epoch. This is the number of batches to summarize before calling *from_summaries* and updating the model parameters. This allows one to do minibatch updates by updating the model parameters before setting the full dataset. If set to None, uses the full dataset. Default is None.

lr_decay [double, optional, positive] The step size decay as a function of the number of iterations. Functionally, this sets the inertia to be $(2+k)^{-lr_decay}$ where *k* is the number of iterations. This causes initial iterations to have more of an impact than later iterations, and is frequently used in minibatch learning. This value is suggested to be between 0.5 and 1. Default is 0, meaning no decay.

callbacks [list, optional] A list of callback objects that describe functionality that should be undertaken over the course of training.

return_history [bool, optional] Whether to return the history during training as well as the model.

verbose [bool, optional] Whether or not to print out improvement information over iterations. Default is False.

n_jobs [int, optional] The number of threads to use when parallelizing the job. This parameter is passed directly into joblib. Default is 1, indicating no parallelism.

Returns

self [GeneralMixtureModel] The fit mixture model.

freeze()

Freeze the distribution, preventing updates from occurring.

from_json()

Deserialize this object from its JSON representation.

from_samples()

Create a mixture model directly from the given dataset.

First, k-means will be run using the given initializations, in order to define initial clusters for the points. These clusters are used to initialize the distributions used. Then, EM is run to refine the parameters of these distributions.

A homogeneous mixture can be defined by passing in a single distribution callable as the first parameter and specifying the number of components, while a heterogeneous mixture can be defined by passing in a list of callables of the appropriate type.

Parameters

- distributions** [array-like, shape (n_components,) or callable] The components of the model. If array, corresponds to the initial distributions of the components. If callable, must also pass in the number of components and kmeans++ will be used to initialize them.
- n_components** [int] If a callable is passed into distributions then this is the number of components to initialize using the kmeans++ algorithm.
- X** [array-like, shape (n_samples, n_dimensions)] This is the data to train on. Each row is a sample, and each column is a dimension to train on.
- weights** [array-like, shape (n_samples,), optional] The initial weights of each sample in the matrix. If nothing is passed in then each sample is assumed to be the same weight. Default is None.
- n_init** [int, optional] The number of initializations of k-means to do before choosing the best. Default is 1.
- init** [str, optional] The initialization algorithm to use for the initial k-means clustering. Must be one of 'first-k', 'random', 'kmeans++', or 'kmeansll'. Default is 'kmeans++'.
- max_kmeans_iterations** [int, optional] The maximum number of iterations to run kmeans for in the initialization step. Default is 1.
- inertia** [double, optional] The weight of the previous parameters of the model. The new parameters will roughly be $\text{old_param} * \text{inertia} + \text{new_param} * (1 - \text{inertia})$, so an inertia of 0 means ignore the old parameters, whereas an inertia of 1 means ignore the new parameters. Default is 0.0.
- pseudocount** [double, optional, positive] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Only effects mixture models defined over discrete distributions. Default is 0.
- stop_threshold** [double, optional, positive] The threshold at which EM will terminate for the improvement of the model. If the model does not improve its fit of the data by a log probability of 0.1 then terminate. Default is 0.1.
- max_iterations** [int, optional, positive] The maximum number of iterations to run EM for. If this limit is hit then it will terminate training, regardless of how well the model is improving per iteration. Default is 1e8.
- batch_size** [int or None, optional] The number of samples in a batch to summarize on. This controls the size of the set sent to *summarize* and so does not make the update any less exact. This is useful when training on a memory map and cannot load all the data into memory. If set to None, batch_size is 1 / n_jobs. Default is None.
- batches_per_epoch** [int or None, optional] The number of batches in an epoch. This is the number of batches to summarize before calling *from_summaries* and updating the model parameters. This allows one to do minibatch updates by updating the model parameters before setting the full dataset. If set to None, uses the full dataset. Default is None.
- lr_decay** [double, optional, positive] The step size decay as a function of the number of iterations. Functionally, this sets the inertia to be $(2+k)^{-\text{lr_decay}}$ where k is the number of iterations. This causes initial iterations to have more of an impact than later iterations, and is frequently used in minibatch learning. This value is suggested to be between 0.5 and 1. Default is 0, meaning no decay.
- callbacks** [list, optional] A list of callback objects that describe functionality that should be undertaken over the course of training.

return_history [bool, optional] Whether to return the history during training as well as the model.

verbose [bool, optional] Whether or not to print out improvement information over iterations. Default is False.

n_jobs [int, optional] The number of threads to use when parallelizing the job. This parameter is passed directly into joblib. Default is 1, indicating no parallelism.

from_summaries ()

Fit the model to the collected sufficient statistics.

Fit the parameters of the model to the sufficient statistics gathered during the summarize calls. This should return an exact update.

Parameters

inertia [double, optional] The weight of the previous parameters of the model. The new parameters will roughly be $\text{old_param} * \text{inertia} + \text{new_param} * (1 - \text{inertia})$, so an inertia of 0 means ignore the old parameters, whereas an inertia of 1 means ignore the new parameters. Default is 0.0.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. If discrete data, will smooth both the prior probabilities of each component and the emissions of each component. Otherwise, will only smooth the prior probabilities of each component. Default is 0.

Returns

None

from_yaml ()

Deserialize this object from its YAML representation.

log_probability ()

Calculate the log probability of a point under the distribution.

The probability of a point is the sum of the probabilities of each distribution multiplied by the weights. Thus, the log probability is the sum of the log probability plus the log prior.

This is the python interface.

Parameters

X [numpy.ndarray, shape=(n, d) or (n, m, d)] The samples to calculate the log probability of. Each row is a sample and each column is a dimension. If emissions are HMMs then shape is (n, m, d) where m is variable length for each observation, and X becomes an array of n (m, d)-shaped arrays.

n_jobs [int, optional] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

log_probability [double] The log probability of the point under the distribution.

predict ()

Predict the most likely component which generated each sample.

Calculate the posterior $P(\text{MID})$ for each sample and return the index of the component most likely to fit it. This corresponds to a simple `argmax` over the responsibility matrix.

This is a sklearn wrapper for the `maximum_a_posteriori` method.

Parameters

X [array-like, shape (n_samples, n_dimensions)] The samples to do the prediction on. Each sample is a row and each column corresponds to a dimension in that sample. For univariate distributions, a single array may be passed in.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

y [array-like, shape (n_samples,)] The predicted component which fits the sample the best.

`predict_log_proba()`

Calculate the posterior log $P(\text{MID})$ for data.

Calculate the log probability of each item having been generated from each component in the model. This returns normalized log probabilities such that the probabilities should sum to 1

This is a sklearn wrapper for the original posterior function.

Parameters

X [array-like, shape (n_samples, n_dimensions)] The samples to do the prediction on. Each sample is a row and each column corresponds to a dimension in that sample. For univariate distributions, a single array may be passed in.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

y [array-like, shape (n_samples, n_components)] The normalized log probability log $P(\text{MID})$ for each sample. This is the probability that the sample was generated from each component.

`predict_proba()`

Calculate the posterior $P(\text{MID})$ for data.

Calculate the probability of each item having been generated from each component in the model. This returns normalized probabilities such that each row should sum to 1.

Since calculating the log probability is much faster, this is just a wrapper which exponentiates the log probability matrix.

Parameters

X [array-like, shape (n_samples, n_dimensions)] The samples to do the prediction on. Each sample is a row and each column corresponds to a dimension in that sample. For univariate distributions, a single array may be passed in.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

probability [array-like, shape (n_samples, n_components)] The normalized probability P(M|D) for each sample. This is the probability that the sample was generated from each component.

probability()

Return the probability of the given symbol under this distribution.

Parameters

symbol [object] The symbol to calculate the probability of

Returns

probability [double] The probability of that point under the distribution.

sample()

Generate a sample from the model.

First, randomly select a component weighted by the prior probability, Then, use the sample method from that component to generate a sample.

Parameters

n [int, optional] The number of samples to generate. Defaults to 1.

random_state [int, numpy.random.RandomState, or None] The random state used for generating samples. If set to none, a random seed will be used. If set to either an integer or a random seed, will produce deterministic outputs.

Returns

sample [array-like or object] A randomly generated sample from the model of the type modelled by the emissions. An integer if using most distributions, or an array if using multivariate ones, or a string for most discrete distributions. If n=1 return an object, if n>1 return an array of the samples.

score()

Return the accuracy of the model on a data set.

Parameters

X [numpy.ndarray, shape=(n, d)] The values of the data set

y [numpy.ndarray, shape=(n,)] The labels of each value

summarize()

Summarize a batch of data and store sufficient statistics.

This will run the expectation step of EM and store sufficient statistics in the appropriate distribution objects. The summarization can be thought of as a chunk of the E step, and the from_summaries method as the M step.

Parameters

X [array-like, shape (n_samples, n_dimensions)] This is the data to train on. Each row is a sample, and each column is a dimension to train on.

weights [array-like, shape (n_samples,), optional] The initial weights of each sample in the matrix. If nothing is passed in then each sample is assumed to be the same weight. Default is None.

Returns

logp [double] The log probability of the data given the current model. This is used to speed up EM.

thaw ()

Thaw the distribution, re-allowing updates to occur.

to_json ()

Serialize the model to JSON.

Parameters

separators [tuple, optional] The two separators to pass to the `json.dumps` function for formatting. Default is `(',', ':')`.

indent [int, optional] The indentation to use at each level. Passed to `json.dumps` for formatting. Default is 4.

Returns

json [str] A properly formatted JSON object.

to_yaml ()

Serialize the model to YAML for compactness.

2.15 Hidden Markov Models

- [IPython Notebook Tutorial](#)
- [IPython Notebook Sequence Alignment Tutorial](#)

Hidden Markov models (HMMs) are a structured probabilistic model that forms a probability distribution of sequences, as opposed to individual symbols. It is similar to a Bayesian network in that it has a directed graphical structure where nodes represent probability distributions, but unlike Bayesian networks in that the edges represent transitions and encode transition probabilities, whereas in Bayesian networks edges encode dependence statements. A HMM can be thought of as a general mixture model plus a transition matrix, where each component in the general Mixture model corresponds to a node in the hidden Markov model, and the transition matrix informs the probability that adjacent symbols in the sequence transition from being generated from one component to another. A strength of HMMs is that they can model variable length sequences whereas other models typically require a fixed feature set. They are extensively used in the fields of natural language processing to model speech, bioinformatics to model biosequences, and robotics to model movement.

The HMM implementation in pomegranate is based off of the implementation in its predecessor, Yet Another Hidden Markov Model (YAHMM). To convert a script that used YAHMM to a script using pomegranate, you only need to change calls to the `Model` class to call `HiddenMarkovModel`. For example, a script that previously looked like the following:

```
from yahmm import *
model = Model()
```

would now be written as

```
from pomegranate import *
model = HiddenMarkovModel()
```

and the remaining method calls should be identical.

2.15.1 Initialization

Hidden Markov models can be initialized in one of two ways depending on if you know the initial parameters of the model, either (1) by defining both the distributions and the graphical structure manually, or (2) running the `from_samples` method to learn both the structure and distributions directly from data. The first initialization method can be used either to specify a pre-defined model that is ready to make predictions, or as the initialization to a training algorithm such as Baum-Welch. It is flexible enough to allow sparse transition matrices and any type of distribution on each node, i.e. normal distributions on several nodes, but a mixture of normals on some nodes modeling more complex phenomena. The second initialization method is less flexible, in that currently each node must have the same distribution type, and that it will only learn dense graphs. Similar to mixture models, this initialization method starts with k-means to initialize the distributions and a uniform probability transition matrix before running Baum-Welch.

If you are initializing the parameters manually, you can do so either by passing in a list of distributions and a transition matrix, or by building the model line-by-line. Let's first take a look at building the model from a list of distributions and a transition matrix.

```
from pomegranate import *
dists = [NormalDistribution(5, 1), NormalDistribution(1, 7), NormalDistribution(8,2)]
trans_mat = numpy.array([[0.7, 0.3, 0.0],
                        [0.0, 0.8, 0.2],
                        [0.0, 0.0, 0.9]])
starts = numpy.array([1.0, 0.0, 0.0])
ends = numpy.array([0.0, 0.0, 0.1])
model = HiddenMarkovModel.from_matrix(trans_mat, dists, starts, ends)
```

Next, let's take a look at building the same model line by line.

```
from pomegranate import *
s1 = State(NormalDistribution(5, 1))
s2 = State(NormalDistribution(1, 7))
s3 = State(NormalDistribution(8, 2))
model = HiddenMarkovModel()
model.add_states(s1, s2, s3)
model.add_transition(model.start, s1, 1.0)
model.add_transition(s1, s1, 0.7)
model.add_transition(s1, s2, 0.3)
model.add_transition(s2, s2, 0.8)
model.add_transition(s2, s3, 0.2)
model.add_transition(s3, s3, 0.9)
model.add_transition(s3, model.end, 0.1)
model.bake()
```

Initially it may seem that the first method is far easier due to it being fewer lines of code. However, when building large sparse models defining a full transition matrix can be cumbersome, especially when it is mostly 0s.

Models built in this manner must be explicitly “baked” at the end. This finalizes the model topology and creates the internal sparse matrix which makes up the model. This step also automatically normalizes all transitions to make sure they sum to 1.0, stores information about tied distributions, edges, pseudocounts, and merges unnecessary silent states in the model for computational efficiency. This can cause the *bake* step to take a little bit of time. If you want to reduce this overhead and are sure you specified the model correctly you can pass in `merge="None"` to the *bake* step to avoid model checking.

The second way to initialize models is to use the `from_samples` class method. The call is identical to initializing a mixture model.

```
>>> from pomegranate import *
>>> model = HiddenMarkovModel.from_samples(NormalDistribution, n_components=5, X=X)
```


Much like a mixture model, all arguments present in the `fit` step can also be passed in to this method. Also like a mixture model, it is initialized by running k-means on the concatenation of all data, ignoring that the symbols are part of a structured sequence. The clusters returned are used to initialize all parameters of the distributions, i.e. both mean and covariances for multivariate Gaussian distributions. The transition matrix is initialized as uniform random probabilities. After the components (distributions on the nodes) are initialized, the given training algorithm is used to refine the parameters of the distributions and learn the appropriate transition probabilities.

2.15.2 Log Probability

There are two common forms of the log probability which are used. The first is the log probability of the most likely path the sequence can take through the model, called the Viterbi probability. This can be calculated using `model.viterbi(sequence)`. However, this is $P(D|S_{ML}, S_{ML}, S_{ML})$ not $P(D|M)$. In order to get $P(D|M)$ we have to sum over all possible paths instead of just the single most likely path. This can be calculated using `model.log_probability(sequence)` and uses the forward algorithm internally. On that note, the full forward matrix can be returned using `model.forward(sequence)` and the full backward matrix can be returned using `model.backward(sequence)`, while the full forward-backward emission and transition matrices can be returned using `model.forward_backward(sequence)`.

2.15.3 Prediction

A common prediction technique is calculating the Viterbi path, which is the most likely sequence of states that generated the sequence given the full model. This is solved using a simple dynamic programming algorithm similar to sequence alignment in bioinformatics. This can be called using `model.viterbi(sequence)`. A sklearn wrapper can be called using `model.predict(sequence, algorithm='viterbi')`.

Another prediction technique is called maximum a posteriori or forward-backward, which uses the forward and backward algorithms to calculate the most likely state per observation in the sequence given the entire remaining alignment. Much like the forward algorithm can calculate the sum-of-all-paths probability instead of the most likely single path, the forward-backward algorithm calculates the best sum-of-all-paths state assignment instead of calculating the single best path. This can be called using `model.predict(sequence, algorithm='map')` and the raw normalized probability matrices can be called using `model.predict_proba(sequence)`.

2.15.4 Fitting

A simple fitting algorithm for hidden Markov models is called Viterbi training. In this method, each observation is tagged with the most likely state to generate it using the Viterbi algorithm. The distributions (emissions) of each states are then updated using MLE estimates on the observations which were generated from them, and the transition matrix is updated by looking at pairs of adjacent state taggings. This can be done using `model.fit(sequence, algorithm='viterbi')`.

However, this is not the best way to do training and much like the other sections there is a way of doing training using sum-of-all-paths probabilities instead of maximally likely path. This is called Baum-Welch or forward-backward training. Instead of using hard assignments based on the Viterbi path, observations are given weights equal to the probability of them having been generated by that state. Weighted MLE can then be done to update the distributions, and the soft transition matrix can give a more precise probability estimate. This is the default training algorithm, and can be called using either `model.fit(sequences)` or explicitly using `model.fit(sequences, algorithm='baum-welch')`.

pomegranate also supports labeled training of hidden Markov models. This setting is where one has state labels for each observation and wishes to derive the transition matrix and observations given those labels. The emissions simply become MLE estimates of the data partitioned by the labels and the transition matrix is calculated directly from the adjacency of labels. This option can be specified using `model.fit(sequences, labels=labels,`

state_names=state_names) where labels has the same shape as sequences and state_names has the set of all possible labels.

Note: The sequence of labels can include hidden states! However, a consequence of this is that each sequence of labels must begin with the start state because that is where each sequence begins with being aligned to the model. For instance, for the sequence of observations [1, 5, 6, 2] the corresponding labels would be ['None-start', 'a', 'b', 'b', 'a'] because the default name of a model is None and the name of the start state is {name}-start. Likewise, you will need to add the end state label at the end of each sequence if you want an explicit end state, making the labels ['None-start', 'a', 'b', 'b', 'a', 'None-end'].

There are a number of optional parameters that provide more control over the training process, including the use of distribution or edge inertia, freezing certain states, tying distributions or edges, and using pseudocounts. See the tutorial linked to at the top of this page for full details on each of these options.

2.15.5 API Reference

class pomegranate.hmm.HiddenMarkovModel

A Hidden Markov Model

A Hidden Markov Model (HMM) is a directed graphical model where nodes are hidden states which contain an observed emission distribution and edges contain the probability of transitioning from one hidden state to another. HMMs allow you to tag each observation in a variable length sequence with the most likely hidden state according to the model.

Parameters

name [str, optional] The name of the model. Default is None.

start [State, optional] An optional state to force the model to start in. Default is None.

end [State, optional] An optional state to force the model to end in. Default is None.

Examples

```
>>> from pomegranate import *
>>> d1 = DiscreteDistribution({'A' : 0.35, 'C' : 0.20, 'G' : 0.05, 'T' : 0.40})
>>> d2 = DiscreteDistribution({'A' : 0.25, 'C' : 0.25, 'G' : 0.25, 'T' : 0.25})
>>> d3 = DiscreteDistribution({'A' : 0.10, 'C' : 0.40, 'G' : 0.40, 'T' : 0.10})
>>>
>>> s1 = State(d1, name="s1")
>>> s2 = State(d2, name="s2")
>>> s3 = State(d3, name="s3")
>>>
>>> model = HiddenMarkovModel('example')
>>> model.add_states([s1, s2, s3])
>>> model.add_transition(model.start, s1, 0.90)
>>> model.add_transition(model.start, s2, 0.10)
>>> model.add_transition(s1, s1, 0.80)
>>> model.add_transition(s1, s2, 0.20)
>>> model.add_transition(s2, s2, 0.90)
>>> model.add_transition(s2, s3, 0.10)
>>> model.add_transition(s3, s3, 0.70)
>>> model.add_transition(s3, model.end, 0.30)
>>> model.bake()
```

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```
>>>
>>> print(model.log_probability(list('ACGACTATTCGAT')))
-22.73896159971087
>>> print(", ".join(state.name for i, state in model.viterbi(list('ACGACTATTCGAT
→'))[1]))
example-start, s1, s2, s2, s2, s2, s2, s2, s2, s2, s2, s2, s2, s3, example-end
```

Attributes**start** [State] A state object corresponding to the initial start of the model**end** [State] A state object corresponding to the forced end of the model**start_index** [int] The index of the start object in the state list**end_index** [int] The index of the end object in the state list**silent_start** [int] The index of the beginning of the silent states in the state list**states** [list] The list of all states in the model, with silent states at the end**add_edge()**

Add a transition from state a to state b which indicates that B is dependent on A in ways specified by the distribution.

add_model()

Add the states and edges of another model to this model.

Parameters**other** [HiddenMarkovModel] The other model to add**Returns****None****add_node()**

Add a node to the graph.

add_nodes()

Add multiple states to the graph.

add_state()

Add a state to the given model.

The state must not already be in the model, nor may it be part of any other model that will eventually be combined with this one.

Parameters**state** [State] A state object to be added to the model.**Returns****None****add_states()**

Add multiple states to the model at the same time.

Parameters**states** [list or generator] Either a list of states which are entered sequentially, or just comma separated values, for example `model.add_states(a, b, c, d)`.

Returns**None****add_transition()**

Add a transition from state a to state b.

Add a transition from state a to state b with the given (non-log) probability. Both states must be in the HMM already. `self.start` and `self.end` are valid arguments here. Probabilities will be normalized such that every node has edges summing to 1, leaving that node, but only when the model is baked. Pseudocounts are allowed as a way of using edge-specific pseudocounts for training.

By specifying a group as a string, you can tie edges together by giving them the same group. This means that a transition across one edge in the group counts as a transition across all edges in terms of training.

Parameters**a** [State] The state that the edge originates from**b** [State] The state that the edge goes to**probability** [double] The probability of transitioning from state a to state b in [0, 1]**pseudocount** [double, optional] The pseudocount to use for this specific edge if using edge pseudocounts for training. Defaults to the probability. Default is None.**group** [str, optional] The name of the group of edges to tie together during training. If groups are used, then a transition across any one edge counts as a transition across all edges. Default is None.**Returns****None****add_transitions()**

Add many transitions at the same time,

Parameters**a** [State or list] Either a state or a list of states where the edges originate.**b** [State or list] Either a state or a list of states where the edges go to.**probabilities** [list] The probabilities associated with each transition.**pseudocounts** [list, optional] The pseudocounts associated with each transition. Default is None.**groups** [list, optional] The groups of each edge. Default is None.**Returns****None****Examples**

```
>>> model.add_transitions([model.start, s1], [s1, model.end], [1., 1.])
>>> model.add_transitions([model.start, s1, s2, s3], s4, [0.2, 0.4, 0.3, 0.9])
>>> model.add_transitions(model.start, [s1, s2, s3], [0.6, 0.2, 0.05])
```

backward()

Run the backward algorithm on the sequence.

Calculate the probability of each observation being aligned to each state by going backward through a sequence. Returns the full backward matrix. Each index i, j corresponds to the sum-of-all-paths log probability of starting at the end of the sequence, and aligning observations to hidden states in such a manner that observation i was aligned to hidden state j . Uses row normalization to dynamically scale each row to prevent underflow errors.

If the sequence is impossible, will return a matrix of nans.

See also:

- Silent state handling taken from p. 71 of “Biological

Sequence Analysis” by Durbin et al., and works for anything which does not have loops of silent states.

- Row normalization technique explained by

<http://www.cs.sjsu.edu/~stamp/RUA/HMM.pdf> on p. 14.

Parameters

sequence [array-like] An array (or list) of observations.

Returns

matrix [array-like, shape (len(sequence), n_states)] The probability of aligning the sequences to states in a backward fashion.

bake ()

Finalize the topology of the model.

Finalize the topology of the model and assign a numerical index to every state. This method must be called before any of the probability- calculating methods.

This fills in self.states (a list of all states in order) and self.transition_log_probabilities (log probabilities for transitions), as well as self.start_index and self.end_index, and self.silent_start (the index of the first silent state).

Parameters

verbose [bool, optional] Return a log of changes made to the model during normalization or merging. Default is False.

merge [“None”, “Partial”, “All”] Merging has three options: “None”: No modifications will be made to the model. “Partial”: A silent state which only has a probability 1 transition

to another silent state will be merged with that silent state. This means that if silent state “S1” has a single transition to silent state “S2”, that all transitions to S1 will now go to S2, with the same probability as before, and S1 will be removed from the model.

“All”: A silent state with a probability 1 transition to any other state, silent or symbol emitting, will be merged in the manner described above. In addition, any orphan states will be removed from the model. An orphan state is a state which does not have any transitions to it OR does not have any transitions from it, except for the start and end of the model. This will iteratively remove orphan chains from the model. This is sometimes desirable, as all states should have both a transition in to get to that state, and a transition out, even if it is only to itself. If the state does not have either, the HMM will likely not work as intended.

Default is ‘All’.

Returns

None

clear_summaries ()

Clear the summary statistics stored in the object.

Parameters

None

Returns

None

concatenate ()

Concatenate this model to another model.

Concatenate this model to another model in such a way that a single probability 1 edge is added between self.end and other.start. Rename all other states appropriately by adding a suffix or prefix if needed.

Parameters

other [HiddenMarkovModel] The other model to concatenate

suffix [str, optional] Add the suffix to the end of all state names in the other model. Default is ‘’.

prefix [str, optional] Add the prefix to the beginning of all state names in the other model. Default is ‘’.

Returns

None

copy ()

Returns a deep copy of the HMM.

Parameters

None

Returns

model [HiddenMarkovModel] A deep copy of the model with entirely new objects.

dense_transition_matrix ()

Returns the dense transition matrix.

Parameters

None

Returns

matrix [numpy.ndarray, shape (n_states, n_states)] A dense transition matrix, containing the log probability of transitioning from each state to each other state.

edge_count ()

Returns the number of edges present in the model.

fit ()

Fit the model to data using either Baum-Welch, Viterbi, or supervised training.

Given a list of sequences, performs re-estimation on the model parameters. The two supported algorithms are “baum-welch”, “viterbi”, and “labeled”, indicating their respective algorithm. “labeled” corresponds to supervised learning that requires passing in a matching list of labels for each symbol seen in the sequences.

Training supports a wide variety of other options including using edge pseudocounts and either edge or distribution inertia.

Parameters

sequences [array-like] An array of some sort (list, numpy.ndarray, tuple..) of sequences, where each sequence is a numpy array, which is 1 dimensional if the HMM is a one dimensional array, or multidimensional if the HMM supports multiple dimensions.

weights [array-like or None, optional] An array of weights, one for each sequence to train on. If None, all sequences are equally weighted. Default is None.

labels [array-like or None, optional] An array of state labels for each sequence. This is only used in 'labeled' training. If used this must be comprised of n lists where n is the number of sequences to train on, and each of those lists must have one label per observation. A None in this list corresponds to no labels for the entire sequence and triggers semi-supervised learning, where the labeled sequences are summarized using labeled fitting and the unlabeled are summarized using the specified algorithm. Default is None.

stop_threshold [double, optional] The threshold the improvement ratio of the models log probability in fitting the scores. Default is 1e-9.

min_iterations [int, optional] The minimum number of iterations to run Baum-Welch training for. Default is 0.

max_iterations [int, optional] The maximum number of iterations to run Baum-Welch training for. Default is 1e8.

algorithm ['baum-welch', 'viterbi', 'labeled'] The training algorithm to use. Baum-Welch uses the forward-backward algorithm to train using a version of structured EM. Viterbi iteratively runs the sequences through the Viterbi algorithm and then uses hard assignments of observations to states using that. Default is 'baum-welch'. Labeled training requires that labels are provided for each observation in each sequence.

pseudocount [double, optional] A pseudocount to add to both transitions and emissions. If supplied, it will override both `transition_pseudocount` and `emission_pseudocount` in the same way that specifying `inertia` will override both `edge_inertia` and `distribution_inertia`. Default is None.

transition_pseudocount [double, optional] A pseudocount to add to all transitions to add a prior to the MLE estimate of the transition probability. Default is 0.

emission_pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Only effects hidden Markov models defined over discrete distributions. Default is 0.

use_pseudocount [bool, optional] Whether to use the pseudocounts defined in the `add_edge` method for edge-specific pseudocounts when updating the transition probability parameters. Does not effect the `transition_pseudocount` and `emission_pseudocount` parameters, but can be used in addition to them. Default is False.

inertia [double or None, optional, range [0, 1]] If double, will set both `edge_inertia` and `distribution_inertia` to be that value. If None, will not override those values. Default is None.

edge_inertia [bool, optional, range [0, 1]] Whether to use inertia when updating the transition probability parameters. Default is 0.0.

distribution_inertia [double, optional, range [0, 1]] Whether to use inertia when updating the distribution parameters. Default is 0.0.

batches_per_epoch [int or None, optional] The number of batches in an epoch. This is the number of batches to summarize before calling *from_summaries* and updating the model parameters. This allows one to do minibatch updates by updating the model parameters before setting the full dataset. If set to None, uses the full dataset. Default is None.

lr_decay [double, optional, positive] The step size decay as a function of the number of iterations. Functionally, this sets the inertia to be $(2+k)^{-lr_decay}$ where k is the number of iterations. This causes initial iterations to have more of an impact than later iterations, and is frequently used in minibatch learning. This value is suggested to be between 0.5 and 1. Default is 0, meaning no decay.

callbacks [list, optional] A list of callback objects that describe functionality that should be undertaken over the course of training.

return_history [bool, optional] Whether to return the history during training as well as the model.

verbose [bool, optional] Whether to print the improvement in the model fitting at each iteration. Default is True.

n_jobs [int, optional] The number of threads to use when performing training. This leads to exact updates. Default is 1.

Returns

improvement [double] The total improvement in fitting the model to the data

`forward()`

Run the forward algorithm on the sequence.

Calculate the probability of each observation being aligned to each state by going forward through a sequence. Returns the full forward matrix. Each index i, j corresponds to the sum-of-all-paths log probability of starting at the beginning of the sequence, and aligning observations to hidden states in such a manner that observation i was aligned to hidden state j . Uses row normalization to dynamically scale each row to prevent underflow errors.

If the sequence is impossible, will return a matrix of nans.

See also:

- Silent state handling taken from p. 71 of “Biological

Sequence Analysis” by Durbin et al., and works for anything which does not have loops of silent states.

- Row normalization technique explained by

<http://www.cs.sjsu.edu/~stamp/RUA/HMM.pdf> on p. 14.

Parameters

sequence [array-like] An array (or list) of observations.

Returns

matrix [array-like, shape (len(sequence), n_states)] The probability of aligning the sequences to states in a forward fashion.

`forward_backward()`

Run the forward-backward algorithm on the sequence.

This algorithm returns an emission matrix and a transition matrix. The emission matrix returns the normalized probability that each each state generated that emission given both the symbol and the entire sequence. The transition matrix returns the expected number of times that a transition is used.

If the sequence is impossible, will return (None, None)

See also:

- Forward and backward algorithm implementations. A comprehensive

description of the forward, backward, and forward-background algorithm is here: http://en.wikipedia.org/wiki/Forward%E2%80%93backward_algorithm

Parameters

sequence [array-like] An array (or list) of observations.

Returns

emissions [array-like, shape (len(sequence), n_nonsilent_states)] The normalized probabilities of each state generating each emission.

transitions [array-like, shape (n_states, n_states)] The expected number of transitions across each edge in the model.

freeze ()

Freeze the distribution, preventing updates from occurring.

freeze_distributions ()

Freeze all the distributions in model.

Upon training only edges will be updated. The parameters of distributions will not be affected.

Parameters

None

Returns

None

from_json ()

Read in a serialized model and return the appropriate classifier.

Parameters

s [str] A JSON formatted string containing the file.

Returns

—

model [object] A properly initialized and baked model.

from_matrix ()

Create a model from a more standard matrix format.

Take in a 2D matrix of floats of size n by n , which are the transition probabilities to go from any state to any other state. May also take in a list of length n representing the names of these nodes, and a model name. Must provide the matrix, and a list of size n representing the distribution you wish to use for that state, a list of size n indicating the probability of starting in a state, and a list of size n indicating the probability of ending in a state.

Parameters

transition_probabilities [array-like, shape (n_states, n_states)] The probabilities of each state transitioning to each other state.

distributions [array-like, shape (n_states)] The distributions for each state. Silent states are indicated by using `None` instead of a distribution object.

starts [array-like, shape (n_states)] The probabilities of starting in each of the states.

ends [array-like, shape (n_states), optional] If passed in, the probabilities of ending in each of the states. If ends is None, then assumes the model has no explicit end state. Default is None.

state_names [array-like, shape (n_states), optional] The name of the states. If None is passed in, default names are generated. Default is None

name [str, optional] The name of the model. Default is None

verbose [bool, optional] The verbose parameter for the underlying bake method. Default is False.

merge ['None', 'Partial', 'All', optional] The merge parameter for the underlying bake method. Default is All

Returns

model [HiddenMarkovModel] The baked model ready to go.

Examples

```
matrix = [[0.4, 0.5], [0.4, 0.5]] distributions = [NormalDistribution(1, .5), NormalDistribution(5, 2)] starts = [1., 0.] ends = [.1., .1] state_names= ["A", "B"]
```

```
model = Model.from_matrix(matrix, distributions, starts, ends, state_names, name="test_model")
```

`from_samples()`

Learn the transitions and emissions of a model directly from data.

This method will learn both the transition matrix, emission distributions, and start probabilities for each state. This will only return a dense graph without any silent states or explicit transitions to an end state. Currently all components must be defined as the same distribution, but soon this restriction will be removed.

If learning a multinomial HMM over discrete characters, the initial emission probabilities are initialized randomly. If learning a continuous valued HMM, such as a Gaussian HMM, then kmeans clustering is used first to identify initial clusters.

Regardless of the type of model, the transition matrix and start probabilities are initialized uniformly. Then the specified learning algorithm (Baum-Welch recommended) is used to refine the parameters of the model.

Parameters

distribution [callable] The emission distribution of the components of the model.

n_components [int] The number of states (or components) to initialize.

X [array-like or generator] An array of some sort (list, numpy.ndarray, tuple..) of sequences, where each sequence is a numpy array, which is 1 dimensional if the HMM is a one dimensional array, or multidimensional if the HMM supports multiple dimensions. Alternatively, a data generator object that yields sequences.

weights [array-like or None, optional] An array of weights, one for each sequence to train on. If None, all sequences are equally weighted. Default is None.

labels [array-like or None, optional] An array of state labels for each sequence. This is only used in 'labeled' training. If used this must be comprised of n lists where n is the number of sequences to train on, and each of those lists must have one label per observation. A None in this list corresponds to no labels for the entire sequence and triggers semi-supervised learning, where the labeled sequences are summarized using labeled fitting and the unlabeled are summarized using the specified algorithm. Default is None.

- algorithm** ['baum-welch', 'viterbi', 'labeled'] The training algorithm to use. Baum-Welch uses the forward-backward algorithm to train using a version of structured EM. Viterbi iteratively runs the sequences through the Viterbi algorithm and then uses hard assignments of observations to states using that. Default is 'baum-welch'. Labeled training requires that labels are provided for each observation in each sequence.
- inertia** [double or None, optional, range [0, 1]] If double, will set both `edge_inertia` and `distribution_inertia` to be that value. If None, will not override those values. Default is None.
- edge_inertia** [bool, optional, range [0, 1]] Whether to use inertia when updating the transition probability parameters. Default is 0.0.
- distribution_inertia** [double, optional, range [0, 1]] Whether to use inertia when updating the distribution parameters. Default is 0.0.
- pseudocount** [double, optional] A pseudocount to add to both transitions and emissions. If supplied, it will override both `transition_pseudocount` and `emission_pseudocount` in the same way that specifying *inertia* will override both *edge_inertia* and *distribution_inertia*. Default is None.
- transition_pseudocount** [double, optional] A pseudocount to add to all transitions to add a prior to the MLE estimate of the transition probability. Default is 0.
- emission_pseudocount** [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Only effects hidden Markov models defined over discrete distributions. Default is 0.
- use_pseudocount** [bool, optional] Whether to use the pseudocounts defined in the *add_edge* method for edge-specific pseudocounts when updating the transition probability parameters. Does not effect the *transition_pseudocount* and *emission_pseudocount* parameters, but can be used in addition to them. Default is False.
- stop_threshold** [double, optional] The threshold the improvement ratio of the models log probability in fitting the scores. Default is 1e-9.
- min_iterations** [int, optional] The minimum number of iterations to run Baum-Welch training for. Default is 0.
- max_iterations** [int, optional] The maximum number of iterations to run Baum-Welch training for. Default is 1e8.
- n_init** [int, optional] The number of times to initialize the k-means clustering before taking the best value. Default is 1.
- init** [str, optional] The initialization method for kmeans. Must be one of 'first-k', 'random', 'kmeans++', or 'kmeansll'. Default is kmeans++.
- max_kmeans_iterations** [int, optional] The number of iterations to run k-means for before starting EM.
- initialization_batch_size** [int or None, optional] The number of batches to use to initialize the model. None means use the entire data set. Default is None.
- batches_per_epoch** [int or None, optional] The number of batches in an epoch. This is the number of batches to summarize before calling *from_summaries* and updating the model parameters. This allows one to do minibatch updates by updating the model parameters before setting the full dataset. If set to None, uses the full dataset. Default is None.
- lr_decay** [double, optional, positive] The step size decay as a function of the number of iterations. Functionally, this sets the inertia to be $(2+k)^{-lr_decay}$ where k is the number

of iterations. This causes initial iterations to have more of an impact than later iterations, and is frequently used in minibatch learning. This value is suggested to be between 0.5 and 1. Default is 0, meaning no decay.

end_state [bool, optional] Whether to calculate the probability of ending in each state or not. Default is False.

state_names [array-like, shape (n_states), optional] The name of the states. If None is passed in, default names are generated. Default is None

name [str, optional] The name of the model. Default is None

keys [list] A list of sets where each set is the keys present in that column. If there are d columns in the data set then this list should have d sets and each set should have at least two keys in it.

random_state [int, numpy.random.RandomState, or None] The random state used for generating samples. If set to none, a random seed will be used. If set to either an integer or a random seed, will produce deterministic outputs.

callbacks [list, optional] A list of callback objects that describe functionality that should be undertaken over the course of training.

return_history [bool, optional] Whether to return the history during training as well as the model.

verbose [bool, optional] Whether to print the improvement in the model fitting at each iteration. Default is True.

n_jobs [int, optional] The number of threads to use when performing training. This leads to exact updates. Default is 1.

Returns

model [HiddenMarkovModel] The model fit to the data.

from_summaries ()

Fit the model to the stored summary statistics.

Parameters

inertia [double or None, optional] The inertia to use for both edges and distributions without needing to set both of them. If None, use the values passed in to those variables. Default is None.

pseudocount [double, optional] A pseudocount to add to both transitions and emissions. If supplied, it will override both `transition_pseudocount` and `emission_pseudocount` in the same way that specifying `inertia` will override both `edge_inertia` and `distribution_inertia`. Default is None.

transition_pseudocount [double, optional] A pseudocount to add to all transitions to add a prior to the MLE estimate of the transition probability. Default is 0.

emission_pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Only effects hidden Markov models defined over discrete distributions. Default is 0.

use_pseudocount [bool, optional] Whether to use the pseudocounts defined in the `add_edge` method for edge-specific pseudocounts when updating the transition probability parameters. Does not effect the `transition_pseudocount` and `emission_pseudocount` parameters, but can be used in addition to them. Default is False.

edge_inertia [bool, optional, range [0, 1]] Whether to use inertia when updating the transition probability parameters. Default is 0.0.

distribution_inertia [double, optional, range [0, 1]] Whether to use inertia when updating the distribution parameters. Default is 0.0.

Returns

None

from_yaml ()

Deserialize this object from its YAML representation.

log_probability ()

Calculate the log probability of a single sequence.

If a path is provided, calculate the log probability of that sequence given the path.

Parameters

sequence [array-like] Return the array of observations in a single sequence of data

check_input [bool, optional] Check to make sure that all emissions fall under the support of the emission distributions. Default is True.

Returns

logp [double] The log probability of the sequence

maximum_a_posteriori ()

Run posterior decoding on the sequence.

MAP decoding is an alternative to viterbi decoding, which returns the most likely state for each observation, based on the forward-backward algorithm. This is also called posterior decoding. This method is described on p. 14 of http://ai.stanford.edu/~serafim/CS262_2007/notes/lecture5.pdf

WARNING: This may produce impossible sequences.

Parameters

sequence [array-like] An array (or list) of observations.

Returns

logp [double] The log probability of the sequence under the Viterbi path

path [list of tuples] Tuples of (state index, state object) of the states along the posterior path.

node_count ()

Returns the number of nodes/states in the model

plot ()

Draw this model's graph using NetworkX and matplotlib.

Note that this relies on networkx's built-in graphing capabilities (and not Graphviz) and thus can't draw self-loops.

See `networkx.draw_networkx()` for the keywords you can pass in.

Parameters

precision [int, optional] The precision with which to round edge probabilities. Default is 4.

****kwargs** [any] The arguments to pass into `networkx.draw_networkx()`

Returns

None

predict ()

Calculate the most likely state for each observation.

This can be either the Viterbi algorithm or maximum a posteriori. It returns the probability of the sequence under that state sequence and the actual state sequence.

This is a sklearn wrapper for the Viterbi and maximum_a_posteriori methods.

Parameters

sequence [array-like] An array (or list) of observations.

algorithm ["map", "viterbi"] The algorithm with which to decode the sequence

Returns

path [list of integers] A list of the ids of states along the MAP or the Viterbi path.

predict_log_proba ()

Calculate the state log probabilities for each observation in the sequence.

Run the forward-backward algorithm on the sequence and return the emission matrix. This is the log normalized probability that each each state generated that emission given both the symbol and the entire sequence.

This is a sklearn wrapper for the forward backward algorithm.

See also:

- Forward and backward algorithm implementations. A comprehensive

description of the forward, backward, and forward-background algorithm is here: http://en.wikipedia.org/wiki/Forward%E2%80%93backward_algorithm

Parameters

sequence [array-like] An array (or list) of observations.

Returns

emissions [array-like, shape (len(sequence), n_nonsilent_states)] The log normalized probabilities of each state generating each emission.

predict_proba ()

Calculate the state probabilities for each observation in the sequence.

Run the forward-backward algorithm on the sequence and return the emission matrix. This is the normalized probability that each each state generated that emission given both the symbol and the entire sequence.

This is a sklearn wrapper for the forward backward algorithm.

See also:

- Forward and backward algorithm implementations. A comprehensive

description of the forward, backward, and forward-background algorithm is here: http://en.wikipedia.org/wiki/Forward%E2%80%93backward_algorithm

Parameters

sequence [array-like] An array (or list) of observations.

Returns

emissions [array-like, shape (len(sequence), n_nonsilent_states)] The normalized probabilities of each state generating each emission.

probability ()

Return the probability of the given symbol under this distribution.

Parameters

symbol [object] The symbol to calculate the probability of

Returns

probability [double] The probability of that point under the distribution.

sample ()

Generate a sequence from the model.

Returns the sequence generated, as a list of emitted items. The model must have been baked first in order to run this method.

If a length is specified and the HMM is infinite (no edges to the end state), then that number of samples will be randomly generated. If the length is specified and the HMM is finite, the method will attempt to generate a prefix of that length. Currently it will force itself to not take an end transition unless that is the only path, making it not a true random sample on a finite model.

WARNING: If the HMM has no explicit end state, must specify a length to use.

Parameters

n [int or None, optional] The number of samples to generate. If None, return only one sample.

length [int, optional] Generate a sequence with a maximal length of this size. Used if you have no explicit end state. Default is 0.

path [bool, optional] Return the path of hidden states in addition to the emissions. If true will return a tuple of (sample, path). Default is False.

random_state [int, numpy.random.RandomState, or None] The random state used for generating samples. If set to none, a random seed will be used. If set to either an integer or a random seed, will produce deterministic outputs.

Returns

sample [list or tuple] If path is true, return a tuple of (sample, path), otherwise return just the samples.

score ()

Return the accuracy of the model on a data set.

Parameters

X [numpy.ndarray, shape=(n, d)] The values of the data set

y [numpy.ndarray, shape=(n,)] The labels of each value

state_count ()

Returns the number of states present in the model.

summarize ()

Summarize data into stored sufficient statistics for out-of-core training. Only implemented for Baum-Welch training since Viterbi is less memory intensive.

Parameters

sequences [array-like] An array of some sort (list, numpy.ndarray, tuple..) of sequences, where each sequence is a numpy array, which is 1 dimensional if the HMM is a one dimensional array, or multidimensional if the HMM supports multiple dimensions.

weights [array-like or None, optional] An array of weights, one for each sequence to train on. If None, all sequences are equally weighted. Default is None.

labels [array-like or None, optional] An array of state labels for each sequence. This is only used in ‘labeled’ training. If used this must be comprised of n lists where n is the number of sequences to train on, and each of those lists must have one label per observation. Default is None.

algorithm [‘baum-welch’, ‘viterbi’, ‘labeled’] The training algorithm to use. Baum-Welch uses the forward-backward algorithm to train using a version of structured EM. Viterbi iteratively runs the sequences through the Viterbi algorithm and then uses hard assignments of observations to states using that. Default is ‘baum-welch’. Labeled training requires that labels are provided for each observation in each sequence.

check_input [bool, optional] Check the input. This casts the input sequences as numpy arrays, and converts non-numeric inputs into numeric inputs for faster processing later. Default is True.

Returns

logp [double] The log probability of the sequences.

thaw()

Thaw the distribution, re-allowing updates to occur.

thaw_distributions()

Thaw all distributions in the model.

Upon training distributions will be updated again.

Parameters

None

Returns

None

to_json()

Serialize the model to a JSON.

Parameters

separators [tuple, optional] The two separators to pass to the json.dumps function for formatting.

indent [int, optional] The indentation to use at each level. Passed to json.dumps for formatting.

Returns

json [str] A properly formatted JSON object.

to_yaml()

Serialize the model to YAML for compactness.

viterbi()

Run the Viterbi algorithm on the sequence.

Run the Viterbi algorithm on the sequence given the model. This finds the ML path of hidden states given the sequence. Returns a tuple of the log probability of the ML path, or (-inf, None) if the sequence is

impossible under the model. If a path is returned, it is a list of tuples of the form (sequence index, state object).

This is fundamentally the same as the forward algorithm using max instead of sum, except the traceback is more complicated, because silent states in the current step can trace back to other silent states in the current step as well as states in the previous step.

See also:

- Viterbi implementation described well in the wikipedia article

http://en.wikipedia.org/wiki/Viterbi_algorithm

Parameters

sequence [array-like] An array (or list) of observations.

Returns

logp [double] The log probability of the sequence under the Viterbi path

path [list of tuples] Tuples of (state index, state object) of the states along the Viterbi path.

2.16 Bayes Classifiers and Naive Bayes

IPython Notebook Tutorial

Bayes classifiers are simple probabilistic classification models based off of Bayes theorem. See the above tutorial for a full primer on how they work, and what the distinction between a naive Bayes classifier and a Bayes classifier is. Essentially, each class is modeled by a probability distribution and classifications are made according to what distribution fits the data the best. They are a supervised version of general mixture models, in that the `predict`, `predict_proba`, and `predict_log_proba` methods return the same values for the same underlying distributions, but that instead of using expectation-maximization to fit to new data they can use the provided labels directly.

2.16.1 Initialization

Bayes classifiers and naive Bayes can both be initialized in one of two ways depending on if you know the parameters of the model beforehand or not, (1) passing in a list of pre-initialized distributions to the model, or (2) using the `from_samples` class method to initialize the model directly from data. For naive Bayes models on multivariate data, the pre-initialized distributions must be a list of `IndependentComponentDistribution` objects since each dimension is modeled independently from the others. For Bayes classifiers on multivariate data a list of any type of multivariate distribution can be provided. For univariate data the two models produce identical results, and can be passed in a list of univariate distributions. For example:

```
from pomegranate import *
d1 = IndependentComponentsDistribution([NormalDistribution(5, 2),
↳NormalDistribution(6, 1), NormalDistribution(9, 1)])
d2 = IndependentComponentsDistribution([NormalDistribution(2, 1),
↳NormalDistribution(8, 1), NormalDistribution(5, 1)])
d3 = IndependentComponentsDistribution([NormalDistribution(3, 1),
↳NormalDistribution(5, 3), NormalDistribution(4, 1)])
model = NaiveBayes([d1, d2, d3])
```

would create a three class naive Bayes classifier that modeled data with three dimensions. Alternatively, we can initialize a Bayes classifier in the following manner

```

from pomegranate import *
d1 = MultivariateGaussianDistribution([5, 6, 9], [[2, 0, 0], [0, 1, 0], [0, 0, 1]])
d2 = MultivariateGaussianDistribution([2, 8, 5], [[1, 0, 0], [0, 1, 0], [0, 0, 1]])
d3 = MultivariateGaussianDistribution([3, 5, 4], [[1, 0, 0], [0, 3, 0], [0, 0, 1]])
model = BayesClassifier([d1, d2, d3])

```

The two examples above functionally create the same model, as the Bayes classifier uses multivariate Gaussian distributions with the same means and a diagonal covariance matrix containing only the variances. However, if we were to fit these models to data later on, the Bayes classifier would learn a full covariance matrix while the naive Bayes would only learn the diagonal.

If we instead wish to initialize our model directly onto data, we use the `from_samples` class method.

```

from pomegranate import *
import numpy
X = numpy.load('data.npy')
y = numpy.load('labels.npy')
model = NaiveBayes.from_samples(NormalDistribution, X, y)

```

This would create a naive Bayes model directly from the data with normal distributions modeling each of the dimensions, and a number of components equal to the number of classes in `y`. Alternatively if we wanted to create a model with different distributions for each dimension we can do the following:

```

>>> model = NaiveBayes.from_samples([NormalDistribution, ExponentialDistribution], X, y)

```

This assumes that your data is two dimensional and that you want to model the first distribution as a normal distribution and the second dimension as an exponential distribution.

We can do pretty much the same thing with Bayes classifiers, except passing in a more complex model.

```

>>> model = BayesClassifier.from_samples(MultivariateGaussianDistribution, X, y)

```

One can use much more complex models than just a multivariate Gaussian with a full covariance matrix when using a Bayes classifier. Specifically, you can also have your distributions be general mixture models, hidden Markov models, and Bayesian networks. For example:

```

>>> model = BayesClassifier.from_samples(BayesianNetwork, X, y)

```

That would require that the data is only discrete valued currently, and the structure learning task may be too long if not set appropriately. However, it is possible. Currently, one cannot simply put in `GeneralMixtureModel` or `HiddenMarkovModel` despite them having a `from_samples` method because there is a great deal of flexibility in terms of the structure or emission distributions. The easiest way to set up one of these more complex models is to build each of the components separately and then feed them into the Bayes classifier method using the first initialization method.

```

>>> d1 = GeneralMixtureModel.from_samples(MultivariateGaussianDistribution, n_
↳ components=5, X=X[y==0])
>>> d2 = GeneralMixtureModel.from_samples(MultivariateGaussianDistribution, n_
↳ components=5, X=X[y==1])
>>> model = BayesClassifier([d1, d2])

```

2.16.2 Prediction

Bayes classifiers and naive Bayes supports the same three prediction methods that the other models support, `predict`, `predict_proba`, and `predict_log_proba`. These methods return the most likely class given the data (`argmaxm P(MID)`), the probability of each class given the data (`P(MID)`), and the log probability of each class

given the data (log P(MID)). It is best to always pass in a 2D matrix even for univariate data, where it would have a shape of (n, 1).

The `predict` method takes in samples and returns the most likely class given the data.

```
from pomegranate import *
model = NaiveBayes([NormalDistribution(5, 2), UniformDistribution(0, 10),
↳ExponentialDistribution(1.0)])
model.predict(np.array([[0], [1], [2], [3], [4]]))
[2, 2, 2, 0, 0]
```

Calling `predict_proba` on five samples for a Naive Bayes with univariate components would look like the following.

```
from pomegranate import *
model = NaiveBayes([NormalDistribution(5, 2), UniformDistribution(0, 10),
↳ExponentialDistribution(1)])
model.predict_proba(np.array([[0], [1], [2], [3], [4]]))
[[ 0.00790443  0.09019051  0.90190506]
 [ 0.05455011  0.20207126  0.74337863]
 [ 0.21579499  0.33322883  0.45097618]
 [ 0.44681566  0.36931382  0.18387052]
 [ 0.59804205  0.33973357  0.06222437]]
```

Multivariate models work the same way.

```
from pomegranate import *
d1 = MultivariateGaussianDistribution([5, 5], [[1, 0], [0, 1]])
d2 = IndependentComponentsDistribution([NormalDistribution(5, 2),
↳NormalDistribution(5, 2)])
model = BayesClassifier([d1, d2])
clf.predict_proba(np.array([[0, 4],
                             [1, 3],
                             [2, 2],
                             [3, 1],
                             [4, 0]]))
array([[ 0.00023312,  0.99976688],
       [ 0.00220745,  0.99779255],
       [ 0.00466169,  0.99533831],
       [ 0.00220745,  0.99779255],
       [ 0.00023312,  0.99976688]])
```

`predict_log_proba` works the same way, returning the log probabilities instead of the probabilities.

2.16.3 Fitting

Both naive Bayes and Bayes classifiers also have a `fit` method that updates the parameters of the model based on new data. The major difference between these methods and the others presented is that these are supervised methods and so need to be passed labels in addition to data. This change propagates also to the `summarize` method, where labels are provided as well.

```
from pomegranate import *
d1 = MultivariateGaussianDistribution([5, 5], [[1, 0], [0, 1]])
d2 = IndependentComponentsDistribution(NormalDistribution(5, 2), NormalDistribution(5,
↳ 2))
model = BayesClassifier([d1, d2])
```

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```
X = np.array([[6.0, 5.0],
              [3.5, 4.0],
              [7.5, 1.5],
              [7.0, 7.0 ]])
y = np.array([0, 0, 1, 1])
model.fit(X, y)
```

As we can see, there are four samples, with the first two samples labeled as class 0 and the last two samples labeled as class 1. Keep in mind that the training samples must match the input requirements for the models used. So if using a univariate distribution, then each sample must contain one item. A bivariate distribution, two. For hidden markov models, the sample can be a list of observations of any length. An example using hidden markov models would be the following.

```
d1 = HiddenMarkovModel...
d2 = HiddenMarkovModel...
d3 = HiddenMarkovModel...
model = BayesClassifier([d1, d2, d3])
X = np.array([list('HHHHHTHTHTTTTH'),
              list('HHTHHTTTHHHHTH'),
              list('TH'),
              list('HHHHT')])
y = np.array([2, 2, 1, 0])
model.fit(X, y)
```

2.16.4 API Reference

class pomegranate.NaiveBayes.NaiveBayes

A naive Bayes model, a supervised alternative to GMM.

A naive Bayes classifier, that treats each dimension independently from each other. This is a simpler version of the Bayes Classifier, that can use any distribution with any covariance structure, including Bayesian networks and hidden Markov models.

Parameters

models [list] A list of initialized distributions.

weights [list or numpy.ndarray or None, default None] The prior probabilities of the components. If None is passed in then defaults to the uniformly distributed priors.

Examples

```
>>> from pomegranate import *
>>> X = [0, 2, 0, 1, 0, 5, 6, 5, 7, 6]
>>> y = [0, 0, 0, 0, 0, 1, 1, 0, 1, 1]
>>> clf = NaiveBayes.from_samples(NormalDistribution, X, y)
>>> clf.predict_proba([6])
array([[0.01973451,  0.98026549]])
```

```
>>> from pomegranate import *
>>> clf = NaiveBayes([NormalDistribution(1, 2), NormalDistribution(0, 1)])
>>> clf.predict_log_proba([[0], [1], [2], [-1]])
array([[ -1.1836569 , -0.36550972],
       [-0.79437677, -0.60122959],
```

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```
[-0.26751248, -1.4493653],
[-1.09861229, -0.40546511]])
```

Attributes

models [list] The model objects, either initialized by the user or fit to data.

weights [numpy.ndarray] The prior probability of each component of the model.

clear_summaries ()

Remove the stored sufficient statistics.

Parameters

None

Returns

None

copy ()

Return a deep copy of this distribution object.

This object will not be tied to any other distribution or connected in any form.

Parameters

None

Returns

distribution [Distribution] A copy of the distribution with the same parameters.

fit ()

Fit the Bayes classifier to the data by passing data to its components.

The fit step for a Bayes classifier with purely labeled data is a simple MLE update on the underlying distributions, grouped by the labels. However, in the semi-supervised the model is trained on a mixture of both labeled and unlabeled data, where the unlabeled data uses the label -1. In this setting, EM is used to train the model. The model is initialized using the labeled data and then sufficient statistics are gathered for both the labeled and unlabeled data, combined, and used to update the parameters.

Parameters

X [numpy.ndarray or list] The dataset to operate on. For most models this is a numpy array with columns corresponding to features and rows corresponding to samples. For markov chains and HMMs this will be a list of variable length sequences.

y [numpy.ndarray or list or None] Data labels for supervised training algorithms.

weights [array-like or None, shape (n_samples,), optional] The initial weights of each sample in the matrix. If nothing is passed in then each sample is assumed to be the same weight. Default is None.

inertia [double, optional] Inertia used for the training the distributions.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Default is 0.

stop_threshold [double, optional, positive] The threshold at which EM will terminate for the improvement of the model. If the model does not improve its fit of the data by a log

probability of 0.1 then terminate. Only required if doing semisupervised learning. Default is 0.1.

max_iterations [int, optional, positive] The maximum number of iterations to run EM for. If this limit is hit then it will terminate training, regardless of how well the model is improving per iteration. Only required if doing semisupervised learning. Default is 1e8.

callbacks [list, optional] A list of callback objects that describe functionality that should be undertaken over the course of training. Only used for semi-supervised learning.

return_history [bool, optional] Whether to return the history during training as well as the model. Only used for semi-supervised learning.

verbose [bool, optional] Whether or not to print out improvement information over iterations. Only required if doing semisupervised learning. Default is False.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

Returns

self [object] Returns the fitted model

freeze ()

Freeze the distribution, preventing updates from occurring.

from_json ()

Deserialize this object from its JSON representation.

from_samples ()

Create a naive Bayes classifier directly from the given dataset.

This will initialize the distributions using maximum likelihood estimates derived by partitioning the dataset using the label vector. If any labels are missing, the model will be trained using EM in a semi-supervised setting.

A homogeneous model can be defined by passing in a single distribution callable as the first parameter and specifying the number of components, while a heterogeneous model can be defined by passing in a list of callables of the appropriate type.

A naive Bayes classifier is a subset of the Bayes classifier in that the math is identical, but the distributions are independent for each feature. Simply put, one can create a multivariate Gaussian Bayes classifier with a full covariance matrix, but a Gaussian naive Bayes would require a diagonal covariance matrix.

Parameters

distributions [array-like, shape (n_components,) or callable]

The components of the model. This should either be a single callable if all components will be the same distribution, or an array of callables, one for each feature.

X [array-like or generator, shape (n_samples, n_dimensions)] This is the data to train on. Each row is a sample, and each column is a dimension to train on.

y [array-like, shape (n_samples,)] The labels for each sample. The labels should be integers between 0 and k-1 for a problem with k classes, or -1 if the label is not known for that sample.

weights [array-like, shape (n_samples,), optional] The initial weights of each sample in the matrix. If nothing is passed in then each sample is assumed to be the same weight. Default is None.

pseudocount [double, optional, positive] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Only effects mixture models defined over discrete distributions. Default is 0.

stop_threshold [double, optional, positive] The threshold at which EM will terminate for the improvement of the model. If the model does not improve its fit of the data by a log probability of 0.1 then terminate. Only required if doing semisupervised learning. Default is 0.1.

max_iterations [int, optional, positive] The maximum number of iterations to run EM for. If this limit is hit then it will terminate training, regardless of how well the model is improving per iteration. Only required if doing semisupervised learning. Default is 1e8.

callbacks [list, optional] A list of callback objects that describe functionality that should be undertaken over the course of training.

return_history [bool, optional] Whether to return the history during training as well as the model.

verbose [bool, optional] Whether or not to print out improvement information over iterations. Only required if doing semisupervised learning. Default is False.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. Default is 1.

Returns

model [NaiveBayes] The fit naive Bayes model.

from_summaries ()

Fit the model to the collected sufficient statistics.

Fit the parameters of the model to the sufficient statistics gathered during the summarize calls. This should return an exact update.

Parameters

inertia [double, optional] The weight of the previous parameters of the model. The new parameters will roughly be $\text{old_param} \times \text{inertia} + \text{new_param} \times (1 - \text{inertia})$, so an inertia of 0 means ignore the old parameters, whereas an inertia of 1 means ignore the new parameters. Default is 0.0.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. If discrete data, will smooth both the prior probabilities of each component and the emissions of each component. Otherwise, will only smooth the prior probabilities of each component. Default is 0.

Returns

None

from_yaml ()

Deserialize this object from its YAML representation.

log_probability ()

Calculate the log probability of a point under the distribution.

The probability of a point is the sum of the probabilities of each distribution multiplied by the weights. Thus, the log probability is the sum of the log probability plus the log prior.

This is the python interface.

Parameters

X [numpy.ndarray, shape=(n, d) or (n, m, d)] The samples to calculate the log probability of. Each row is a sample and each column is a dimension. If emissions are HMMs then shape is (n, m, d) where m is variable length for each observation, and X becomes an array of n (m, d)-shaped arrays.

n_jobs [int, optional] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

log_probability [double] The log probability of the point under the distribution.

`predict ()`

Predict the most likely component which generated each sample.

Calculate the posterior P(MID) for each sample and return the index of the component most likely to fit it. This corresponds to a simple argmax over the responsibility matrix.

This is a sklearn wrapper for the `maximum_a_posteriori` method.

Parameters

X [array-like, shape (n_samples, n_dimensions)] The samples to do the prediction on. Each sample is a row and each column corresponds to a dimension in that sample. For univariate distributions, a single array may be passed in.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

y [array-like, shape (n_samples,)] The predicted component which fits the sample the best.

`predict_log_proba ()`

Calculate the posterior log P(MID) for data.

Calculate the log probability of each item having been generated from each component in the model. This returns normalized log probabilities such that the probabilities should sum to 1

This is a sklearn wrapper for the original posterior function.

Parameters

X [array-like, shape (n_samples, n_dimensions)] The samples to do the prediction on. Each sample is a row and each column corresponds to a dimension in that sample. For univariate distributions, a single array may be passed in.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

y [array-like, shape (n_samples, n_components)] The normalized log probability $\log P(\text{MID})$ for each sample. This is the probability that the sample was generated from each component.

`predict_proba()`

Calculate the posterior $P(\text{MID})$ for data.

Calculate the probability of each item having been generated from each component in the model. This returns normalized probabilities such that each row should sum to 1.

Since calculating the log probability is much faster, this is just a wrapper which exponentiates the log probability matrix.

Parameters

X [array-like, shape (n_samples, n_dimensions)] The samples to do the prediction on. Each sample is a row and each column corresponds to a dimension in that sample. For univariate distributions, a single array may be passed in.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

probability [array-like, shape (n_samples, n_components)] The normalized probability $P(\text{MID})$ for each sample. This is the probability that the sample was generated from each component.

`probability()`

Return the probability of the given symbol under this distribution.

Parameters

symbol [object] The symbol to calculate the probability of

Returns

probability [double] The probability of that point under the distribution.

`sample()`

Generate a sample from the model.

First, randomly select a component weighted by the prior probability, Then, use the sample method from that component to generate a sample.

Parameters

n [int, optional] The number of samples to generate. Defaults to 1.

random_state [int, numpy.random.RandomState, or None] The random state used for generating samples. If set to none, a random seed will be used. If set to either an integer or a random seed, will produce deterministic outputs.

Returns

sample [array-like or object] A randomly generated sample from the model of the type modelled by the emissions. An integer if using most distributions, or an array if using multivariate ones, or a string for most discrete distributions. If $n=1$ return an object, if $n>1$ return an array of the samples.

score ()

Return the accuracy of the model on a data set.

Parameters

X [numpy.ndarray, shape=(n, d)] The values of the data set

y [numpy.ndarray, shape=(n,)] The labels of each value

summarize ()

Summarize data into stored sufficient statistics for out-of-core training.

Parameters

X [array-like, shape (n_samples, variable)] Array of the samples, which can be either fixed size or variable depending on the underlying components.

y [array-like, shape (n_samples,)] Array of the known labels as integers

weights [array-like, shape (n_samples,) optional] Array of the weight of each sample, a positive float

Returns

None

thaw ()

Thaw the distribution, re-allowing updates to occur.

to_json ()

Serialize the model to JSON.

Parameters

separators [tuple, optional] The two separators to pass to the `json.dumps` function for formatting. Default is `(' ', ': ')`.

indent [int, optional] The indentation to use at each level. Passed to `json.dumps` for formatting. Default is 4.

Returns

json [str] A properly formatted JSON object.

to_yaml ()

Serialize the model to YAML for compactness.

class `pomegranate.BayesClassifier.BayesClassifier`

A Bayes classifier, a more general form of a naive Bayes classifier.

A Bayes classifier, like a naive Bayes classifier, uses Bayes' rule in order to calculate the posterior probability of the classes, which are used for the predictions. However, a naive Bayes classifier assumes that each of the features are independent of each other and so can be modelled as independent distributions. A generalization of that, the Bayes classifier, allows for an arbitrary covariance between the features. This allows for more complicated components to be used, up to and including even HMMs to form a classifier over sequences, or mixtures to form a classifier with complex emissions.

Parameters

models [list] A list of initialized distribution objects to use as the components in the model.

weights [list or numpy.ndarray or None, default None] The prior probabilities of the components. If None is passed in then defaults to the uniformly distributed priors.

Examples

```
>>> from pomegranate import *
>>>
>>> d1 = NormalDistribution(3, 2)
>>> d2 = NormalDistribution(5, 1.5)
>>>
>>> clf = BayesClassifier([d1, d2])
>>> clf.predict_proba([[6]])
array([[ 0.2331767,  0.7668233]])
>>> X = [[0], [2], [0], [1], [0], [5], [6], [5], [7], [6]]
>>> y = [0, 0, 0, 0, 0, 1, 1, 0, 1, 1]
>>> clf.fit(X, y)
>>> clf.predict_proba([[6]])
array([[ 0.01973451,  0.98026549]])
```

Attributes

models [list] The model objects, either initialized by the user or fit to data.

weights [numpy.ndarray] The prior probability of each component of the model.

clear_summaries()

Remove the stored sufficient statistics.

Parameters

None

Returns

None

copy()

Return a deep copy of this distribution object.

This object will not be tied to any other distribution or connected in any form.

Parameters

None

Returns

distribution [Distribution] A copy of the distribution with the same parameters.

fit()

Fit the Bayes classifier to the data by passing data to its components.

The fit step for a Bayes classifier with purely labeled data is a simple MLE update on the underlying distributions, grouped by the labels. However, in the semi-supervised model is trained on a mixture of both labeled and unlabeled data, where the unlabeled data uses the label -1. In this setting, EM is used to train the model. The model is initialized using the labeled data and then sufficient statistics are gathered for both the labeled and unlabeled data, combined, and used to update the parameters.

Parameters

- X** [numpy.ndarray or list] The dataset to operate on. For most models this is a numpy array with columns corresponding to features and rows corresponding to samples. For markov chains and HMMs this will be a list of variable length sequences.
- y** [numpy.ndarray or list or None] Data labels for supervised training algorithms.
- weights** [array-like or None, shape (n_samples,), optional] The initial weights of each sample in the matrix. If nothing is passed in then each sample is assumed to be the same weight. Default is None.
- inertia** [double, optional] Inertia used for the training the distributions.
- pseudocount** [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Default is 0.
- stop_threshold** [double, optional, positive] The threshold at which EM will terminate for the improvement of the model. If the model does not improve its fit of the data by a log probability of 0.1 then terminate. Only required if doing semisupervised learning. Default is 0.1.
- max_iterations** [int, optional, positive] The maximum number of iterations to run EM for. If this limit is hit then it will terminate training, regardless of how well the model is improving per iteration. Only required if doing semisupervised learning. Default is 1e8.
- callbacks** [list, optional] A list of callback objects that describe functionality that should be undertaken over the course of training. Only used for semi-supervised learning.
- return_history** [bool, optional] Whether to return the history during training as well as the model. Only used for semi-supervised learning.
- verbose** [bool, optional] Whether or not to print out improvement information over iterations. Only required if doing semisupervised learning. Default is False.
- n_jobs** [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

Returns

self [object] Returns the fitted model

freeze ()

Freeze the distribution, preventing updates from occurring.

from_json ()

Deserialize this object from its JSON representation.

from_samples ()

Create a Bayes classifier directly from the given dataset.

This will initialize the distributions using maximum likelihood estimates derived by partitioning the dataset using the label vector. If any labels are missing, the model will be trained using EM in a semi-supervised setting.

A homogeneous model can be defined by passing in a single distribution callable as the first parameter and specifying the number of components, while a heterogeneous model can be defined by passing in a list of callables of the appropriate type.

A Bayes classifier is a superset of the naive Bayes classifier in that the math is identical, but the distributions used do not have to be independent for each feature. Simply put, one can create a multivariate Gaussian Bayes classifier with a full covariance matrix, but a Gaussian naive Bayes would require a diagonal covariance matrix.

Parameters

distributions [array-like, shape (n_components,) or callable]

The components of the model. This should either be a single callable if all components will be the same distribution, or an array of callables, one for each feature.

X [array-like, shape (n_samples, n_dimensions)] This is the data to train on. Each row is a sample, and each column is a dimension to train on.

y [array-like, shape (n_samples,)] The labels for each sample. The labels should be integers between 0 and k-1 for a problem with k classes, or -1 if the label is not known for that sample.

weights [array-like, shape (n_samples,), optional] The initial weights of each sample in the matrix. If nothing is passed in then each sample is assumed to be the same weight. Default is None.

inertia [double, optional] Inertia used for the training the distributions.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Default is 0.

stop_threshold [double, optional, positive] The threshold at which EM will terminate for the improvement of the model. If the model does not improve its fit of the data by a log probability of 0.1 then terminate. Only required if doing semisupervised learning. Default is 0.1.

max_iterations [int, optional, positive] The maximum number of iterations to run EM for. If this limit is hit then it will terminate training, regardless of how well the model is improving per iteration. Only required if doing semisupervised learning. Default is 1e8.

callbacks [list, optional] A list of callback objects that describe functionality that should be undertaken over the course of training.

return_history [bool, optional] Whether to return the history during training as well as the model.

keys [list] A list of sets where each set is the keys present in that column. If there are d columns in the data set then this list should have d sets and each set should have at least two keys in it.

verbose [bool, optional] Whether or not to print out improvement information over iterations. Only required if doing semisupervised learning. Default is False.

n_jobs [int, optional] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

****kwargs** [dict, optional] Any arguments to pass into the *from_samples* methods of other objects that are being created such as BayesianNetworks or HMMs.

Returns

model [BayesClassifier] The fit Bayes classifier model.

from_summaries ()

Fit the model to the collected sufficient statistics.

Fit the parameters of the model to the sufficient statistics gathered during the summarize calls. This should return an exact update.

Parameters

inertia [double, optional] The weight of the previous parameters of the model. The new parameters will roughly be $\text{old_param} * \text{inertia} + \text{new_param} * (1 - \text{inertia})$, so an inertia of 0 means ignore the old parameters, whereas an inertia of 1 means ignore the new parameters. Default is 0.0.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. If discrete data, will smooth both the prior probabilities of each component and the emissions of each component. Otherwise, will only smooth the prior probabilities of each component. Default is 0.

Returns

None

from_yaml ()

Deserialize this object from its YAML representation.

log_probability ()

Calculate the log probability of a point under the distribution.

The probability of a point is the sum of the probabilities of each distribution multiplied by the weights. Thus, the log probability is the sum of the log probability plus the log prior.

This is the python interface.

Parameters

X [numpy.ndarray, shape=(n, d) or (n, m, d)] The samples to calculate the log probability of. Each row is a sample and each column is a dimension. If emissions are HMMs then shape is (n, m, d) where m is variable length for each observation, and X becomes an array of n (m, d)-shaped arrays.

n_jobs [int, optional] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

log_probability [double] The log probability of the point under the distribution.

predict ()

Predict the most likely component which generated each sample.

Calculate the posterior P(MID) for each sample and return the index of the component most likely to fit it. This corresponds to a simple argmax over the responsibility matrix.

This is a sklearn wrapper for the maximum_a_posteriori method.

Parameters

X [array-like, shape (n_samples, n_dimensions)] The samples to do the prediction on. Each sample is a row and each column corresponds to a dimension in that sample. For univariate distributions, a single array may be passed in.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

y [array-like, shape (n_samples,)] The predicted component which fits the sample the best.

`predict_log_proba()`

Calculate the posterior log P(MID) for data.

Calculate the log probability of each item having been generated from each component in the model. This returns normalized log probabilities such that the probabilities should sum to 1

This is a sklearn wrapper for the original posterior function.

Parameters

X [array-like, shape (n_samples, n_dimensions)] The samples to do the prediction on. Each sample is a row and each column corresponds to a dimension in that sample. For univariate distributions, a single array may be passed in.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

y [array-like, shape (n_samples, n_components)] The normalized log probability log P(MID) for each sample. This is the probability that the sample was generated from each component.

`predict_proba()`

Calculate the posterior P(MID) for data.

Calculate the probability of each item having been generated from each component in the model. This returns normalized probabilities such that each row should sum to 1.

Since calculating the log probability is much faster, this is just a wrapper which exponentiates the log probability matrix.

Parameters

X [array-like, shape (n_samples, n_dimensions)] The samples to do the prediction on. Each sample is a row and each column corresponds to a dimension in that sample. For univariate distributions, a single array may be passed in.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

batch_size: int or None, optional The size of the batches to make predictions on. Passing in None means splitting the data set evenly among the number of jobs. Default is None.

Returns

probability [array-like, shape (n_samples, n_components)] The normalized probability P(MID) for each sample. This is the probability that the sample was generated from each component.

probability()

Return the probability of the given symbol under this distribution.

Parameters

symbol [object] The symbol to calculate the probability of

Returns

probability [double] The probability of that point under the distribution.

sample()

Generate a sample from the model.

First, randomly select a component weighted by the prior probability, Then, use the sample method from that component to generate a sample.

Parameters

n [int, optional] The number of samples to generate. Defaults to 1.

random_state [int, numpy.random.RandomState, or None] The random state used for generating samples. If set to none, a random seed will be used. If set to either an integer or a random seed, will produce deterministic outputs.

Returns

sample [array-like or object] A randomly generated sample from the model of the type modelled by the emissions. An integer if using most distributions, or an array if using multivariate ones, or a string for most discrete distributions. If n=1 return an object, if n>1 return an array of the samples.

score()

Return the accuracy of the model on a data set.

Parameters

X [numpy.ndarray, shape=(n, d)] The values of the data set

y [numpy.ndarray, shape=(n,)] The labels of each value

summarize()

Summarize data into stored sufficient statistics for out-of-core training.

Parameters

X [array-like, shape (n_samples, variable)] Array of the samples, which can be either fixed size or variable depending on the underlying components.

y [array-like, shape (n_samples,)] Array of the known labels as integers

weights [array-like, shape (n_samples,) optional] Array of the weight of each sample, a positive float

Returns

None

thaw()

Thaw the distribution, re-allowing updates to occur.

`to_json()`

Serialize the model to JSON.

Parameters

separators [tuple, optional] The two separators to pass to the `json.dumps` function for formatting. Default is `(',', ':')`.

indent [int, optional] The indentation to use at each level. Passed to `json.dumps` for formatting. Default is 4.

Returns

json [str] A properly formatted JSON object.

`to_yaml()`

Serialize the model to YAML for compactness.

2.17 Markov Chains

IPython Notebook Tutorial

Markov chains are form of structured model over sequences. They represent the probability of each character in the sequence as a conditional probability of the last k symbols. For example, a 3rd order Markov chain would have each symbol depend on the last three symbols. A 0th order Markov chain is a naive predictor where each symbol is independent of all other symbols. Currently pomegranate only supports discrete emission Markov chains where each symbol is a discrete symbol versus a continuous number (like 'A' 'B' 'C' instead of 17.32 or 19.65).

2.17.1 Initialization

Markov chains can almost be represented by a single conditional probability table (CPT), except that the probability of the first k elements (for a k -th order Markov chain) cannot be appropriately represented except by using special characters. Due to this pomegranate takes in a series of $k+1$ distributions representing the first k elements. For example for a second order Markov chain:

```
from pomegranate import *
d1 = DiscreteDistribution({'A': 0.25, 'B': 0.75})
d2 = ConditionalProbabilityTable([['A', 'A', 0.1],
                                  ['A', 'B', 0.9],
                                  ['B', 'A', 0.6],
                                  ['B', 'B', 0.4]], [d1])
d3 = ConditionalProbabilityTable([['A', 'A', 'A', 0.4],
                                  ['A', 'A', 'B', 0.6],
                                  ['A', 'B', 'A', 0.8],
                                  ['A', 'B', 'B', 0.2],
                                  ['B', 'A', 'A', 0.9],
                                  ['B', 'A', 'B', 0.1],
                                  ['B', 'B', 'A', 0.2],
                                  ['B', 'B', 'B', 0.8]], [d1, d2])
model = MarkovChain([d1, d2, d3])
```

2.17.2 Probability

The probability of a sequence under the Markov chain is just the probability of the first character under the first distribution times the probability of the second character under the second distribution and so forth until you go past

the (k+1)th character, which remains evaluated under the (k+1)th distribution. We can calculate the probability or log probability in the same manner as any of the other models. Given the model shown before:

```
>>> model.log_probability(['A', 'B', 'B', 'B'])
-3.324236340526027
>>> model.log_probability(['A', 'A', 'A', 'A'])
-5.521460917862246
```

2.17.3 Fitting

Markov chains are not very complicated to train. For each sequence the appropriate symbols are sent to the appropriate distributions and maximum likelihood estimates are used to update the parameters of the distributions. There are no latent factors to train and so no expectation maximization or iterative algorithms are needed to train anything.

2.17.4 API Reference

class pomegranate.MarkovChain.**MarkovChain**

A Markov Chain.

Implemented as a series of conditional distributions, the Markov chain models $P(X_i | X_{i-1} \dots X_{i-k})$ for a k-th order Markov network. The conditional dependencies are directly on the emissions, and not on a hidden state as in a hidden Markov model.

Parameters

distributions [list, shape (k+1)] A list of the conditional distributions which make up the markov chain. Begins with $P(X_i)$, then $P(X_i | X_{i-1})$. For a k-th order markov chain you must put in k+1 distributions.

Examples

```
>>> from pomegranate import *
>>> d1 = DiscreteDistribution({'A': 0.25, 'B': 0.75})
>>> d2 = ConditionalProbabilityTable([['A', 'A', 0.33],
                                     ['B', 'A', 0.67],
                                     ['A', 'B', 0.82],
                                     ['B', 'B', 0.18]], [d1])

>>> mc = MarkovChain([d1, d2])
>>> mc.log_probability(list('ABBAABABABAABABA'))
-8.9119890701808213
```

Attributes

distributions [list, shape (k+1)] The distributions which make up the chain.

fit()

Fit the model to new data using MLE.

The underlying distributions are fed in their appropriate points and weights and are updated.

Parameters

sequences [array-like, shape (n_samples, variable)] This is the data to train on. Each row is a sample which contains a sequence of variable length

weights [array-like, shape (n_samples,), optional] The initial weights of each sample. If nothing is passed in then each sample is assumed to be the same weight. Default is None.

inertia [double, optional] The weight of the previous parameters of the model. The new parameters will roughly be $\text{old_param} * \text{inertia} + \text{new_param} * (1 - \text{inertia})$, so an inertia of 0 means ignore the old parameters, whereas an inertia of 1 means ignore the new parameters. Default is 0.0.

Returns

None

`from_json()`

Read in a serialized model and return the appropriate classifier.

Parameters

s [str] A JSON formatted string containing the file.

Returns

model [object] A properly initialized and baked model.

`from_samples()`

Learn the Markov chain from data.

Takes in the memory of the chain (k) and learns the initial distribution and probability tables associated with the proper parameters.

Parameters

X [array-like, list or numpy.array] The data to fit the structure too as a list of sequences of variable length. Since the data will be of variable length, there is no set form

weights [array-like, shape (n_nodes), optional] The weight of each sample as a positive double. Default is None.

k [int, optional] The number of samples back to condition on in the model. Default is 1.

Returns

model [MarkovChain] The learned markov chain model.

`from_summaries()`

Fit the model to the collected sufficient statistics.

Fit the parameters of the model to the sufficient statistics gathered during the summarize calls. This should return an exact update.

Parameters

inertia [double, optional] The weight of the previous parameters of the model. The new parameters will roughly be $\text{old_param} * \text{inertia} + \text{new_param} * (1 - \text{inertia})$, so an inertia of 0 means ignore the old parameters, whereas an inertia of 1 means ignore the new parameters. Default is 0.0.

Returns

None

`log_probability()`

Calculate the log probability of the sequence under the model.

This calculates the first slices of increasing size under the corresponding first few components of the model until size k is reached, at which all slices are evaluated under the final component.

Parameters

sequence [array-like] An array of observations

Returns

logp [double] The log probability of the sequence under the model.

`sample()`

Create a random sample from the model.

Parameters

length [int or Distribution] Give either the length of the sample you want to generate, or a distribution object which will be randomly sampled for the length. Continuous distributions will have their sample rounded to the nearest integer, minimum 1.

Returns

sequence [array-like, shape = (length,)] A sequence randomly generated from the markov chain.

`summarize()`

Summarize a batch of data and store sufficient statistics.

This will summarize the sequences into sufficient statistics stored in each distribution.

Parameters

sequences [array-like, shape (n_samples, variable)] This is the data to train on. Each row is a sample which contains a sequence of variable length

weights [array-like, shape (n_samples,), optional] The initial weights of each sample. If nothing is passed in then each sample is assumed to be the same weight. Default is None.

Returns

None

`to_json()`

Serialize the model to a JSON.

Parameters

separators [tuple, optional] The two separators to pass to the `json.dumps` function for formatting. Default is `(',', ':')`.

indent [int, optional] The indentation to use at each level. Passed to `json.dumps` for formatting. Default is 4.

Returns

json [str] A properly formatted JSON object.

2.18 Bayesian Networks

- [IPython Notebook Tutorial](#)
- [IPython Notebook Structure Learning Tutorial](#)

Bayesian networks are a probabilistic model that are especially good at inference given incomplete data. Much like a hidden Markov model, they consist of a directed graphical model (though Bayesian networks must also be acyclic) and a set of probability distributions. The edges encode dependency statements between the variables, where the

lack of an edge between any pair of variables indicates a conditional independence. Each node encodes a probability distribution, where root nodes encode univariate probability distributions and inner/leaf nodes encode conditional probability distributions. Bayesian networks are exceptionally flexible when doing inference, as any subset of variables can be observed, and inference done over all other variables, without needing to define these groups in advance. In fact, the set of observed variables can change from one sample to the next without needing to modify the underlying algorithm at all.

Currently, pomegranate only supports discrete Bayesian networks, meaning that the values must be categories, i.e. ‘apples’ and ‘oranges’, or 1 and 2, where 1 and 2 refer to categories, not numbers, and so 2 is not explicitly ‘bigger’ than 1.

2.18.1 Initialization

Bayesian networks can be initialized in two ways, depending on whether the underlying graphical structure is known or not: (1) the graphical structure can be built one node at a time with pre-initialized distributions set for each node, or (2) both the graphical structure and distributions can be learned directly from data. This mirrors the other models that are implemented in pomegranate. However, typically expectation maximization is used to fit the parameters of the distribution, and so initialization (such as through k-means) is typically fast whereas fitting is slow. For Bayesian networks, the opposite is the case. Fitting can be done quickly by just summing counts through the data, while initialization is hard as it requires an exponential time search through all possible DAGs to identify the optimal graph. More is discussed in the tutorials above and in the fitting section below.

Let’s take a look at initializing a Bayesian network in the first manner by quickly implementing the [Monty Hall problem](#). The Monty Hall problem arose from the gameshow *Let’s Make a Deal*, where a guest had to choose which one of three doors had a prize behind it. The twist was that after the guest chose, the host, originally Monty Hall, would then open one of the doors the guest did not pick and ask if the guest wanted to switch which door they had picked. Initial inspection may lead you to believe that if there are only two doors left, there is a 50-50 chance of you picking the right one, and so there is no advantage one way or the other. However, it has been proven both through simulations and analytically that there is in fact a 66% chance of getting the prize if the guest switches their door, regardless of the door they initially went with.

Our network will have three nodes, one for the guest, one for the prize, and one for the door Monty chooses to open. The door the guest initially chooses and the door the prize is behind are uniform random processes across the three doors, but the door which Monty opens is dependent on both the door the guest chooses (it cannot be the door the guest chooses), and the door the prize is behind (it cannot be the door with the prize behind it).

```
from pomegranate import *

guest = DiscreteDistribution({'A': 1./3, 'B': 1./3, 'C': 1./3})
prize = DiscreteDistribution({'A': 1./3, 'B': 1./3, 'C': 1./3})
monty = ConditionalProbabilityTable(
    [['A', 'A', 'A', 0.0],
     ['A', 'A', 'B', 0.5],
     ['A', 'A', 'C', 0.5],
     ['A', 'B', 'A', 0.0],
     ['A', 'B', 'B', 0.0],
     ['A', 'B', 'C', 1.0],
     ['A', 'C', 'A', 0.0],
     ['A', 'C', 'B', 1.0],
     ['A', 'C', 'C', 0.0],
     ['B', 'A', 'A', 0.0],
     ['B', 'A', 'B', 0.0],
     ['B', 'A', 'C', 1.0],
     ['B', 'B', 'A', 0.5],
     ['B', 'B', 'B', 0.0],
     ['B', 'B', 'C', 0.5],
```

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```

        ['B', 'C', 'A', 1.0],
        ['B', 'C', 'B', 0.0],
        ['B', 'C', 'C', 0.0],
        ['C', 'A', 'A', 0.0],
        ['C', 'A', 'B', 1.0],
        ['C', 'A', 'C', 0.0],
        ['C', 'B', 'A', 1.0],
        ['C', 'B', 'B', 0.0],
        ['C', 'B', 'C', 0.0],
        ['C', 'C', 'A', 0.5],
        ['C', 'C', 'B', 0.5],
        ['C', 'C', 'C', 0.0]], [guest, prize])

s1 = Node(guest, name="guest")
s2 = Node(prize, name="prize")
s3 = Node(monty, name="monty")

model = BayesianNetwork("Monty Hall Problem")
model.add_states(s1, s2, s3)
model.add_edge(s1, s3)
model.add_edge(s2, s3)
model.bake()

```

Note: The objects ‘state’ and ‘node’ are really the same thing and can be used interchangeably. The only difference is the name, as hidden Markov models use ‘state’ in the literature frequently whereas Bayesian networks use ‘node’ frequently.

The conditional distribution must be explicitly spelled out in this example, followed by a list of the parents in the same order as the columns take in the table that is provided (e.g. the columns in the table correspond to guest, prize, monty, probability.)

However, one can also initialize a Bayesian network based completely on data. As mentioned before, the exact version of this algorithm takes exponential time with the number of variables and typically can’t be done on more than ~25 variables. This is because there are a super-exponential number of directed acyclic graphs that one could define over a set of variables, but fortunately one can use dynamic programming in order to reduce this complexity down to “simply exponential.” The implementation of the exact algorithm actually goes further than the original dynamic programming algorithm by implementing an A* search to somewhat reduce computational time but drastically reduce required memory, sometimes by an order of magnitude.

```

from pomegranate import *
import numpy

X = numpy.load('data.npy')
model = BayesianNetwork.from_samples(X, algorithm='exact')

```

The exact algorithm is not the default, though. The default is a novel greedy algorithm that greedily chooses a topological ordering of the variables, but optimally identifies the best parents for each variable given this ordering. It is significantly faster and more memory efficient than the exact algorithm and produces far better estimates than using a Chow-Liu tree. This is set to the default to avoid locking up the computers of users that unintentionally tell their computers to do a near-impossible task.

2.18.2 Probability

You can calculate the probability of a sample under a Bayesian network as the product of the probability of each variable given its parents, if it has any. This can be expressed as $P = \prod_{i=1}^d P(D_i|Pa_i)$ for a sample with d dimensions. For example, in the Monty Hal problem, the probability of a show is the probability of the guest choosing the respective door, times the probability of the prize being behind a given door, times the probability of Monty opening a given door given the previous two values. For example, using the manually initialized network above:

```
>>> print(model.probability([[ 'A', 'A', 'A'],
                             [ 'A', 'A', 'B'],
                             [ 'C', 'C', 'B']]))
[ 0.          0.05555556  0.05555556]
```

2.18.3 Prediction

Bayesian networks are frequently used to infer/impute the value of missing variables given the observed values. In other models, typically there is either a single or fixed set of missing variables, such as latent factors, that need to be imputed, and so returning a fixed vector or matrix as the predictions makes sense. However, in the case of Bayesian networks, we can make no such assumptions, and so when data is passed in for prediction it should be in the format as a matrix with `None` in the missing variables that need to be inferred. The return is thus a filled in matrix where the Nones have been replaced with the imputed values. For example:

```
>>> print(model.predict([[ 'A', 'B', None],
                        [ 'A', 'C', None],
                        [ 'C', 'B', None]]))
[ 'A' 'B' 'C' ]
[ 'A' 'C' 'B' ]
[ 'C' 'B' 'A' ]
```

In this example, the final column is the one that is always missing, but a more complex example is as follows:

```
>>> print(model.predict([[ 'A', 'B', None],
                        [ 'A', None, 'C'],
                        [None, 'B', 'A']]))
[ 'A' 'B' 'C' ]
[ 'A' 'B' 'C' ]
[ 'C' 'B' 'A' ]
```

2.18.4 Fitting

Fitting a Bayesian network to data is a fairly simple process. Essentially, for each variable, you need consider only that column of data and the columns corresponding to that variables parents. If it is a univariate distribution, then the maximum likelihood estimate is just the count of each symbol divided by the number of samples in the data. If it is a multivariate distribution, it ends up being the probability of each symbol in the variable of interest given the combination of symbols in the parents. For example, consider a binary dataset with two variables, X and Y, where X is a parent of Y. First, we would go through the dataset and calculate $P(X=0)$ and $P(X=1)$. Then, we would calculate $P(Y=0|X=0)$, $P(Y=1|X=0)$, $P(Y=0|X=1)$, and $P(Y=1|X=1)$. Those values encode all of the parameters of the Bayesian network.

2.18.5 API Reference

class `pomegranate.BayesianNetwork.BayesianNetwork`

A Bayesian Network Model.

A Bayesian network is a directed graph where nodes represent variables, edges represent conditional dependencies of the children on their parents, and the lack of an edge represents a conditional independence.

Parameters

name [str, optional] The name of the model. Default is None

Attributes

states [list, shape (n_states,)] A list of all the state objects in the model

graph [networkx.DiGraph] The underlying graph object.

add_edge ()

Add a transition from state a to state b which indicates that B is dependent on A in ways specified by the distribution.

add_node ()

Add a node to the graph.

add_nodes ()

Add multiple states to the graph.

add_state ()

Another name for a node.

add_states ()

Another name for a node.

add_transition ()

Transitions and edges are the same.

bake ()

Finalize the topology of the model.

Assign a numerical index to every state and create the underlying arrays corresponding to the states and edges between the states. This method must be called before any of the probability-calculating methods. This includes converting conditional probability tables into joint probability tables and creating a list of both marginal and table nodes.

Parameters

None

Returns

None

clear_summaries ()

Clear the summary statistics stored in the object.

copy ()

Return a deep copy of this distribution object.

This object will not be tied to any other distribution or connected in any form.

Parameters

None

Returns

distribution [Distribution] A copy of the distribution with the same parameters.

dense_transition_matrix ()

Returns the dense transition matrix. Useful if the transitions of somewhat small models need to be analyzed.

edge_count ()

Returns the number of edges present in the model.

fit ()

Fit the model to data using MLE estimates.

Fit the model to the data by updating each of the components of the model, which are univariate or multivariate distributions. This uses a simple MLE estimate to update the distributions according to their summarize or fit methods.

This is a wrapper for the summarize and from_summaries methods.

Parameters

X [array-like or generator, shape (n_samples, n_nodes)] The data to train on, where each row is a sample and each column corresponds to the associated variable.

weights [array-like, shape (n_nodes), optional] The weight of each sample as a positive double. Default is None.

inertia [double, optional] The inertia for updating the distributions, passed along to the distribution method. Default is 0.0.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Only effects hidden Markov models defined over discrete distributions. Default is 0.

verbose [bool, optional] Whether or not to print out improvement information over iterations. Only required if doing semisupervised learning. Default is False.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

Returns

self [BayesianNetwork] The fit Bayesian network object with updated model parameters.

freeze ()

Freeze the distribution, preventing updates from occurring.

from_json ()

Read in a serialized Bayesian Network and return the appropriate object.

Parameters

s [str] A JSON formatted string containing the file.

Returns

model [object] A properly initialized and baked model.

from_samples ()

Learn the structure of the network from data.

There are currently two types of approaches implemented. The first, the Chow-Liu algorithm, finds a tree-like structure from symmetric mutual-information scores given a root node (the *root* parameter). The second type searches through structures and returns the structure that maximizes the following objective function:

$$P(\text{DIM}) + \text{penalty} * |\mathbf{M}|$$

where $P(\text{DIM})$ is the probability of the data given the found model, penalty is a user-specified parameters, and $|\mathbf{M}|$ is the number of parameters in the model. When this penalty is $\log_2(|\mathbf{D}|) / 2$ (the default) where $|\mathbf{D}|$ is the weight sum of the examples, this is equivalent to the minimum description length (MDL).

There are currently three ways that the learned structure can be controlled. The first is to increase the penalty term to increase sparsity. The second is to pass in a specified list of edges that must exist (*include_edges*) or cannot exist (*exclude_edges*). Lastly, a constraint graph can be specified where each node in the graph is a set of variables being modeled and the edges in the graph indicate which sets of variables can be parents to which other sets of variables (and where a self-loop is the normal structure learning step).

Parameters

X [array-like or generator, shape (n_samples, n_nodes)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

weights [array-like, shape (n_nodes), optional] The weight of each sample as a positive double. Default is None.

algorithm [str, one of 'chow-liu', 'greedy', 'exact', 'exact-dp' optional] The algorithm to use for learning the Bayesian network. Default is 'greedy' that greedily attempts to find the best structure, and frequently can identify the optimal structure. 'exact' uses DP/A* to find the optimal Bayesian network, and 'exact-dp' tries to find the shortest path on the entire order lattice, which is more memory and computationally expensive. 'exact' and 'exact-dp' should give identical results, with 'exact-dp' remaining an option mostly for debugging reasons. 'chow-liu' will return the optimal tree-like structure for the Bayesian network, which is a very fast approximation but not always the best network.

max_parents [int, optional] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.

penalty [float or None, optional] The weighting of the model complexity term in the objective function. Increasing this value will encourage sparsity whereas setting the value to 0 will result in an unregularized structure. Default is $\log_2(|\mathbf{D}|) / 2$ where $|\mathbf{D}|$ is the sum of the weights of the data.

root [int, optional] For algorithms which require a single root ('chow-liu'), this is the root for which all edges point away from. User may specify which column to use as the root. Default is the first column.

constraint_graph [networkx.DiGraph or None, optional] A directed graph showing valid parent sets for each variable. Each node is a set of variables, and edges represent which variables can be valid parents of those variables. The naive structure learning task is just all variables in a single node with a self edge, meaning that you know nothing about

include_edges [list or None, optional] A list of (parent, child) tuples that are edges which must be present in the found structure.

exclude_edges [list or None, optional] A list of (parent, child) tuples that are edges which cannot be present in the found structure.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Default is 0.

state_names [array-like, shape (n_nodes), optional] A list of meaningful names to be applied to nodes

name [str, optional] The name of the model. Default is None.

reduce_dataset [bool, optional] Given the discrete nature of these datasets, frequently a user will pass in a dataset that has many identical samples. It is time consuming to go through these redundant samples and a far more efficient use of time to simply calculate a new dataset comprised of the subset of unique observed samples weighted by the number of times they occur in the dataset. This typically will speed up all algorithms, including when using a constraint graph. Default is True.

keys [list] A list of sets where each set is the keys present in that column. If there are d columns in the data set then this list should have d sets and each set should have at least two keys in it.

n_jobs [int, optional] The number of threads to use when learning the structure of the network. If a constraint graph is provided, this will parallelize the tasks as directed by the constraint graph. If one is not provided it will parallelize the building of the parent graphs. Both cases will provide large speed gains.

Returns

model [BayesianNetwork] The learned BayesianNetwork.

from_structure()

Return a Bayesian network from a predefined structure.

Pass in the structure of the network as a tuple of tuples and get a fit network in return. The tuple should contain n tuples, with one for each node in the graph. Each inner tuple should be of the parents for that node. For example, a three node graph where both node 0 and 1 have node 2 as a parent would be specified as ((2,), (2,), ()).

Parameters

X [array-like, shape (n_samples, n_nodes)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

structure [tuple of tuples] The parents for each node in the graph. If a node has no parents, then do not specify any parents.

weights [array-like, shape (n_nodes), optional] The weight of each sample as a positive double. Default is None.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Default is 0.

name [str, optional] The name of the model. Default is None.

state_names [array-like, shape (n_nodes), optional] A list of meaningful names to be applied to nodes

keys [list] A list of sets where each set is the keys present in that column. If there are d columns in the data set then this list should have d sets and each set should have at least two keys in it.

Returns

model [BayesianNetwork] A Bayesian network with the specified structure.

from_summaries()

Use MLE on the stored sufficient statistics to train the model.

This uses MLE estimates on the stored sufficient statistics to train the model.

Parameters

inertia [double, optional] The inertia for updating the distributions, passed along to the distribution method. Default is 0.0.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Default is 0.

Returns

None

from_yaml()

Deserialize this object from its YAML representation.

log_probability()

Return the log probability of samples under the Bayesian network.

The log probability is just the sum of the log probabilities under each of the components. The log probability of a sample under the graph $A \rightarrow B$ is just $P(A) \cdot P(B|A)$. This will return a vector of log probabilities, one for each sample.

Parameters

X [array-like, shape (n_samples, n_dim)] The sample is a vector of points where each dimension represents the same variable as added to the graph originally. It doesn't matter what the connections between these variables are, just that they are all ordered the same.

check_input [bool, optional] Check to make sure that the observed symbol is a valid symbol for that distribution to produce. Default is True.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

Returns

logp [numpy.ndarray or double] The log probability of the samples if many, or the single log probability.

marginal()

Return the marginal probabilities of each variable in the graph.

This is equivalent to a pass of belief propagation on a graph where no data has been given. This will calculate the probability of each variable being in each possible emission when nothing is known.

Parameters

None

Returns

marginals [array-like, shape (n_nodes)] An array of univariate distribution objects showing the marginal probabilities of that variable.

node_count()

Returns the number of nodes/states in the model

plot()

Draw this model's graph using pygraphviz.

Returns

None

`predict()`

Predict missing values of a data matrix using MLE.

Impute the missing values of a data matrix using the maximally likely predictions according to the forward-backward algorithm. Run each sample through the algorithm (`predict_proba`) and replace missing values with the maximally likely predicted emission.

Parameters

X [array-like, shape (n_samples, n_nodes)] Data matrix to impute. Missing values must be either None (if lists) or `np.nan` (if `numpy.ndarray`). Will fill in these values with the maximally likely ones.

max_iterations [int, optional] Number of iterations to run loopy belief propagation for. Default is 100.

check_input [bool, optional] Check to make sure that the observed symbol is a valid symbol for that distribution to produce. Default is True.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

Returns

y_hat [`numpy.ndarray`, shape (n_samples, n_nodes)] This is the data matrix with the missing values imputed.

`predict_proba()`

Returns the probabilities of each variable in the graph given evidence.

This calculates the marginal probability distributions for each state given the evidence provided through loopy belief propagation. Loopy belief propagation is an approximate algorithm which is exact for certain graph structures.

Parameters

X [dict or array-like, shape \leq n_nodes] The evidence supplied to the graph. This can either be a dictionary with keys being state names and values being the observed values (either the emissions or a distribution over the emissions) or an array with the values being ordered according to the nodes incorporation in the graph (the order fed into `.add_states/add_nodes`) and None for variables which are unknown. It can also be vectorized, so a list of dictionaries can be passed in where each dictionary is a single sample, or a list of lists where each list is a single sample, both formatted as mentioned before.

max_iterations [int, optional] The number of iterations with which to do loopy belief propagation. Usually requires only 1. Default is 100.

check_input [bool, optional] Check to make sure that the observed symbol is a valid symbol for that distribution to produce. Default is True.

n_jobs [int, optional] The number of threads to use when parallelizing the job. This parameter is passed directly into `joblib`. Default is 1, indicating no parallelism.

Returns

y_hat [array-like, shape (n_samples, n_nodes)] An array of univariate distribution objects showing the probabilities of each variable.

`probability()`

Return the probability of the given symbol under this distribution.

Parameters

symbol [object] The symbol to calculate the probability of

Returns

probability [double] The probability of that point under the distribution.

sample ()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

score ()

Return the accuracy of the model on a data set.

Parameters

X [numpy.ndarray, shape=(n, d)] The values of the data set

y [numpy.ndarray, shape=(n,)] The labels of each value

state_count ()

Returns the number of states present in the model.

summarize ()

Summarize a batch of data and store the sufficient statistics.

This will partition the dataset into columns which belong to their appropriate distribution. If the distribution has parents, then multiple columns are sent to the distribution. This relies mostly on the summarize function of the underlying distribution.

Parameters

X [array-like, shape (n_samples, n_nodes)] The data to train on, where each row is a sample and each column corresponds to the associated variable.

weights [array-like, shape (n_nodes), optional] The weight of each sample as a positive double. Default is None.

Returns

None

thaw ()

Thaw the distribution, re-allowing updates to occur.

to_json ()

Serialize the model to a JSON.

Parameters

separators [tuple, optional] The two separators to pass to the json.dumps function for formatting.

indent [int, optional] The indentation to use at each level. Passed to json.dumps for formatting.

Returns

json [str] A properly formatted JSON object.

to_yaml ()

Serialize the model to YAML for compactness.

class pomegranate.BayesianNetwork.**ParentGraph**

Generate a parent graph for a single variable over its parents.

This will generate the parent graph for a single parents given the data. A parent graph is the dynamically generated best parent set and respective score for each combination of parent variables. For example, if we are generating a parent graph for x_1 over x_2 , x_3 , and x_4 , we may calculate that having x_2 as a parent is better than x_2, x_3 and so store the value of x_2 in the node for x_2, x_3 .

Parameters

X [numpy.ndarray, shape=(n, d)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

weights [numpy.ndarray, shape=(n,)] The weight of each sample as a positive double. Default is None.

key_count [numpy.ndarray, shape=(d,)] The number of unique keys in each column.

include_parents [tuple] A set of parents that this node must have.

exclude_parents [tuple] A set of parents that this node cannot have.

pseudocount [double] A pseudocount to add to each possibility.

penalty [float or None, optional] The weighting of the model complexity term in the objective function. Increasing this value will encourage sparsity whereas setting the value to 0 will result in an unregularized structure. Default is $\log_2(\mathbf{ID}) / 2$ where \mathbf{ID} is the sum of the weights of the data.

max_parents [int] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.

parent_set [tuple, default ()] The variables which are possible parents for this variable. If nothing is passed in then it defaults to all other variables, as one would expect in the naive case. This allows for cases where we want to build a parent graph over only a subset of the variables.

Returns

structure [tuple, shape=(d,)] The parents for each variable in this SCC

pomegranate.BayesianNetwork.**discrete_exact_a_star** ()

Find the optimal graph over a set of variables with no other knowledge.

This is the naive dynamic programming structure learning task where the optimal graph is identified from a set of variables using an order graph and parent graphs. This can be used either when no constraint graph is provided or for a SCC which is made up of a node containing a self-loop. It uses DP/A* in order to find the optimal graph without considering all possible topological sorts. A greedy version of the algorithm can be used that massively reduces both the computational and memory cost while frequently producing the optimal graph.

Parameters

X [numpy.ndarray, shape=(n, d)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

weights [numpy.ndarray, shape=(n,)] The weight of each sample as a positive double. Default is None.

- key_count** [numpy.ndarray, shape=(d,)] The number of unique keys in each column.
- include_edges** [list or None] A list of (parent, child) tuples where each tuple corresponds to an edge that must exist in the found structure.
- exclude_edges** [list or None] A list of (parent, child) tuples where each tuple corresponds to an edge that cannot exist in the found structure.
- pseudocount** [double] A pseudocount to add to each possibility.
- penalty** [float or None, optional] The weighting of the model complexity term in the objective function. Increasing this value will encourage sparsity whereas setting the value to 0 will result in an unregularized structure. Default is $\log_2(\mathbf{ID}) / 2$ where **ID** is the sum of the weights of the data.
- max_parents** [int] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.
- n_jobs** [int] The number of threads to use when learning the structure of the network. This parallelizes the creation of the parent graphs.

Returns

- structure** [tuple, shape=(d,)] The parents for each variable in this SCC

`pomegranate.BayesianNetwork.discrete_exact_component()`

Find the optimal graph over a multi-node component of the constant graph.

The general algorithm in this case is to begin with each variable and add all possible single children for that entry recursively until completion. This will result in a far sparser order graph than before. In addition, one can eliminate entries from the parent graphs that contain invalid parents as they are a fast of computational time.

Parameters

- X** [numpy.ndarray, shape=(n, d)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.
- weights** [numpy.ndarray, shape=(n,)] The weight of each sample as a positive double. Default is None.
- include_edges** [list or None] A list of (parent, child) tuples where each tuple corresponds to an edge that must exist in the found structure.
- exclude_edges** [list or None] A list of (parent, child) tuples where each tuple corresponds to an edge that cannot exist in the found structure.
- key_count** [numpy.ndarray, shape=(d,)] The number of unique keys in each column.
- pseudocount** [double] A pseudocount to add to each possibility.
- penalty** [float or None, optional] The weighting of the model complexity term in the objective function. Increasing this value will encourage sparsity whereas setting the value to 0 will result in an unregularized structure. Default is $\log_2(\mathbf{ID}) / 2$ where **ID** is the sum of the weights of the data.
- max_parents** [int] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.
- n_jobs** [int] The number of threads to use when learning the structure of the network. This parallelizes the creation of the parent graphs.

Returns

structure [tuple, shape=(d,)] The parents for each variable in this SCC

`pomegranate.BayesianNetwork.discrete_exact_dp()`

Find the optimal graph over a set of variables with no other knowledge.

This is the naive dynamic programming structure learning task where the optimal graph is identified from a set of variables using an order graph and parent graphs. This can be used either when no constraint graph is provided or for a SCC which is made up of a node containing a self-loop. This is a reference implementation that uses the naive shortest path algorithm over the entire order graph. The ‘exact’ option uses the A* path in order to avoid considering the full order graph.

Parameters

X [numpy.ndarray, shape=(n, d)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

weights [numpy.ndarray, shape=(n,)] The weight of each sample as a positive double. Default is None.

key_count [numpy.ndarray, shape=(d,)] The number of unique keys in each column.

include_edges [list or None] A set of (parent, child) tuples where each tuple is an edge that must exist in the found structure.

exclude_edges [list or None] A set of (parent, child) tuples where each tuple is an edge that cannot exist in the found structure.

penalty [float or None, optional] The weighting of the model complexity term in the objective function. Increasing this value will encourage sparsity whereas setting the value to 0 will result in an unregularized structure. Default is $\log_2(\mathbf{ID}) / 2$ where **ID** is the sum of the weights of the data.

max_parents [int] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.

n_jobs [int] The number of threads to use when learning the structure of the network. This parallelizes the creation of the parent graphs.

Returns

structure [tuple, shape=(d,)] The parents for each variable in this SCC

`pomegranate.BayesianNetwork.discrete_exact_slap()`

Find the optimal graph in a node with a Self Loop And Parents (SLAP).

Instead of just performing exact BNSL over the set of all parents and removing the offending edges there are efficiencies that can be gained by considering the structure. In particular, parents not coming from the main node do not need to be considered in the order graph but simply added to each entry after creation of the order graph. This is because those variables occur earlier in the topological ordering but it doesn’t matter how they occur otherwise. Parent graphs must be defined over all variables however.

Parameters

X [numpy.ndarray, shape=(n, d)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

weights [numpy.ndarray, shape=(n,)] The weight of each sample as a positive double. Default is None.

key_count [numpy.ndarray, shape=(d,)] The number of unique keys in each column.

include_edges [list or None] A list of (parent, child) tuples where each tuple corresponds to an edge that must exist in the found structure.

exclude_edges [list or None] A list of (parent, child) tuples where each tuple corresponds to an edge that cannot exist in the found structure.

pseudocount [double] A pseudocount to add to each possibility.

penalty [float or None, optional] The weighting of the model complexity term in the objective function. Increasing this value will encourage sparsity whereas setting the value to 0 will result in an unregularized structure. Default is $\log_2(\mathbf{ID}) / 2$ where **ID** is the sum of the weights of the data.

max_parents [int] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.

n_jobs [int] The number of threads to use when learning the structure of the network. This parallelizes the creation of the parent graphs.

Returns

structure [tuple, shape=(d,)] The parents for each variable in this SCC

`pomegranate.BayesianNetwork.discrete_exact_with_constraints()`

This returns the optimal Bayesian network given a set of constraints.

This function controls the process of learning the Bayesian network by taking in a constraint graph, identifying the strongly connected components (SCCs) and solving each one using the appropriate algorithm. This is mostly an internal function.

Parameters

X [numpy.ndarray, shape=(n, d)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

weights [numpy.ndarray, shape=(n,)] The weight of each sample as a positive double. Default is None.

key_count [numpy.ndarray, shape=(d,)] The number of unique keys in each column.

include_edges [list or None] A set of (parent, child) tuples where each tuple is an edge that must exist in the found structure.

exclude_edges [list or None] A set of (parent, child) tuples where each tuple is an edge that cannot exist in the found structure.

pseudocount [double] A pseudocount to add to each possibility.

penalty [float or None, optional] The weighting of the model complexity term in the objective function. Increasing this value will encourage sparsity whereas setting the value to 0 will result in an unregularized structure. Default is $\log_2(\mathbf{ID}) / 2$ where **ID** is the sum of the weights of the data.

max_parents [int] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.

constraint_graph [networkx.DiGraph] A directed graph showing valid parent sets for each variable. Each node is a set of variables, and edges represent which variables can be valid parents of those variables. The naive structure learning task is just all variables in a single node with a self edge, meaning that you know nothing about

n_jobs [int] The number of threads to use when learning the structure of the network. This parallelized both the creation of the parent graphs for each variable and the solving of the SCCs. -1 means use all available resources. Default is 1, meaning no parallelism.

Returns

structure [tuple, shape=(d,)] The parents for each variable in the network.

`pomegranate.BayesianNetwork.discrete_exact_with_constraints_task()`

This is a wrapper for the function to be parallelized by joblib.

This function takes in a single task as an id and a set of parents and children and calls the appropriate function. This is mostly a wrapper for joblib to parallelize.

Parameters

X [numpy.ndarray, shape=(n, d)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

weights [numpy.ndarray, shape=(n,)] The weight of each sample as a positive double. Default is None.

key_count [numpy.ndarray, shape=(d,)] The number of unique keys in each column.

include_edges [list or None] A set of (parent, child) tuples where each tuple is an edge that must exist in the found structure.

exclude_edges [list or None] A set of (parent, child) tuples where each tuple is an edge that cannot exist in the found structure.

pseudocount [double] A pseudocount to add to each possibility.

penalty [float or None, optional] The weighting of the model complexity term in the objective function. Increasing this value will encourage sparsity whereas setting the value to 0 will result in an unregularized structure. Default is $\log_2(\mathbf{ID}) / 2$ where **ID** is the sum of the weights of the data.

max_parents [int] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.

task [tuple] A 3-tuple containing the id, the set of parents and the set of children to learn a component of the Bayesian network over. The cases represent a SCC of the following:

0 - Self loop and no parents 1 - Self loop and parents 2 - Parents and no self loop
3 - Multiple nodes

n_jobs [int] The number of threads to use when learning the structure of the network. This parallelizes the creation of the parent graphs for each task or the finding of best parents in case 2.

Returns

structure [tuple, shape=(d,)] The parents for each variable in this SCC

`pomegranate.BayesianNetwork.discrete_greedy()`

Find the optimal graph over a set of variables with no other knowledge.

Parameters

X [numpy.ndarray, shape=(n, d)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

weights [numpy.ndarray, shape=(n,)] The weight of each sample as a positive double. Default is None.

key_count [numpy.ndarray, shape=(d,)] The number of unique keys in each column.

include_edges [list or None] A list of (parent, child) tuples where each tuple corresponds to an edge that must exist in the found structure.

exclude_edges [list or None] A list of (parent, child) tuples where each tuple corresponds to an edge that cannot exist in the found structure.

pseudocount [double] A pseudocount to add to each possibility.

penalty [float or None, optional] The weighting of the model complexity term in the objective function. Increasing this value will encourage sparsity whereas setting the value to 0 will result in an unregularized structure. Default is $\log_2(\mathbf{DI}) / 2$ where **DI** is the sum of the weights of the data.

max_parents [int] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.

n_jobs [int] The number of threads to use when learning the structure of the network. This parallelizes the creation of the parent graphs.

Returns

structure [tuple, shape=(d,)] The parents for each variable in this SCC

`pomegranate.BayesianNetwork.generate_parent_graph()`
 Generate a parent graph for a single variable over its parents.

This will generate the parent graph for a single parents given the data. A parent graph is the dynamically generated best parent set and respective score for each combination of parent variables. For example, if we are generating a parent graph for x_1 over x_2 , x_3 , and x_4 , we may calculate that having x_2 as a parent is better than x_2, x_3 and so store the value of x_2 in the node for x_2, x_3 .

Parameters

X [numpy.ndarray, shape=(n, d)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

weights [numpy.ndarray, shape=(n,)] The weight of each sample as a positive double. Default is None.

key_count [numpy.ndarray, shape=(d,)] The number of unique keys in each column.

i [int] The column index to build the parent graph for.

include_edges [list or None] A list of (parent, child) tuples where each tuple corresponds to an edge that must exist in the found structure.

exclude_edges [list or None] A list of (parent, child) tuples where each tuple corresponds to an edge that cannot exist in the found structure.

pseudocount [double] A pseudocount to add to each possibility.

penalty [float or None, optional] The weighting of the model complexity term in the objective function. Increasing this value will encourage sparsity whereas setting the value to 0 will result in an unregularized structure. Default is $\log_2(\mathbf{DI}) / 2$ where **DI** is the sum of the weights of the data.

max_parents [int] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.

parent_set [tuple, default ()] The variables which are possible parents for this variable. If nothing is passed in then it defaults to all other variables, as one would expect in the

naive case. This allows for cases where we want to build a parent graph over only a subset of the variables.

Returns

structure [tuple, shape=(d,)] The parents for each variable in this SCC

2.19 Markov Networks

- [IPython Notebook Tutorial](#)

Markov networks (sometimes called Markov random fields) are probabilistic models that are typically represented using an undirected graph. Each of the nodes in the graph represents a variable in the data and each of the edges represent an associate. Unlike Bayesian networks which have directed edges and clear directions of causality, Markov networks have undirected edges and only encode associations.

Currently, pomegranate only supports discrete Markov networks, meaning that the values must be categories, i.e. ‘apples’ and ‘oranges’, or 1 and 2, where 1 and 2 refer to categories, not numbers, and so 2 is not explicitly ‘bigger’ than 1.

2.19.1 Initialization

Markov networks can be initialized in two ways, depending on whether the underlying graphical structure is known or not: (1) a list of the joint probabilities tables can be passed into the initialization, with one table per clique in the graph, or (2) both the graphical structure and distributions can be learned directly from data. This mirrors the other models that are implemented in pomegranate. However, because finding the optimal Markov network requires enumerating a number of potential graphs that is exponential with the number of dimensions in the data, it can be fairly time intensive to find the exact network.

Let’s see an example of creating a Markov network with three cliques in it.

```
from pomegranate import *

d1 = JointProbabilityTable([
    [0, 0, 0.1],
    [0, 1, 0.2],
    [1, 0, 0.4],
    [1, 1, 0.3]], [0, 1])

d2 = JointProbabilityTable([
    [0, 0, 0, 0.05],
    [0, 0, 1, 0.15],
    [0, 1, 0, 0.07],
    [0, 1, 1, 0.03],
    [1, 0, 0, 0.12],
    [1, 0, 1, 0.18],
    [1, 1, 0, 0.10],
    [1, 1, 1, 0.30]], [1, 2, 3])

d3 = JointProbabilityTable([
    [0, 0, 0, 0.08],
    [0, 0, 1, 0.12],
    [0, 1, 0, 0.11],
    [0, 1, 1, 0.19],
    [1, 0, 0, 0.04],
```

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```

    [1, 0, 1, 0.06],
    [1, 1, 0, 0.23],
    [1, 1, 1, 0.17]], [2, 3, 4])

model = MarkovNetwork([d1, d2, d3])
model.bake()

```

That was fairly simple. Each *JointProbabilityTable* object just had to include the table of all values that the variables can take as well as a list of variable indexes that are included in the table, in the order from left to right that they appear. For example, in *d1*, the first column of the table corresponds to the first column of data in a data matrix and the second column in the table corresponds to the second column in a data matrix.

One can also initialize a Markov network based completely on data. Currently, the only algorithm that pomegranate supports for this is the Chow-Liu tree-building algorithm. This algorithm first calculates the mutual information between all pairs of variables and then determines the maximum spanning tree through it. This process generally captures the strongest dependencies in the data set. However, because it requires all variables to have at least one connection, it can lead to instances where variables are incorrectly associated with each other. Overall, it generally performs well and it fairly fast to calculate.

```

from pomegranate import *
import numpy

X = numpy.random.randint(2, size=(100, 6))
model = MarkovNetwork.from_samples(X)

```

2.19.2 Probability

The probability of an example under a Markov network is more difficult to calculate than under a Bayesian network. With a Bayesian network, one can simply multiply the probabilities of each variable given its parents to get a probability of the entire example. However, repeating this process for a Markov network (by plugging in the values of each clique and multiplying across all cliques) results in a value called the “unnormalized” probability. This value is called “unnormalized” because the sum of this value across all combinations of values that the variables in an example can take does not sum to 1.

The normalization of an “unnormalized” probability requires the calculation of a partition function. This function (frequently abbreviated *Z*) is just the sum of the probability of all combinations of values that the variables can take. After calculation, one can just divide the unnormalized probability by this value to get the normalized probability. The only problem is that the calculation of the partition function requires the summation over a number of examples that grows exponentially with the number of dimensions. You can read more about this in the tutorial.

If you have a small number of variables (<30) it shouldn’t be a problem to calculate the partition function and then normalized probabilities.

```

>>> print(model.probability([1, 0, 1, 0, 1]))
-4.429966143312331

```

2.19.3 Prediction

Markov networks can be used to predict the value of missing variables given the observed values in a process called “inference.” In other predictive models there are typically a single or fixed set of missing values that need to be predicted, commonly referred to as the labels. However, in the case of Markov (or Bayesian) networks, the missing

values can be any variables and the inference process will use all of the available data to impute those missing values. For example:

```
>>> print(model.predict([[None, 0, None, 1, None]]))
[[1, 0, 0, 1, 1]]
```

2.19.4 API Reference

class pomegranate.MarkovNetwork.**MarkovNetwork**

A Markov Network Model.

A Markov network is an undirected graph where nodes represent variables, edges represent associations between the variables, and the lack of an edge represents a conditional independence.

Parameters

distributions [list, tuple, or numpy.ndarray] A collection of joint probability distributions that represent the

name [str, optional] The name of the model. Default is None

bake ()

Finalize the topology of the underlying factor graph model.

Assign a numerical index to every clique and create the underlying factor graph model. This method must be called before any of the probability-calculating or inference methods because the probability calculating methods rely on the partition function and the inference methods rely on the factor graph.

Parameters

calculate_partition [bool, optional] Whether to calculate the partition function. This is not necessary if the goal is simply to perform inference, but is required if the goal is to calculate the probability of examples under the model.

Returns

None

clear_summaries ()

Clear the summary statistics stored in the object.

copy ()

Return a deep copy of this distribution object.

This object will not be tied to any other distribution or connected in any form.

Parameters

None

Returns

distribution [Distribution] A copy of the distribution with the same parameters.

fit ()

Fit the model to data using MLE estimates.

Fit the model to the data by updating each of the components of the model, which are univariate or multivariate distributions. This uses a simple MLE estimate to update the distributions according to their summarize or fit methods.

This is a wrapper for the summarize and from_summaries methods.

Parameters

- X** [array-like, shape (n_samples, n_nodes)] The data to train on, where each row is a sample and each column corresponds to the associated variable.
- weights** [array-like, shape (n_nodes), optional] The weight of each sample as a positive double. Default is None.
- inertia** [double, optional] The inertia for updating the distributions, passed along to the distribution method. Default is 0.0.
- pseudocount** [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Only effects hidden Markov models defined over discrete distributions. Default is 0.
- verbose** [bool, optional] Whether or not to print out improvement information over iterations. Only required if doing semisupervised learning. Default is False.
- calculate_partition** [bool, optional] Whether to calculate the partition function. This is not necessary if the goal is simply to perform inference, but is required if the goal is to calculate the probability of examples under the model.
- n_jobs** [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

Returns

- self** [MarkovNetwork] The fit Markov network object with updated model parameters.

freeze ()

Freeze the distribution, preventing updates from occurring.

from_json ()

Read in a serialized Markov Network and return the appropriate object.

Parameters

- s** [str] A JSON formatted string containing the file.

Returns

- model** [object] A properly initialized and baked model.

from_samples ()

Learn the structure of the network from data.

Find the structure of the network from data using a Markov structure learning score. This currently enumerates all the exponential number of structures and finds the best according to the score. This allows weights on the different samples as well. The score that is optimized is the minimum description length (MDL).

If not all states for a variable appear in the supplied data, this function can not gurantee that the returned Markov Network is optimal when 'exact' or 'exact-dp' is used. This is because the number of states for each node is derived only from the data provided, and the scoring function depends on the number of states of a variable.

Parameters

- X** [array-like, shape (n_samples, n_nodes)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.
- weights** [array-like, shape (n_nodes), optional] The weight of each sample as a positive double. Default is None.

algorithm [str, one of ‘chow-liu’, ‘greedy’, ‘exact’, ‘exact-dp’ optional] The algorithm to use for learning the Bayesian network. Default is ‘greedy’ that greedily attempts to find the best structure, and frequently can identify the optimal structure. ‘exact’ uses DP/A* to find the optimal Bayesian network, and ‘exact-dp’ tries to find the shortest path on the entire order lattice, which is more memory and computationally expensive. ‘exact’ and ‘exact-dp’ should give identical results, with ‘exact-dp’ remaining an option mostly for debugging reasons. ‘chow-liu’ will return the optimal tree-like structure for the Bayesian network, which is a very fast approximation but not always the best network.

max_parents [int, optional] The maximum number of parents a node can have. If used, this means using the k-learn procedure. Can drastically speed up algorithms. If -1, no max on parents. Default is -1.

root [int, optional] For algorithms which require a single root (‘chow-liu’), this is the root for which all edges point away from. User may specify which column to use as the root. Default is the first column.

constraint_graph [networkx.DiGraph or None, optional] A directed graph showing valid parent sets for each variable. Each node is a set of variables, and edges represent which variables can be valid parents of those variables. The naive structure learning task is just all variables in a single node with a self edge, meaning that you know nothing about

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don’t happen to occur in the data. Default is 0.

name [str, optional] The name of the model. Default is None.

reduce_dataset [bool, optional] Given the discrete nature of these datasets, frequently a user will pass in a dataset that has many identical samples. It is time consuming to go through these redundant samples and a far more efficient use of time to simply calculate a new dataset comprised of the subset of unique observed samples weighted by the number of times they occur in the dataset. This typically will speed up all algorithms, including when using a constraint graph. Default is True.

n_jobs [int, optional] The number of threads to use when learning the structure of the network. If a constraint graph is provided, this will parallelize the tasks as directed by the constraint graph. If one is not provided it will parallelize the building of the parent graphs. Both cases will provide large speed gains.

Returns

model [MarkovNetwork] The learned Markov Network.

from_structure ()

Return a Markov network from a predefined structure.

Pass in the structure of the network as a tuple of tuples and get a fit network in return. The tuple should contain n tuples, with one for each node in the graph. Each inner tuple should be of the parents for that node. For example, a three node graph where both node 0 and 1 have node 2 as a parent would be specified as ((2,), (2,), ()).

Parameters

X [array-like, shape (n_samples, n_nodes)] The data to fit the structure too, where each row is a sample and each column corresponds to the associated variable.

structure [tuple of tuples] The parents for each node in the graph. If a node has no parents, then do not specify any parents.

weights [array-like, shape (n_nodes), optional] The weight of each sample as a positive double. Default is None.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Default is 0.

Returns

model [MarkovNetwork] A Markov network with the specified structure.

from_summaries ()

Use MLE on the stored sufficient statistics to train the model.

Parameters

inertia [double, optional] The inertia for updating the distributions, passed along to the distribution method. Default is 0.0.

pseudocount [double, optional] A pseudocount to add to the emission of each distribution. This effectively smoothes the states to prevent 0. probability symbols if they don't happen to occur in the data. Default is 0.

calculate_partition [bool, optional] Whether to calculate the partition function. This is not necessary if the goal is simply to perform inference, but is required if the goal is to calculate the probability of examples under the model.

Returns

None

from_yaml ()

Deserialize this object from its YAML representation.

log_probability ()

Return the log probability of samples under the Markov network.

The log probability is just the sum of the log probabilities under each of the components minus the partition function. This method will return a vector of log probabilities, one for each sample.

Parameters

X [array-like, shape (n_samples, n_dim)] The sample is a vector of points where each dimension represents the same variable as added to the graph originally. It doesn't matter what the connections between these variables are, just that they are all ordered the same.

n_jobs [int, optional] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

unnormalized [bool, optional] Whether to return the unnormalized or normalized probabilities. The normalized probabilities requires the partition function to be calculated.

Returns

logp [numpy.ndarray or double] The log probability of the samples if many, or the single log probability.

marginal ()

Return the marginal probabilities of each variable in the graph.

This is equivalent to a pass of belief propagation on a graph where no data has been given. This will calculate the probability of each variable being in each possible emission when nothing is known.

Parameters**None****Returns**

marginals [array-like, shape (n_nodes)] An array of univariate distribution objects showing the marginal probabilities of that variable.

predict ()

Predict missing values of a data matrix using MLE.

Impute the missing values of a data matrix using the maximally likely predictions according to the loopy belief propagation (also known as the forward-backward) algorithm. Run each example through the algorithm (predict_proba) and replace missing values with the maximally likely predicted emission.

Parameters

X [array-like, shape (n_samples, n_nodes)] Data matrix to impute. Missing values must be either None (if lists) or np.nan (if numpy.ndarray). Will fill in these values with the maximally likely ones.

max_iterations [int, optional] Number of iterations to run loopy belief propagation for. Default is 100.

n_jobs [int] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

Returns

y_hat [numpy.ndarray, shape (n_samples, n_nodes)] This is the data matrix with the missing values imputed.

predict_proba ()

Returns the probabilities of each variable in the graph given evidence.

This calculates the marginal probability distributions for each state given the evidence provided through loopy belief propagation. Loopy belief propagation is an approximate algorithm which is exact for certain graph structures.

Parameters

X [dict or array-like, shape \leq n_nodes] The evidence supplied to the graph. This can either be a dictionary with keys being state names and values being the observed values (either the emissions or a distribution over the emissions) or an array with the values being ordered according to the nodes incorporation in the graph and None for variables which are unknown. It can also be vectorized, so a list of dictionaries can be passed in where each dictionary is a single sample, or a list of lists where each list is a single sample, both formatted as mentioned before. The preferred method is as an numpy array.

max_iterations [int, optional] The number of iterations with which to do loopy belief propagation. Usually requires only 1. Default is 100.

check_input [bool, optional] Check to make sure that the observed symbol is a valid symbol for that distribution to produce. Default is True.

n_jobs [int, optional] The number of threads to use when parallelizing the job. This parameter is passed directly into joblib. Default is 1, indicating no parallelism.

Returns

y_hat [array-like, shape (n_samples, n_nodes)] An array of univariate distribution objects showing the probabilities of each variable.

probability ()

Return the probability of samples under the Markov network.

This is just a wrapper that exponentiates the result from the log probability method.

Parameters

X [array-like, shape (n_samples, n_dim)] The sample is a vector of points where each dimension represents the same variable as added to the graph originally. It doesn't matter what the connections between these variables are, just that they are all ordered the same.

n_jobs [int, optional] The number of jobs to use to parallelize, either the number of threads or the number of processes to use. -1 means use all available resources. Default is 1.

unnormalized [bool, optional] Whether to return the unnormalized or normalized probabilities. The normalized probabilities requires the partition function to be calculated.

Returns

prob [numpy.ndarray or double] The log probability of the samples if many, or the single log probability.

sample ()

Return a random item sampled from this distribution.

Parameters

n [int or None, optional] The number of samples to return. Default is None, which is to generate a single sample.

Returns

sample [double or object] Returns a sample from the distribution of a type in the support of the distribution.

score ()

Return the accuracy of the model on a data set.

Parameters

X [numpy.ndarray, shape=(n, d)] The values of the data set

y [numpy.ndarray, shape=(n,)] The labels of each value

summarize ()

Summarize a batch of data and store the sufficient statistics.

This will partition the dataset into columns which belong to their appropriate distribution. If the distribution has parents, then multiple columns are sent to the distribution. This relies mostly on the summarize function of the underlying distribution.

Parameters

X [array-like, shape (n_samples, n_nodes)] The data to train on, where each row is a sample and each column corresponds to the associated variable.

weights [array-like, shape (n_nodes), optional] The weight of each sample as a positive double. Default is None.

Returns

None

thaw()

Thaw the distribution, re-allowing updates to occur.

to_json()

Serialize the model to a JSON.

Parameters

separators [tuple, optional] The two separators to pass to the `json.dumps` function for formatting.

indent [int, optional] The indentation to use at each level. Passed to `json.dumps` for formatting.

Returns

json [str] A properly formatted JSON object.

to_yaml()

Serialize the model to YAML for compactness.

`pomegranate.MarkovNetwork.discrete_chow_liu_tree()`

Find the Chow-Liu tree that spans a data set.

The Chow-Liu algorithm first calculates the mutual information between each pair of variables and then constructs a maximum spanning tree given that. This algorithm slightly from the one implemented for Bayesian networks because Bayesian networks are directed and need a node to be the root. In contrast, the structure here is undirected and so is a simple maximum spanning tree.

2.20 Factor Graphs

2.20.1 API Reference

class `pomegranate.FactorGraph.FactorGraph`

A Factor Graph model.

A bipartite graph where conditional probability tables are on one side, and marginals for each of the variables involved are on the other side.

Parameters

name [str, optional] The name of the model. Default is `None`.

bake()

Finalize the topology of the model.

Assign a numerical index to every state and create the underlying arrays corresponding to the states and edges between the states. This method must be called before any of the probability-calculating methods. This is the same as the HMM `bake`, except that at the end it sets current state information.

Parameters

None

Returns

None

from_json()

Read in a serialized `FactorGraph` and return the appropriate instance.

Parameters

s: **str** A JSON formatted string containing the file.

Returns

model: **object** A properly instantiated and baked model.

marginal()

Return the marginal probabilities of each variable in the graph.

This is equivalent to a pass of belief propagation on a graph where no data has been given. This will calculate the probability of each variable being in each possible emission when nothing is known.

Parameters

None

Returns

marginals [array-like, shape (n_nodes)] An array of univariate distribution objects showing the marginal probabilities of that variable.

plot()

Draw this model's graph using NetworkX and matplotlib.

Note that this relies on networkx's built-in graphing capabilities (and not Graphviz) and thus can't draw self-loops.

See `networkx.draw_networkx()` for the keywords you can pass in.

Parameters

****kwargs** [any] The arguments to pass into `networkx.draw_networkx()`

Returns

None

predict_proba()

Returns the probabilities of each variable in the graph given evidence.

This calculates the marginal probability distributions for each state given the evidence provided through loopy belief propagation. Loopy belief propagation is an approximate algorithm which is exact for certain graph structures.

Parameters

data [dict or array-like, shape \leq n_nodes, optional] The evidence supplied to the graph. This can either be a dictionary with keys being state names and values being the observed values (either the emissions or a distribution over the emissions) or an array with the values being ordered according to the nodes incorporation in the graph (the order fed into `.add_states/add_nodes`) and `None` for variables which are unknown. If nothing is fed in then calculate the marginal of the graph.

max_iterations [int, optional] The number of iterations with which to do loopy belief propagation. Usually requires only 1.

check_input [bool, optional] Check to make sure that the observed symbol is a valid symbol for that distribution to produce.

Returns

probabilities [array-like, shape (n_nodes)] An array of univariate distribution objects showing the probabilities of each variable.

to_json()

Serialize the model to JSON

Parameters

separators: tuple, optional The two separators to pass to the `json.dumps` function for formatting.

indent: int, optional The indentation to use at each level. Passed to `json.dumps` for formatting.

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